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Habibi, Parsa; Rahbari, Ahmadreza; Blazquez, Samuel; Vega, Carlos; Dey, Poulumi; Vlugt, Thijs J.H.; Moulton, Othonas A.

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A New Force Field for OH⁻ for Computing Thermodynamic and Transport Properties of H₂ and O₂ in Aqueous NaOH and KOH Solutions

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Parsa Habibi, Ahmadreza Rahbari, Samuel Blazquez, Carlos Vega, Poulumi Dey, Thijs J. H. Vlugt, and Othonas A. Moulτος*



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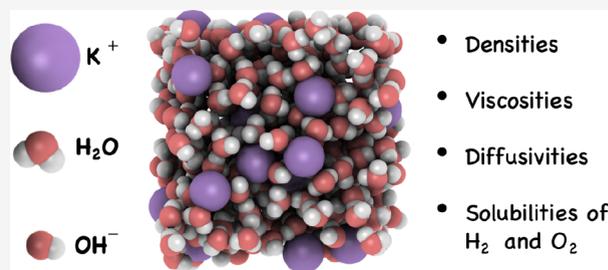


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ABSTRACT: The thermophysical properties of aqueous electrolyte solutions are of interest for applications such as water electrolyzers and fuel cells. Molecular dynamics (MD) and continuous fractional component Monte Carlo (CFCMC) simulations are used to calculate densities, transport properties (i.e., self-diffusivities and dynamic viscosities), and solubilities of H₂ and O₂ in aqueous sodium and potassium hydroxide (NaOH and KOH) solutions for a wide electrolyte concentration range (0–8 mol/kg). Simulations are carried out for a temperature and pressure range of 298–353 K and 1–100 bar, respectively. The TIP4P/2005 water model is used in combination with a newly parametrized OH⁻ force field for NaOH and KOH. The computed dynamic viscosities at 298 K for NaOH and KOH solutions are within 5% from the reported experimental data up to an electrolyte concentration of 6 mol/kg. For most of the thermodynamic conditions (especially at high concentrations, pressures, and temperatures) experimental data are largely lacking. We present an extensive collection of new data and engineering equations for H₂ and O₂ self-diffusivities and solubilities in NaOH and KOH solutions, which can be used for process design and optimization of efficient alkaline electrolyzers and fuel cells.



1. INTRODUCTION

Modeling aqueous alkaline solutions is of interest for a broad array of manufacturing and separation processes.^{1,2} Aqueous alkaline solutions containing potassium hydroxide (KOH) and sodium hydroxide (NaOH) are often used for electrolysis and in fuel cells due to their high ionic conductivities and low cost.^{3–7} NaOH and KOH have solubilities exceeding 18 mol/kg in water at 293 K (and above)^{8,9} and significantly influence the thermophysical properties of the solution.¹⁰ The interplay between different thermophysical properties (e.g., densities, viscosities, and ionic conductivities) of aqueous NaOH and KOH solutions influences the product gas purity, and the energy (and Faradaic) efficiency of alkaline-water electrolyzers.^{11–13} Knowledge of the thermodynamic and transport properties of hydrogen (H₂) and oxygen (O₂) gas in aqueous NaOH and KOH solutions is therefore highly relevant for optimization and process design of electrolyzers.^{12,14}

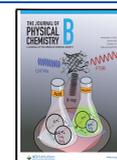
Modeling electrolyte systems is a challenging endeavor because of the strong long-range ionic interactions, which make the solutions highly nonideal.^{1,15–17} Electrolyte solutions are commonly modeled using semiempirical equations of state and molecular based simulations.^{1,15–26} Semiempirical equations provide a rapid and convenient method for the prediction

of thermophysical properties.¹⁵ The quality of these equations depends on the availability of accurate experimental and simulation data.^{18–22} For aqueous alkaline solutions, experimental data for self-diffusivities and solubilities of H₂ and O₂ at high concentrations (above 4 mol/kg), temperatures (323–373 K), and pressures (above 50 bar) is lacking, especially in the case of aqueous NaOH solutions.^{14,27} These temperatures (ca. 353 K) and concentrations (4–12 mol/kg electrolyte solution) are especially relevant for alkaline electrolyzers.^{3,7,28–30} Molecular simulations (i.e., molecular dynamics (MD) and Monte Carlo (MC)) can be used as a complementary approach to experiments³¹ to provide insight at conditions for which experimental data are limited and difficult to obtain due to high temperatures, pressures, and the

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corrosiveness of the solution (in case of strong alkaline solutions).

Molecular simulations of electrolyte systems can be studied using either ab initio simulations or force-field-based methods.^{1,32,33} Ab initio simulations have the potential to more accurately describe the structure and solvation of the ions,^{32,34} but these simulations are computationally expensive and are limited to systems comprising hundreds of atoms for time scales of the order of pico-seconds. To precisely calculate transport properties of fluids, long simulations of several nanoseconds are essential.^{24,35} To account for ion–ion and ion–water interactions at high electrolyte concentrations, water molecules need to be modeled explicitly,^{36,37} which makes the computations more costly. To overcome both the time and system-size restrictions of ab initio calculations, force-field-based methods are usually preferred for large-scale production of thermophysical data.

Force fields for aqueous electrolytes can be polarizable or nonpolarizable.^{38–41} The nonpolarizable TIP4P/2005 water model⁴² has proven to be quite suitable for predicting densities, viscosities, and self-diffusivities of water.^{42–44} In an attempt to model the effective charge screening that occurs in electrolyte solutions, ions are modeled as scaled charges in nonpolarizable force fields.¹ Prior research has demonstrated that the use of scaled charges significantly helps in capturing the correct dynamics of ions.^{38,45–47} Scaled charge models for ions such as Na⁺, K⁺, and Cl[−] have been developed by Zeron et al. (the so-called Madrid-2019 force field)^{38,47} and used in combination with the TIP4P/2005 water model.³⁸ These force fields yield reasonable predictions for densities, dynamic viscosities, and self-diffusivities of aqueous electrolytes with a scaled charge of 0.85 for concentrations up to 4 mol/kg salt.³⁸ However, the dynamic viscosities computed using the Madrid-2019 force field deviate from experiments at higher molalities. To address this, Vega and co-workers have developed a new force field called the Madrid-Transport with a scaled charge of 0.75.⁴⁷ This force field can accurately predict dynamic viscosities of aqueous NaCl and KCl solutions up to their solubility limit.⁴⁷ Despite the importance of alkaline systems, there is no Madrid-force field for OH[−] to accurately predict densities and dynamic viscosities of aqueous NaOH and KOH systems. Existing OH[−] force fields are often used to simulate the solvation energy^{48–50} and structure,^{51–56} and cannot be used directly in combination with the TIP4P/2005 water model and the Madrid-force fields^{38,47} for Na⁺ and K⁺ ions as they do not use scaled charges of −0.85 or −0.75.

Here, we propose several nonpolarizable two-site OH[−] force fields with scaled charges of −0.85 and −0.75, respectively. One of the newly proposed OH[−] force fields with a scaled charge of −0.75 yields accurate predictions for both densities and dynamic viscosities of aqueous NaOH and KOH solutions for concentrations ranging from 0 to 8 mol/kg, at temperatures ranging from 298 to 353 K. We use this force field to compute the self-diffusivities of H₂ and O₂ in aqueous NaOH and KOH solutions using MD. Solubilities of these gases as functions of concentrations, and temperatures, and pressures are computed using Continuous Fractional Component Monte Carlo (CFCMC) simulations.^{57–59} Our data, obtained from molecular simulations, are compared to available experimental data on H₂ and O₂ in KOH solutions. Our simulations can adequately describe the trends observed in experiments for variations in both concentration and temperature. The self-diffusivities and solubilities of H₂ and O₂ in NaOH and KOH

solutions are then fitted to semiempirical engineering equations. These engineering equations can be used for process modeling, and for optimizing electrolyzers and fuel cells.¹²

This paper is organized as follows. In section 2, details on the force fields are provided, and the molecular simulation (MD and MC) techniques are explained. In section 3, force field optimization of OH[−] is discussed, and the results for viscosities, H₂ and O₂ self-diffusivities, and solubilities at temperatures ranging from 298 to 353 K are provided. Our conclusions are summarized in section 4.

