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Improved Anomaly Detection and Localization Using Whitening-Enhanced Autoencoders

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Abstract-Anomaly detection is of considerable significance in engineering applications, such as the monitoring and control of large-scale energy systems. This article investigates the ability to accurately detect and localize the source of anomalies, using an autoencoder neural networkbased detector. Correlations between residuals are identified as a source of misclassifications, and whitening transformations that decorrelate input features and/or residuals are analyzed as a potential solution. For two use cases, regarding spatially distributed wind power generation and temporal profiles of electricity consumption, the performance of various data processing combinations was quantified. Whitening of the input data was found to be most beneficial for accurate detection, with a slight benefit for the combined whitening of inputs and residuals. For localization of anomalies, whitening of residuals was preferred, and the best performance was obtained using standardization of the input data and whitening of the residuals using the zero-phase component analysis (ZCA) or zero-phase component analysis-correlation (ZCA-cor) whitening matrix with a small additional offset.

Index Terms—Anomaly detection, autoencoder, renewable generation, whitening transformation.

I. INTRODUCTION

M ONITORING and control of large-scale engineering systems require accurate measurements and dependable communication infrastructure—and methods to process that data for operational awareness. An important example is the case of electrical power systems that are increasingly reliant on variable renewable generation [1]. In this context, it is important to detect anomalies in high dimensional, highly variable observations from a multitude of sensors. For example, mild reductions in power generation caused by a wind turbine component malfunction or physical disturbance. Insufficient performance

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of anomaly detectors may threaten both the economic dispatch and secure control of power systems [2].

In recent years, with the development of deep neural networkrelated technologies, an unsupervised data-driven approach for anomaly detection has been proposed in the form of an autoencoder-based classifier [3]. It considers anomaly detection as a one-class classification task by learning patterns of normal operating states. This is well-suited to the inherent data imbalance in anomaly detection applications and the fastevolving power grid [4]. On this basis, techniques have been designed to detect anomalies in renewable energy systems using autoencoder-based detectors. For example, in [5], [6], and [7], the authors have proposed an autoencoder neural network to analyze anomalies of wind turbine components using power generation or other supervisory control and data acquisition (SCADA) data. However, the basic autoencoder-based anomaly detector is based on thresholding of residuals (reconstruction errors) using a Euclidean distance metric. This does not account for significant dependencies between measurements, such as the spatial and temporal correlations of renewable resources [8]. The mismatch between the detector design and features of the data could have a negative impact on detection sensitivity and localization performance.

In view of this, some authors have proposed using the Mahalanobis distance to measure the *residuals* and, thus, acquire more accurate classification boundaries for autoencoder-based anomaly detectors [9]. Authors of [10], [11], and [12] reported autoencoder-based wind turbine fault detectors using the Mahalanobis distance. However, it has not yet been investigated how the modified detection boundaries impact the anomaly localization performance.

Apart from adjusting residuals, the correlated renewable generation data, which are the *input* of autoencoder network, can be decorrelated and standardized (i.e., whitened [13]) before fed into the autoencoder. This technique has been considered in the field of computer vision, with a focus on image and video datasets, for example, the image retrieval [14] and object recognition [15]. However, there has been little quantitative analysis of detection sensitivity and localization performance improvement in the context of utilizing an autoencoder-based detector with input data whitening [16]. Furthermore, what is not yet clear is the impact of processing the inputs and residuals *together* on the capacity of a detector.

This article bridges these identified gaps by investigating the impact of whitening input data and residuals and quantifying

1551-3203 © 2023 IEEE. Personal use is permitted, but republication/redistribution requires IEEE permission. See https://www.ieee.org/publications/rights/index.html for more information. the improvement of detection sensitivity and localization performance using our proposed metrics. This is done in the context of two high-dimensional energy system use cases. The main contributions of this article are listed as follows.

- Comparative studies of different data processing methods, neural network configuration schemes, and whitening matrix selections are carried out, and their influences on anomaly detection sensitivity and localization accuracy are quantified using a variety of metrics.
- 2) We propose a combined whitening of the input features and of autoencoder residuals, which is shown to maximize detection sensitivity in two high-dimensional use cases: one for spatially correlated renewable wind power generation and one for electricity consumption time series.
- 3) A combination of input feature standardization and zero-phase component analysis-correlation (ZCA-cor)or zero-phase component analysis (ZCA)-based residual whitening is shown to enhance the visibility of anomalies and, thus, achieve an outstanding localization performance of an anomaly detector. The performance is further enhanced by a tunable offset to the whitening transformation.

II. ANOMALY DETECTION MECHANISM

Anomaly detection is essentially a classification problem with the objective of distinguishing anomalous data from data that is considered "normal" [17]. The most common approach is to treat anomaly detection as a supervised learning task, e.g., using support vector machines (SVMs) [18] or deep neural network classifiers [19]. However, supervised learning requires a training dataset with representative normal system operations and anomalies. Such datasets are in short supply because of the rarity of anomalies, unwillingness to share data, and evolving anomalies. Thus, it is difficult to learn a satisfactory discriminator of "normal" and "anomalous" scenarios on this basis [20].

Alternatively, anomaly detection can be approached as a one-class classification problem (e.g., using a one-class SVM approach [21]), where the detector is trained on examples of only "normal" operation data using an autoencoder-based neural network. Observations with features that deviate substantially from those in the training data will be considered anomalies. There are two main advantages to this approach. First, the autoencoder-based mechanism avoids the need to gather or generate anomalous data to create balanced datasets for training the classifiers. Second, by focusing on what is normal only, the proposed mechanism is naturally prepared for unknown anomaly patterns.