2. METHODOLOGY

2.1. Force Fields. The four-site TIP4P/2005 water model is used in all simulations.⁴² This model can accurately describe the densities and transport properties of pure H₂O and of gases dissolved in H₂O for a wide range of conditions.^{31,42–44,60,61} The two-site Bohn model⁶² is used for modeling O₂. For H₂, the single-site Vrabec model⁶³ and the three-site Marx model⁶⁴ are used. These force fields for H₂ and O₂ have shown to accurately describe gas diffusivities in pure water at various pressures and temperatures.³¹ The single-site H₂ Vrabec model is less computationally demanding (no bonds or angles) than the three-site Marx model and yields similar self-diffusivities in pure TIP4P/2005 water (see Figure S1). This force field is used for computing self-diffusivities of H₂ in NaOH and KOH solutions. The Marx model yields significantly more accurate H₂ solubilities than the Vrabec model in pure TIP4P/2005 water (see Figure S1) and is used for computing H₂ solubilities in NaOH and KOH solutions. For the K⁺ and Na⁺ ions, the Madrid-Transport (+0.75)⁴⁷ and Madrid-2019 (+0.85)³⁸ force fields are used (parameters listed in Table 1). For OH[−], several

Table 1. Force Field Parameters for the Na⁺ and K⁺ Models Used (Madrid-2019³⁸ and Madrid-Transport⁴⁷)^a

	Madrid-2019		Madrid-Transport	
	Na ⁺	K ⁺	Na ⁺	K ⁺
$q_M/[e]$	0.85	0.85	0.75	0.75
$\epsilon_{MM}/k_B/[K]$	177.08	238.83	177.08	238.83
$\sigma_{MM}/[Å]$	2.21737	2.30140	2.21737	2.30140
$\epsilon_{MO_w}/k_B/[K]$	95.42	168.43	95.42	168.43
$\sigma_{MO_w}/[Å]$	2.60838	2.89040	2.38725	2.89540

^a ϵ and σ are the Lennard-Jones parameters and q is the atomic partial charge. M refers to the Na⁺ or K⁺ atom. O_w refers to the O-atom of water (TIP4P/2005⁴² model). The Lorentz–Berthelot mixing rules^{65,66} are applied for all mixtures, with the exception of [Na/K – H₂O] LJ interactions as specified in this table.

force fields are proposed in this work. The details for OH[−] force field are discussed in section 3.1. All force fields considered in this work are rigid. All interaction parameters for the TIP4P/2005 water, H₂, and O₂ models are provided in the Supporting Information (Tables S1–S3). The Lennard-Jones (LJ) and Coulombic interactions are considered for modeling the intermolecular interactions. The Lorentz–Berthelot mixing rules^{65,66} are applied with the exception of [Na/K – H₂O] LJ interactions as specified in Table 1.

2.2. MD Simulations. MD simulations are carried out as implemented in the open-source Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS).⁶⁷ The Verlet algorithm,⁶⁸ with a time step of 1 fs, is used for integrating the

equations of motion. Periodic boundary conditions are imposed in all directions. For H₂O, O₂, and OH⁻, the SHAKE algorithm in LAMMPS^{67,69} is used to fix the bond lengths (and the bond angle of H₂O). Analytic tail corrections for energies and pressures are applied to the LJ part of the potential. The cutoff radius for both LJ and Coulombic potentials is set to 10 Å. The particle–particle particle-mesh (PPPM)^{66,70} method is used for long-range electrostatic interactions with a relative error of 10⁻⁵.

The OCTP tool⁷¹ is used in LAMMPS to calculate the transport properties. The simulations are initially equilibrated in the *NPT* and *NVT* ensembles for a period of ca. 2 ns. Production runs (in *NVT*) of 10–50 ns are used to calculate dynamic viscosities and self-diffusivities. To obtain an ensemble mean and a standard deviation, each calculation is repeated 5 times with a different random seed for the initial velocity. The Nosé–Hoover thermostat and barostat^{66,72,73} are used, with a coupling constant of 100 and 1000 fs, respectively. The modifications of the Nosé–Hoover for rigid bodies, proposed by Kamberaj,⁷⁴ are used in LAMMPS. The densities and transport properties are calculated in a simulation box containing 700 H₂O molecules. The corresponding numbers of NaOH and KOH molecules, in combination with the respective molarities are provided in Tables S4 and S5. All initial configurations are created using the PACKMOL software.⁷⁵ Two gas molecules (H₂ or O₂) (corresponding to infinite dilution) are used to calculate self-diffusivities of the gases in the aqueous NaOH and KOH solutions. All self-diffusivities, computed from mean-square displacements,⁷¹ are corrected for finite-size effects using the Yeh–Hummer equation:^{76–79}

$$D_i = D_i^{\text{MD}} + \frac{k_B T \xi}{6\pi\eta L} \quad (1)$$

where D_i^{MD} and D_i denote the self-diffusivities calculated by MD and corrected for finite-size effects for species i , respectively, k_B is the Boltzmann constant, T is the temperature (in K), ξ is a dimensionless number equal to 2.837298 for a cubic simulation box, and L is the length of the simulation box.^{76,78} The dynamic viscosities (η), obtained from the MD simulations, do not have finite-size effects.^{78,80–82} To ensure no precipitation takes place and to calculate radial distribution functions, simulations are also carried out for a larger box size with 4200 H₂O molecules for 10 ns.

2.3. CFCMC Simulations. The solubilities in this work are calculated using Henry coefficients (H).⁸³ The Henry coefficients for H₂ and O₂ in aqueous NaOH and KOH solutions are computed using MC simulations in the Continuous Fractional Component^{57–59} isobaric–isothermal (CFCNPT) ensemble. All MC simulations are carried out using the open-source Brick-CFCMC software.^{57,84,85} All molecules are considered as rigid, and only intermolecular LJ and Coulombic interactions are considered. A cutoff radius of 10 Å is used for both the LJ and Coulombic interactions. The Ewald summation with a relative precision of 10⁻⁶ is used for the electrostatics. Analytic tail corrections for energies and pressures are applied to the LJ part of the potential.⁶⁶ Periodic boundary conditions are imposed in all directions. All MC simulations contained 300 water molecules. For all the compositions considered, the corresponding numbers of NaOH and KOH molecules and the respective molarities are provided in Table S4 and S5. Simulations are carried out at

temperatures of 298, 323, 333, 343, and 353 K, at H₂ and O₂ pressures of 1, 50, and 100 bar.

To calculate the excess chemical potentials and solubilities of H₂ and O₂, “fractional” molecules are introduced. In contrast to “whole” or normal molecules, the interactions of “fractional” molecules with other molecules are scaled with a continuous order parameter λ (in the range of [0, 1]):^{57,86} $\lambda = 0$ indicates no interactions between the fractional and whole molecules (ideal gas), while $\lambda = 1$ indicates full interactions, corresponding to a “whole” or normal/unscaled molecule. For more details regarding the scaling of the interactions of fractional molecules the reader is referred to refs 87–89. A single fractional molecule of H₂ (and O₂) is used to calculate the excess chemical potentials of the respective molecules in the solution. All other molecules in the simulation are whole molecules. The Wang–Landau algorithm^{90,91} is used to construct a biasing weight function for λ ($W(\lambda)$). The biasing weight function helps in overcoming possible energy barriers in λ -space, to ensure a flat observed probability distribution.⁸³ 100 bins are used to obtain a histogram of λ values, thereby computing the probability of occurrence for each λ value. The Boltzmann average of any parameter (A) can be computed using⁸³

$$\langle A \rangle_{\text{Boltzmann}} = \frac{\langle A \exp[-W(\lambda)] \rangle}{\langle \exp[-W(\lambda)] \rangle} \quad (2)$$

The infinite dilution excess chemical potential ($\mu^{\text{ex},\infty}$) can be related to the Boltzmann sampled probability distribution of λ ($p(\lambda)$) using^{57,83}

$$\mu^{\text{ex},\infty} = -k_B T \ln \frac{p(\lambda = 1)}{p(\lambda = 0)} \quad (3)$$

where $p(\lambda = 1)$ and $p(\lambda = 0)$ are the Boltzmann sampled probability distribution of λ at 1 and 0, respectively. The molarity based Henry coefficient (H) is defined as⁸³

$$H = \lim_{f_i \rightarrow 0} \frac{f_i}{m_i/m_0} \quad (4)$$

in which f_i is the fugacity of a solute in the gas phase, m_i is the molarity of the gas in the solution (mol/L), and m_0 is set to 1 mol/L. The infinite dilution excess chemical potential of H₂ and O₂ can be related to the molarity based Henry coefficient using⁸³

$$H = m_0 R T \exp \left[\frac{\mu^{\text{ex},\infty}}{k_B T} \right] \quad (5)$$

where R is the universal gas constant. For all simulations, 4×10^5 equilibration cycles are carried out followed by 4×10^5 production cycles. A cycle refers to N number of trial moves, with N corresponding to the total number of molecules, with a minimum of 20. Trial moves are selected with the following probabilities: 1% volume changes, 35% translations, 29% rotations, 25% λ changes, and 10% reinsertions of the fractional molecules at random locations inside the simulation box. The maximum displacements for volume changes, molecule translations, rotations, and λ changes are adjusted to obtain ca. 50% acceptance of trial moves. For each condition (concentration, temperature, pressure), 20 independent simulations are performed. The final Boltzmann probability distributions of λ are averaged in blocks of 4 to obtain 5 independent averaged distributions. For all averaged distribu-

tions, the excess chemical potentials and Henry coefficients are calculated to obtain a mean value and the standard deviation. All the raw data for the MD and MC simulations are shown in Tables S6–S11.

3. RESULTS AND DISCUSSION

3.1. Force Field Optimization. To construct accurate models for aqueous NaOH and KOH solutions, four different

Table 2. Force Field Parameters for OH⁻^a

model	$q_{\text{O}}/[\text{e}]$	$q_{\text{H}}/[\text{e}]$	q_{OH}	$\sigma_{\text{OO}}/[\text{\AA}]$	$\epsilon_{\text{OO}}/k_{\text{B}}/[\text{K}]$	$\sigma_{\text{HH}}/[\text{\AA}]$	$\epsilon_{\text{HH}}/k_{\text{B}}/[\text{K}]$
FF1	-1.2181	+0.4681	-0.75	3.65	30.19	1.443	22.13
FF2	-1.3805	+0.5305	-0.85	3.85	30.19	1.443	22.13
FF3	-1.0500	+0.3000	-0.75	3.55	30.19	1.443	22.13
FF4	-0.9750	+0.2250	-0.75	3.45	30.19	1.443	22.13

^aThe bond length of O–H is set to 0.98 Å. For all models, the sigma for H (σ_{HH}) is set to 1.443 Å.⁵² The Lennard-Jones ϵ parameters for O and H ($\epsilon_{\text{OO}}/k_{\text{B}}$, $\epsilon_{\text{HH}}/k_{\text{B}}$) are based on refs 52 and 56 and are set to 30.19 and 22.13 K, respectively, for all the models. The FF1 force field for OH⁻ is recommended.

two-site OH⁻ (i.e., O ^{δ^-} and H ^{δ^+}) force fields are considered (FF1–FF4) combined with the TIP4P/2005 water⁴² and the Madrid-2019³⁸ or Madrid-Transport⁴⁷ force fields for Na⁺ and K⁺. These force fields and their corresponding parameters are listed in Table 2. For all OH⁻ models, the O–H bond length is set to 0.98 Å, similar to the works of refs 52 and 53. FF1, FF3, and FF4 have a total scaled charge (q_{OH}) of -0.75 on OH⁻, while FF2 has a total scaled charge of -0.85. These force fields are used in combination with the Madrid-Transport (+0.75)⁴⁷ and Madrid-2019 (+0.85)³⁸ Na⁺ and K⁺ models such that the total charge of NaOH and KOH clusters becomes 0. The charge of OH⁻ is distributed on the O (q_{O}) and H (q_{H}) atom. For FF1 and FF2, the charges on the O and H atoms have the same ratios as in the work by Botti et al. on the structure of concentrated NaOH solutions.⁵² The charge distributions of the FF3 and FF4 models are based on Quantum Theory of Atoms in Molecules (QTAIM) calculations for OH⁻, which have indicated that the O atom can have an unscaled charge of

-1.4 to -1.3.⁹² For this reason, for the FF3 and FF4 models, the charge on the O atom are set to -1.4×0.75 and -1.3×0.75 , respectively. The charge on the H atom (q_{H}) is set such that $q_{\text{O}} + q_{\text{H}} = q_{\text{OH}}$. For each force field, the Lennard-Jones σ parameter of the O atom (σ_{OO}) is adjusted based on the experimental densities of aqueous NaOH and KOH solutions.^{10,93,94}

Figure 1 shows the variation of densities as functions of electrolyte concentrations for both NaOH and KOH. By adjusting the value of σ_{OO} , it is possible to obtain an excellent agreement for all the different models. All the densities obtained deviate less than 2% from experimental fits found in literature. A larger negative charge on O (q_{O}) results in a larger optimum σ_{OO} parameter, to counteract the strong attractive Coulombic interactions. The experimental fits of Olsson⁹⁴ (for densities and viscosities of aqueous NaOH), Gilliam⁹³ (densities of aqueous KOH), and Guo⁹⁵ (viscosities of aqueous KOH) are used and shown as lines in Figure 1.

The dynamic viscosities of aqueous NaOH and KOH solutions calculated using FF1–FF4 are shown in Figure 2. It can be observed that the choice of the total charge (q_{OH}), and the resulting σ_{OO} has a significant influence on the viscosities, especially at higher concentrations in which the influence of ion–ion interactions become more important. The influence of ion size on the viscosities and densities is shown in Figure S2. In case of FF2 (with $q_{\text{OH}} = -0.85$), the dynamic viscosity is overestimated by more than a factor 3 compared to the experimental fit for the highest concentration of NaOH. For aqueous KOH, the FF2 model overestimates the dynamic viscosity by around 40% at the highest concentration of KOH. The FF1, FF3, and FF4 models with $q_{\text{OH}} = -0.75$ show a much better agreement with the experimental fit. The findings of the Madrid-Transport model for aqueous NaCl and KCl solutions⁴⁷ also show that a scaled charge of 0.75 leads to better predictions of transport properties (especially at concentrations above 4 mol/kg salt) compared to a scaled charge of 0.85. Overall, the FF1 model shows the best agreement with the experimental viscosities and densities. For this reason, only the results of the FF1 model will be used and discussed further in this work.

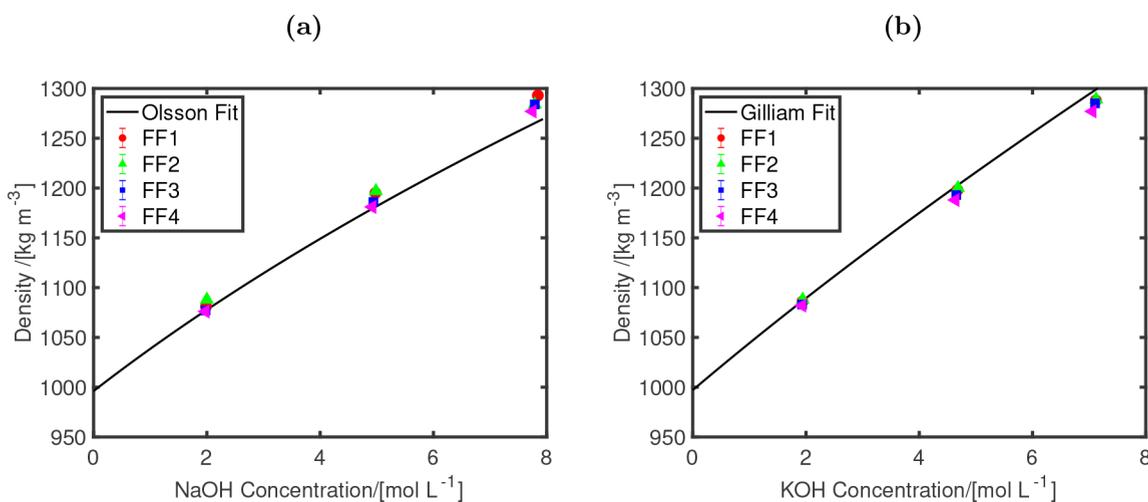


Figure 1. Densities at 298 K and 1 bar as functions of the electrolyte concentrations for (a) NaOH and (b) KOH. Four different OH⁻ force fields are considered (FF1–FF4) and compared to experimental fits (shown as lines) of Olsson⁹⁴ (for NaOH) and Gilliam^{10,93} (for KOH). The different parameters used for all the force fields are listed in Table 2.

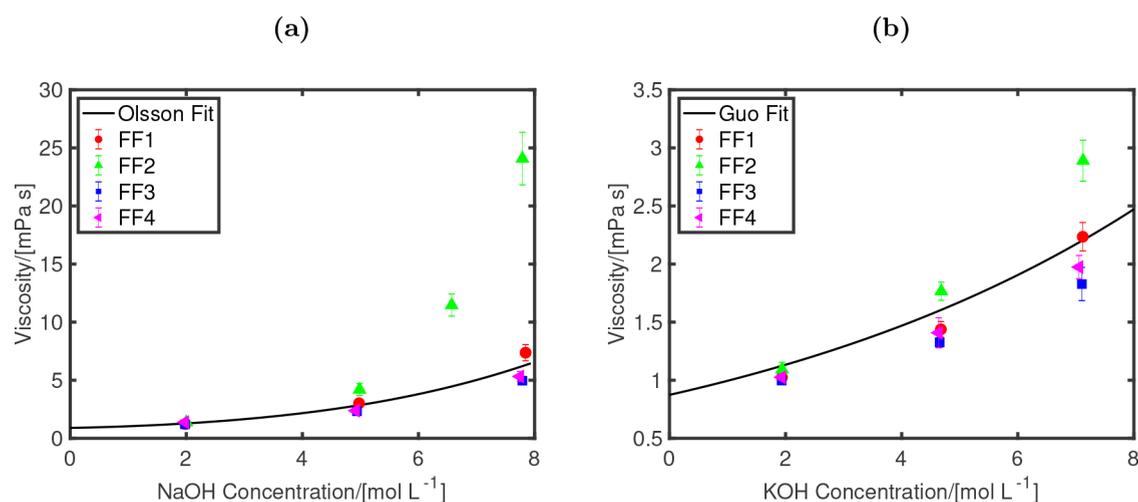


Figure 2. Dynamic viscosities at 298 K and 1 bar as functions of the electrolyte concentrations for (a) NaOH, and (b) KOH. Four different OH[−] force fields are considered (FF1–FF4) and compared to experimental fits (shown as lines) of Olsson⁹⁴ (for NaOH) and Guo⁹⁵ (for KOH). The different parameters used for all the force fields are listed in Table 2.

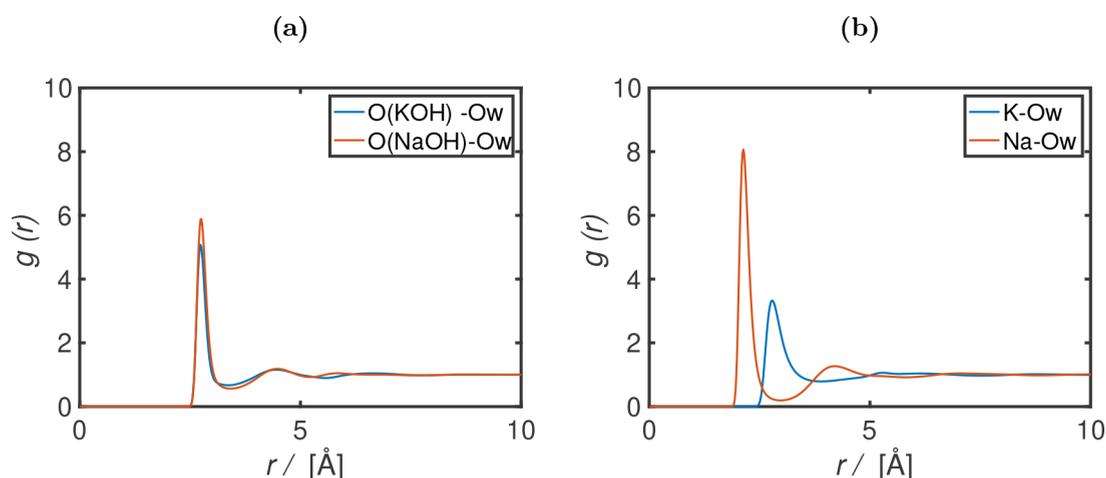


Figure 3. Radial distribution functions ($g(r)$) for (a) O(KOH)–O_w (O of water) and O(NaOH)–O_w and (b) K⁺(KOH)–O_w and Na⁺(NaOH)–O_w, as a function of radial distance r (Å), at 298 K, 1 bar, and a concentration of 5 mol/kg (corresponding to a molarity of 4.98 mol/L for NaOH, and 4.68 mol/L for KOH). The FF1 OH[−] model, in combination with the TIP4P/2005 water model⁴² and the Madrid-Transport Na⁺ and K⁺ models,⁴⁷ are used for the MD simulations.

Table 3. Finite Size-Corrected (Using eq 1) Self-Diffusivities of Cations (D_{cation}) (Na⁺, K⁺) and OH[−] (D_{OH^-}) at Different Molalities of 1.99 and 0.48 mol/kg Calculated Using MD^a

	$D_{\text{cation}}/[10^{-9} \text{ m}^2 \text{ s}^{-1}]$		$D_{\text{OH}^-}/[10^{-9} \text{ m}^2 \text{ s}^{-1}]$	
	MD	expt	MD	expt
molality (mol/kg)	1.99	0.48	0	0
NaOH	1.02	1.36	1.33	0.90
KOH	1.59	1.95	1.96	1.17
			1.09	1.23
				5.27

^aA comparison is made with experimental diffusion coefficients at infinite dilution of ions.⁹⁷ The FF1 OH[−] model, in combination with the TIP4P/2005 water model⁴² and the Madrid-Transport Na⁺ and K⁺ models,⁴⁷ are used for the MD simulations.

The radial distribution functions (RDFs) for anion–O_w (O of water) and cation–O_w are shown in Figure 3. The RDFs for the anion–anion, anion–cation, and cation–cations are shown in Figure S3. Based on the RDFs, the hydration numbers (n_{hyd}) are calculated using³⁸

$$n_{\text{hyd}} = 4\pi\rho_w \int_0^{r_{\text{min}}} g_w(r)r^2 dr \quad (6)$$

where g_w is the anion/cation–O_w RDF, r is the radial distance, r_{min} is the position of the first minimum in the RDF, and ρ_w is the number density of water in the solution. Our results show a first peak at approximately 2.13 and 2.79 Å for Na⁺–O_w and K⁺–O_w, respectively. The cation hydration numbers are 4.9 and 7.2 for Na⁺ and K⁺, respectively, at a molality of 5 mol/kg (corresponding to a molarity of 4.98 mol/L for NaOH, and 4.68 mol/L for KOH). Crystallization of ions is not observed for all our MD simulations of 10–50 ns based on the RDFs. Experimental and simulation results in literature suggest a first RDF peak at approximately 2.4–2.5 Å^{33,52,55} for Na⁺–O_w and a peak at approximately 2.7–2.8 Å for K⁺–O_w.⁵³ The reported hydration numbers (in the first shell) are in the ranges of 4–8 and 6–8 for Na⁺ and K⁺, respectively.⁹⁶ For OH[−], the results show a first peak at approximately 2.75 Å for OH[−]–O_w, with hydration numbers of 4.8 and 5.9 for KOH and NaOH, respectively, at a molality of 5 mol/kg. Other molecular simulations in literature report a first peak ranging from 2.3 to

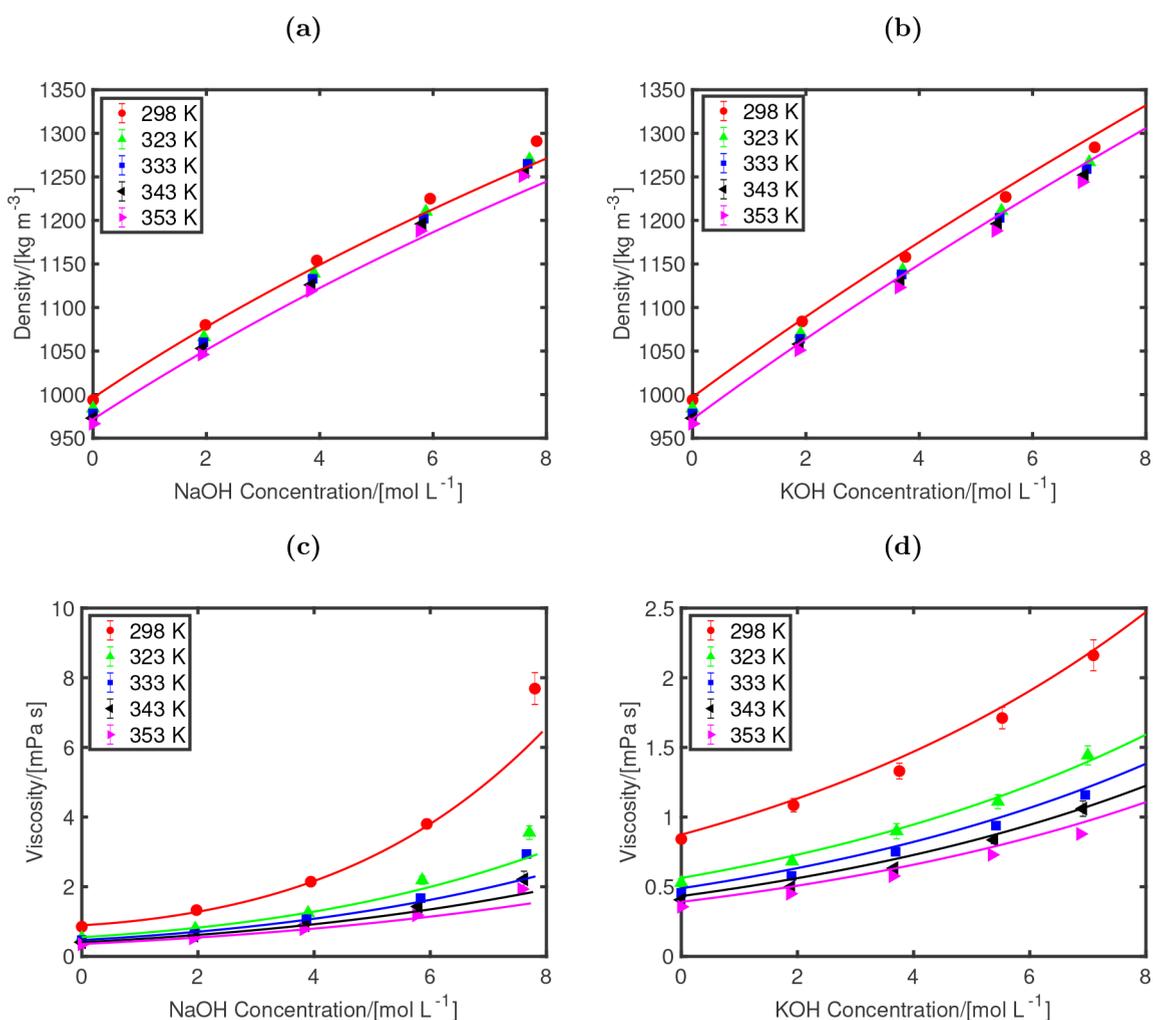


Figure 4. Densities (a, b) and dynamic viscosities (c, d) as functions of concentrations (mol/L) for aqueous NaOH (a, c) and KOH (b, d) at 1 bar. The simulation results at temperatures 298 (red), 323 (green), 333 (blue), 343 (black), and 353 (purple) K are shown. The lines represent experimental correlations. For densities, the Olsson⁹⁴ and Gilliam correlations⁹³ at 298 (red) and 353 (purple) K are shown. For viscosities, the Olsson⁹⁴ (NaOH) and Guo⁹⁵ (KOH) correlations are plotted for all temperatures with the same color scheme as the simulation points. The FF1 OH⁻ model, in combination with the TIP4P/2005 water model⁴² and the Madrid-Transport Na⁺ and K⁺ models,⁴⁷ is used for the MD simulations.

2.7 Å for the first OH⁻-O_W peak.^{33,52,55} The combined Car-Parrinello MD and X-ray diffraction studies of Megyes et al. for aqueous NaOH report a OH⁻-O_W distance ranging from 2.65 to 2.70 Å, with hydration numbers ranging from 3 to 5.³³ Overall, our force field results show agreement with other studies, albeit slightly overpredicting the first OH⁻-O_W peak and the hydration.

The self-diffusivities of NaOH and KOH are listed in Table 3. Even though for Na⁺ and K⁺ the self-diffusivities at infinite dilution are close, this is not the case for OH⁻ (underestimated by a factor ca. 5). For reasonable values of σ_{O_0} , ϵ_{O_0} , and q_{O} , we could not obtain OH⁻ self-diffusivities close to the values reported by experiments⁹⁷ without causing significant deviations from experimental densities and viscosities. This result is expected as classical OH⁻ models cannot capture the details of the solvation of OH⁻ in water and the proton transfer mechanism, which lead to anomalously high OH⁻ mobilities as discussed by Tuckerman et al.^{34,98} As such, our model, similarly to other classical force fields, is not suitable for predicting OH⁻ diffusivities of NaOH and KOH. Since electrical conductivities vastly depend on the mobility of the OH⁻ ions in the solution, the new OH⁻ model presented here

is unable to accurately predict electrical conductivities of aqueous NaOH and KOH solutions. Although our classical force field cannot capture the proton transfer mechanism, it can correctly predict the dynamic viscosities of the electrolyte solutions. As the aim of this study is to study the transport properties and solubilities of H₂ and O₂ gas in aqueous NaOH and KOH electrolytes, correct predictions of densities and viscosities are sufficient. Developing an OH⁻ force field by taking into account the proton transfer mechanism and accurate OH⁻ mobilities is beyond the scope of this work as quantum mechanical based force fields will be required.

3.2. Densities and Viscosities. It is important to show that the NaOH and KOH models (FF1 OH⁻ model, and the Madrid-Transport models of Na⁺, and K⁺)⁴⁷ can accurately predict the temperature-dependence of densities and viscosities. Figure 4 shows the densities and viscosities at different temperatures for both NaOH and KOH solutions. The agreement between MD simulations and experimental fits is excellent for aqueous KOH. For aqueous NaOH solutions, the results of densities are overestimated by ca. 2% and for dynamic viscosities by ca. 20% at the highest concentration (molality 8 mol/kg). Despite this, the trends of densities and

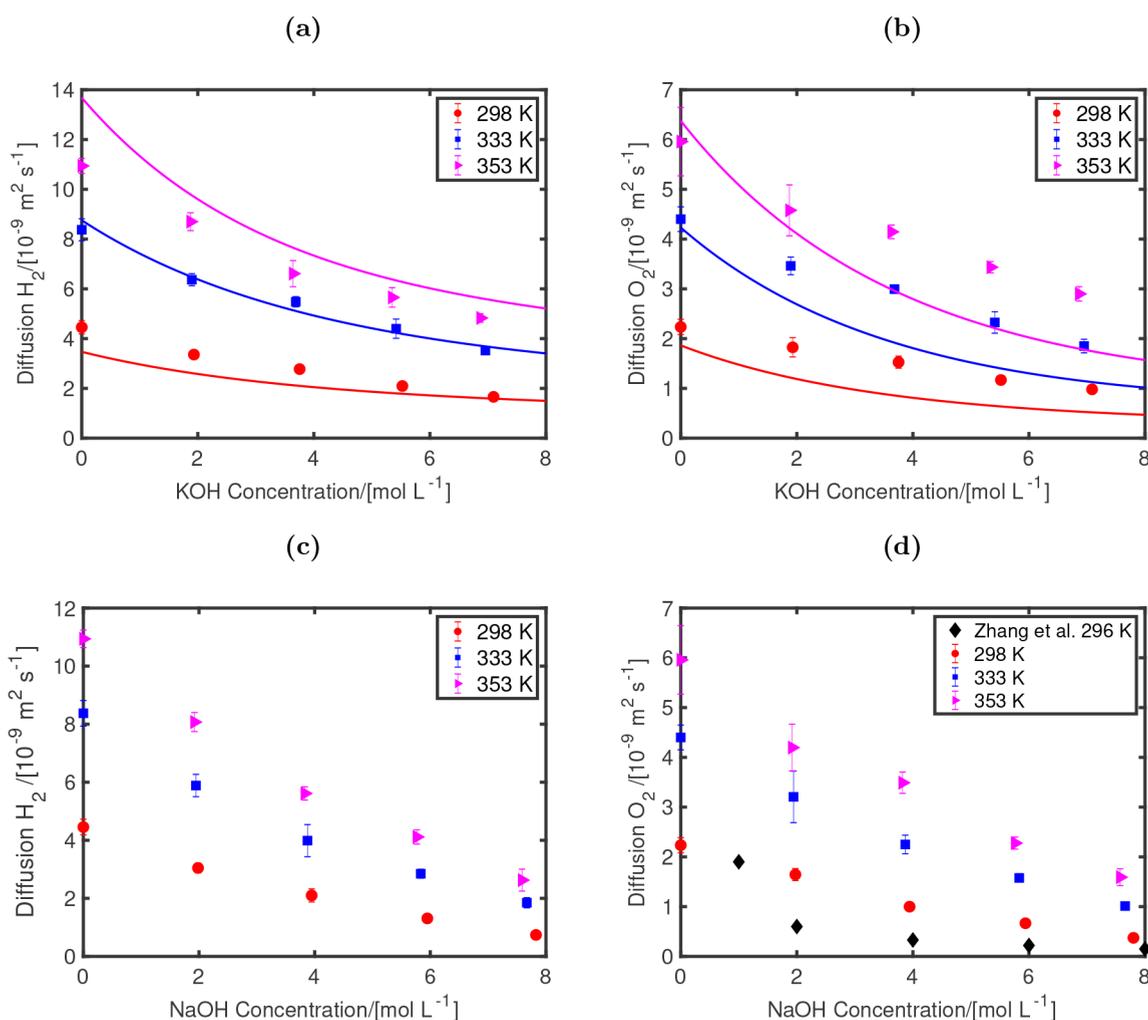


Figure 5. H_2 (a, c) and O_2 (b, d) self-diffusivities as functions of KOH (a, b) and NaOH (c, d) concentrations at different temperatures (298, 333, and 353 K) at 1 bar. For diffusivities of H_2 and O_2 in the KOH solution, the experimental data of Tham et al.^{27,99} at 298 (red), 333 (blue), and 353 K (purple) are fitted using eq 4 and shown in (a) and (b) as lines. The fitting coefficients of these data are shown in Table 4. The experimental diffusivities of O_2 in NaOH solution at 296 K (black) provided by Zhang et al.¹⁴ are plotted as points. The FF1 OH^- model, in combination with the TIP4P/2005 water model,⁴² the Bohn O_2 model,⁶² the Vrabec H_2 model,⁶³ and the Madrid-Transport Na^+ and K^+ models,⁴⁷ is used for the MD simulations.

Table 4. Fitting Parameters for eq 7 for H_2 and O_2 Self-Diffusivities in Aqueous NaOH and KOH Solutions^a

	a_0	a_1	a_2	a_3	a_4
H_2 -KOH (expt)	0.4066	-0.5903	0.4748	-0.1421	2.288
O_2 -KOH (expt)	0.2625	-0.5124	0.4345	-0.1278	2.201
H_2 -KOH (MD)	3.844	-5.006	3.686	-1.511	1.606
O_2 -KOH (MD)	1.511	-2.092	2.483	-1.743	1.701
H_2 -NaOH (MD)	3.344	-5.725	4.649	-2.103	1.648
O_2 -NaOH (MD)	1.313	-2.105	1.604	-0.7482	1.743

^aThe values for a_0 (in units of 10^{-11} m^2/s), a_1 (in units of 10^{-12} m^2/s (L/mol)), a_2 (in units of 10^{-13} m^2/s (L/mol)²), a_3 (in units of 10^{-14} m^2/s (L/mol)³), and a_4 (in units of 10^{-2} K^{-1}) are shown for both the MD simulations obtained in this work (range of validity: 0–8 mol/L, 298–353 K), and the experimental work of Tham et al. (at 298, 333, and 353 K) for H_2 and O_2 diffusion coefficient in KOH solutions (range of validity: 0–14 mol/L). The FF1 OH^- model, in combination with the TIP4P/2005 water model, the Bohn O_2 model, the Vrabec H_2 model, and the Madrid-Transport Na^+ and K^+ models is used for the MD simulations.

viscosities for variations of electrolyte concentration and temperature are well-predicted by the MD simulations using the new force fields. Densities and viscosities show a much weaker dependence on pressure (in the range of 1 to 100 bar) compared to temperature (in the range of 298 to 353 K) due to the incompressibility of the liquid phase. The variations of densities and viscosities as a function of pressure are shown in Figure S4.

3.3. Self-Diffusivities of H_2 and O_2 in Aqueous NaOH and KOH. The finite size-corrected self-diffusivities (using eq 1) of H_2 and O_2 in aqueous NaOH and KOH solutions calculated using MD simulations at various temperatures are shown in Figure 5. The results obtained by our MD simulations for the KOH solution are compared to the experimental data of Tham et al.^{27,99} at different temperatures, i.e., 298, 333, and 353 K. For H_2 self-diffusivities, our results are in quantitative agreement with the results of Tham et al.^{27,99} The increase in H_2 and O_2 diffusivities at higher temperatures are well-predicted. These trends are linked to the decrease of the dynamic viscosities of the solutions, which the MD simulations capture correctly. In our simulations for O_2 ,

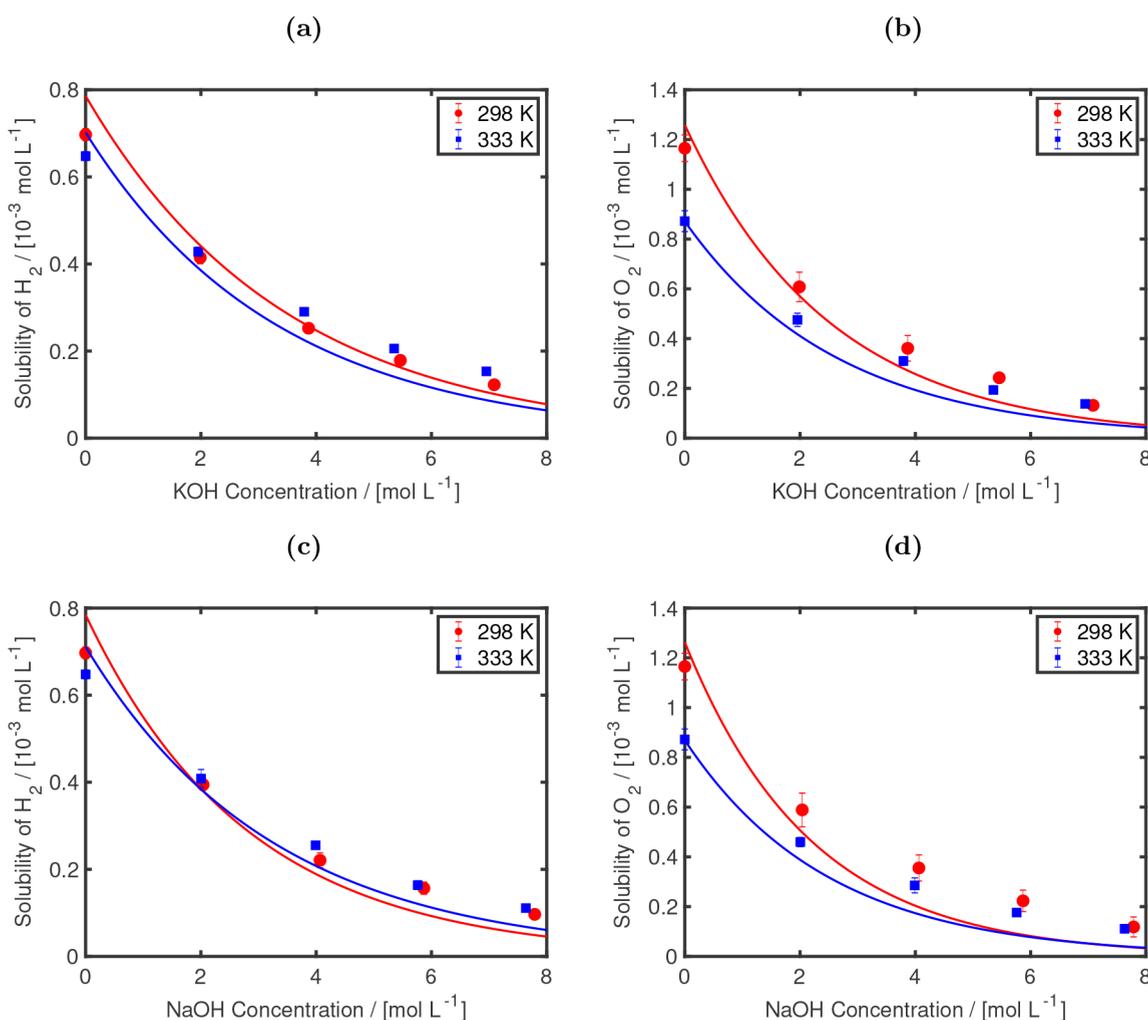


Figure 6. H_2 (a, c) and O_2 (b, d) solubilities as functions of KOH (a, b) and NaOH (c, d) concentrations at different temperatures of 298, and 333 K at 1 bar. For solubilities of H_2 and O_2 in KOH solutions, the experimental data of Walker et al.⁹⁹ at 298 (red), and 333 K (blue) is fitted using eq 8 and shown in (a) and (b) as lines. The fitting coefficients are shown in Table 5. For H_2 and O_2 solubilities in NaOH solutions, the Sechenov model^{100,101} (using the parameters provided by Weisenberger et al.¹⁰¹), and the experimental solubilities in pure water⁹⁹ are used to obtain the experimental fits, which are shown as lines. The FF1 OH^- model, in combination with the TIP4P/2005 water model,⁴² the Bohn O_2 model,⁶² the Marx H_2 model,⁶⁴ and the Madrid-Transport Na^+ and K^+ models,⁴⁷ is used for the MC simulations.

Table 5. Fitting Parameters for eq 8 for the H_2 and O_2 Solubilities (mol/L) in NaOH and KOH Solution^a

	f_0	f_1	f_2	f_3	f_4
H_2 -KOH (expt)	-1.944	-3.167	9.517	-5.337	8.078
O_2 -KOH (expt)	-5.712	5.854	16.961	-8.993	12.494
H_2 -KOH (MC)	-5.468	10.077	4.874	-2.526	3.773
O_2 -KOH (MC)	-5.670	8.889	13.935	-7.331	10.218
H_2 -NaOH (MC)	-4.749	7.241	4.874	-2.526	3.773
O_2 -NaOH (MC)	-4.093	4.057	13.935	-7.331	10.218

^aThe values for f_0 (10^{-1} (L/mol)), f_1 (10^{-4} (L/mol) K^{-1}), f_2 (10^{-3} (mol/L)), f_3 (10^{-5} (mol/L) K^{-1}), and f_4 (10^{-8} (mol/L) K^{-1}) are shown for both the MC simulations obtained in this work (range of validity: 0–8 mol/L, 298–353 K), and the experimental work of Walker et al. (at 298, 333, and 353 K) for H_2 and O_2 solubilities in KOH solutions (range of validity: 0–14 mol/L). The FF1 OH^- model, in combination with the TIP4P/2005 water model, the Bohn O_2 model, the Marx H_2 model, and the Madrid-Transport Na^+ and K^+ models, is used for the MC simulations.

the decay in the self-diffusivities with respect to variations of KOH concentrations are underpredicted with respect to the

experimental data. Zhang et al.¹⁴ report experimental O_2 diffusivities in aqueous NaOH at 296 K. Although the results of Zhang et al.¹⁴ for O_2 diffusivity at 1 mol/L NaOH is in agreement to ours, at 2 mol/L their results show a sharp decrease of the O_2 diffusivities by approximately a factor 1/3 with respect to diffusivities at 1 mol/L NaOH.¹⁴ This sharp decline is not observed in our calculations. However, the current force field models have managed to qualitatively predict the trends for a wide concentration (0–8 mol/kg) and temperature (298–353 K) range. For H_2 self-diffusivities in aqueous NaOH no experimental data at these different temperatures are found. Thus, our simulations serve as a first prediction for these data.

The simulation results (at 298, 323, 333, 343, and 353 K) in this work (shown in Figure S5), and the experimental data of Tham et al. (at 298, 333, and 353 K)^{27,99} are fitted to an engineering equation with an Arrhenius-inspired term for temperature variations:

$$D_i = (a_0 + a_1C + a_2C^2 + a_3C^3) \exp(a_4T) \quad (7)$$

where D_i is the self-diffusivity of H_2 and O_2 in NaOH and KOH solutions, a_0 – a_4 are fitting constants, C is the electrolyte concentration (in mol/L), and T is the temperature (in K). All fitting parameters for H_2 and O_2 in the aqueous NaOH and KOH solutions are listed in Table 4. Equation 7 provides an excellent fit for both the simulation results found in this work and the experimental data of Tham et al.²⁷ as shown in Figure S5.

3.4. Solubilities of H_2 and O_2 in Aqueous NaOH and KOH. In Figure 6, the H_2 and O_2 solubilities obtained using CFMCM calculations are shown as functions of NaOH and KOH concentrations. In this figure, only the results at 298 and 333 K are shown as solubilities (especially at higher electrolyte concentrations) vary only weakly in the temperature range of 298–353 K. The solubilities of H_2 and O_2 at 298, 323, 333, 343, and 353 K are shown in Figure S7.

As a comparison the experimental data provided by Walker et al.⁹⁹ on the solubilities of H_2 and O_2 in aqueous KOH are fitted and plotted in Figure 6a,b. This experimental data are also in agreement with the experiments of Davis et al.¹⁰² for O_2 solubilities (at 298 and 333 K) and with the Sechenov model.¹⁰¹ The Sechenov model¹⁰⁰ (with the parameters provided by Weisenberger et al.)¹⁰¹ is an empirical model, which predicts the salting out effect^{103,104} at different temperatures (273–363 K) and electrolyte concentrations.¹⁰¹ For NaOH, our data are compared to the Sechenov model as direct experimental data at these two temperatures are not available. Zhang et al.¹⁴ report solubilities of O_2 in aqueous NaOH at 296 K. Our simulations show agreement with data and experimental fits for both H_2 and O_2 . Both the salting out phenomena and the temperature trends are captured by our simulations. At low electrolyte concentrations (below 2 mol/L), increasing the temperature from 298 to 333 K leads to slightly lower H_2 and O_2 solubilities. At higher molarities, the solubilities become less dependent on the temperature and the concentration of the salts dominate the solubilities. The simulation results and experimental data of Walker et al.⁹⁹ for H_2 and O_2 solubilities in aqueous KOH and NaOH are fitted to a Sechenov-based¹⁰¹ engineering equation:

$$\ln\left(\frac{C_G}{C_{G,0}}\right) = (f_0 + f_1 T)C \quad (8)$$

where C_G and $C_{G,0}$ are the solubility of the gas in the electrolyte and pure water at 1 bar, respectively. f_0 and f_1 are fitting constants. The temperature dependence of the parameter $C_{G,0}$ can be fitted as

$$C_{G,0} = f_2 + f_3 T + f_4 T^2 \quad (9)$$

where f_2 – f_4 are additional fitting parameters. The optimized fitting parameters for MC simulations in this work and the experimental data of Walker et al. for H_2 and O_2 solubilities are shown in Table 5. Equation 8 provides an excellent fit for both the simulation results found in this work and the experimental data present in the literature, as shown in Figure S7.

4. CONCLUSIONS

The self-diffusivities and solubilities of H_2 and O_2 in aqueous NaOH and KOH solutions are modeled using MD and CFMCM simulations. A new two-site nonpolarizable OH^- force field (FF1 model) is proposed with a scaled charge of -0.75 , which matches with the TIP4P/2005 water and the

Madrid-Transport models for Na^+ and K^+ . Although our classical force field cannot capture the proton transfer mechanism, which influences the OH^- diffusivities, it can predict the densities, dynamic viscosities, and the salting out of H_2 and O_2 in aqueous NaOH and KOH solutions. Excellent agreement is observed between simulation and experimental data for both densities and dynamic viscosities of NaOH and KOH for a concentration range of 0–6 mol/kg and a temperature range of 298–353 K. This model is used to generate self-diffusivity and solubility data for H_2 and O_2 in aqueous NaOH and KOH solutions for a temperature range of 298–353 K and a concentration range of 0–8 mol/kg. The computed data and existing experimental results are used to fit engineering equations. The obtained data and engineering equations can be used for process modeling and optimizing electrolyzers and fuel cells.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcb.2c06381>.

Comparison of the Marx⁶⁴ and Vrabec⁶³ H_2 force fields for the prediction of H_2 self-diffusivities (finite-size corrected⁷⁸) and solubilities in pure TIP4P/2005 water; influence of OH^- ion size on densities, and viscosities at 1 bar and 298 K; radial distribution functions (RDFs) of cation–anion, cation–anion, and anion–anion of NaOH and KOH solutions at 1 bar and 298 K; variation of densities and dynamic viscosities for a pressure range of 1–100 bar at 298 K for different concentrations of aqueous NaOH and KOH; engineering fits for experimental and simulation data for diffusivities of H_2 and O_2 in aqueous NaOH and KOH solutions; solubilities of H_2 and O_2 for a pressure range of 1–100 bar at 298 K in pure water calculated using Monte Carlo simulations; engineering fits for experimental and simulation data for solubilities of H_2 and O_2 in aqueous NaOH and KOH solutions; force field details for TIP4P/2005 water,⁴² Vrabec⁶³ H_2 , Marx⁶⁴ H_2 , and Bohn⁶² O_2 ;³⁸ number of Na^+ and K^+ ions used for molecular dynamics and Monte Carlo simulations and the respective electrolyte weight percentages (wt %), molalities, and molarities (at 298 K and 1 bar); raw data for densities, viscosities, and self-diffusivities of H_2 and O_2 at various temperatures and concentrations of aqueous KOH at 1 and 100 bar; raw data for densities, viscosities, and self-diffusivities of H_2 and O_2 at various temperatures and concentrations of aqueous NaOH at 1 and 100 bar; raw data for excess chemical potentials, Henry coefficients, and solubilities of H_2 and O_2 at various temperatures and concentrations of aqueous KOH and NaOH at 1 bar (PDF)

■ AUTHOR INFORMATION

Corresponding Author

Othonas A. Moulτος – *Engineering Thermodynamics, Process & Energy Department, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CB Delft, The Netherlands*; orcid.org/0000-0001-7477-9684; Email: O.moultos@tudelft.nl

Authors

Parsa Habibi – Engineering Thermodynamics, Process & Energy Department, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CD Delft, The Netherlands; Department of Materials Science and Engineering, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CD Delft, The Netherlands

Ahmadreza Rahbari – Engineering Thermodynamics, Process & Energy Department, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CD Delft, The Netherlands; orcid.org/0000-0002-6474-3028

Samuel Blazquez – Depto. Química Física, Fac. Ciencias Químicas, Universidad Complutense de Madrid, 28040 Madrid, Spain; orcid.org/0000-0002-6218-3880

Carlos Vega – Depto. Química Física, Fac. Ciencias Químicas, Universidad Complutense de Madrid, 28040 Madrid, Spain; orcid.org/0000-0002-2417-9645

Poulumi Dey – Department of Materials Science and Engineering, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CD Delft, The Netherlands; orcid.org/0000-0003-4679-1752

Thijs J. H. Vlugt – Engineering Thermodynamics, Process & Energy Department, Faculty of Mechanical, Maritime and Materials Engineering, Delft University of Technology, 2628 CD Delft, The Netherlands; orcid.org/0000-0003-3059-8712

Complete contact information is available at:
<https://pubs.acs.org/10.1021/acs.jpcc.2c06381>

Notes

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