A. Autoencoder Training

Autoencoders learn the most important features of the training data (i.e., normal power system measurements) by sending the measurements through an information bottleneck while attempting to reconstruct the training data with minimal error [3]. The structure of the autoencoder algorithm is depicted in Fig. 1. The dimension reduction process of mapping the *n*-dimensional input data to the code in the bottleneck layer *B* through hidden layers H_1 to H_p is named the *encoder*. Afterwards, the *decoder*



Fig. 1. Schematic of the autoencoder.

decompresses the code to n-dimensional output data. Weight matrices K and bias vectors b are utilized in the encoding and decoding process as

$$x = g(K_p^e(\dots g(K_0^e z + b_0^e) \dots) + b_p^e),$$
(1a)

$$\hat{z} = g(K_p^d(\dots g(K_0^d x + b_0^d) \dots) + b_p^d),$$
 (1b)

where K_p^e and K_p^d denote weight matrices for encoding and decoding process, respectively, b_p^e and b_p^d are bias vectors, and $g(\cdot)$ represents a nonlinear element-wise activation function. $z \in \mathbb{R}^n$ refers to the input data vector, x is the data in the bottleneck layer B, and vector $\hat{z} \in \mathbb{R}^n$ stands for the output.

The residual vector associated with a training observation z_i is given by $r_i = z_i - \hat{z}_i$. The corresponding reconstruction error R_i is commonly expressed as the 2-norm of r_i , and the objective of the training process is to minimize the mean value of all reconstruction errors \mathcal{R}_i as

$$\min_{K,b} \left\{ J := \frac{1}{k} \sum_{i=1}^{k} \|r_i\|_2 \right\},$$
(2)

where k denotes the total number of the observations used for the autoencoder training process.

B. Anomaly Classification

In this work, an anomaly is defined as an observation that does not match the patterns inferred from data that are considered normal. Specifically, the observation is in a region of observation space that is estimated to contain less than a predefined fraction of data—thereby limiting the false positive (FP) rate of the assignment of observations to anomalies.

After the convergence of the objective J, the trained autoencoder is utilized to encode and decode the validation data, resulting in reconstruction errors \mathcal{R}_v , which are used to determine an anomaly threshold τ_v^{α} equal to the α th percentile of \mathcal{R}_v ; for example, at the value where an "inflection point" occurs in the error distribution [17]. Finally, the reconstruction errors \mathcal{R}_e of the test data are compared with τ_v^{α} to classify states into normal $(R_e \leq \tau_v^{\alpha})$ and anomalous $(R_e > \tau_v^{\alpha})$ data.

Geometrically, R_i denotes the Euclidean distance between the input z_i and reconstructed data \hat{z}_i . The τ_v^{α} stands for the maximum distance that a data point can be considered normal. Notably, the spatial set that is not further than τ_v^{α} is defined as



Fig. 2. Illustrative two-dimensional distributions of: (a) original residuals, (b) whitened original residuals, (c) synthetic anomalous residuals obtained by shifting, and (d) anomalous residuals whitened according to the normal data. The residuals are classified as TN, FP, TP, and FN by comparing with a 95% threshold ($\alpha = 95$) calculated on a validation set.

an "estimated normal data zone." It is an *n*-ball in the space of residuals, with radius τ_v^{α} and centered on the origin.

C. Problem Formulation

Power system measurements exhibit spatial-temporal dependencies. For example, due to geographic factors, the scale, and irradiance of renewable resources, such as wind and solar are spatially dependent within a given region [8]. Autoencoderbased neural networks are trained to replicate these correlated inputs on the output side with minimal reconstruction errors.

Dependencies in inputs may also lead to correlated residuals. An example in Fig. 2 shows two dimensions of the residuals obtained in the case study of Section IV. The residuals of normal test data shown in Fig. 2(a) are classified into true negatives (TNs) and FPs by the threshold τ_v^{α} . However, the assumption of a circular "estimated normal data zone" is not appropriate for this ellipsoidal distribution. Fig. 2(c) illustrates this with simulated anomalous data that is obtained by shifting the residuals. Many clearly anomalous points are within the normal circle and therefore not detected [false negatives (FNs)]. This reduces the probability that an actual anomaly is identified: the true positive (TP) rate (TPR), also known as detection sensitivity. The illustration in two dimensions also applies to residuals in higher dimensions.

III. DETECTOR ENHANCEMENTS

A. Data Whitening for Performance Improvement

In view of the elliptically distributed residuals and concomitant errors in anomaly detection, whitening (also known as sphering) the observations is a promising approach to improve the detection performance. By removing the correlations between the residual components, the *n*-ball may better describe the normal data distribution, and anomalies may be detected more accurately. The potential effectiveness of this approach is depicted in Fig. 2(b) and (d). Whitening can be applied in three different combinations of two approaches as follows:

- 1) whitening of the input data;
- 2) whitening of generated residuals;
- 3) combined whitening of the input data and residuals.

1) Whitening Transformations: We first summarize properties of the whitening transformation. Consider a random vector $Z = (z_1, ..., z_n)^T$, with the (nonsingular) covariance matrix $\text{Cov}(Z, Z) = \Sigma \in \mathbb{R}^{n \times n}$. We define the (also nonsingular) whitening transformation matrix $W \in \mathbb{R}^{n \times n}$ such that

$$V = (V_1, \dots, V_n)^T = WZ,$$
(3)

where the elements of the random vector v are uncorrelated and have unit variance: Cov(V, V) = 1. We determine constraints on W by expanding

$$\operatorname{Cov}(V, V) = \operatorname{E} \left[WZ(WZ)^T \right] - \operatorname{E}[WZ]\operatorname{E} \left[(WZ)^T \right]$$
$$= W \left(\operatorname{E}[ZZ^T] - \operatorname{E}[Z]\operatorname{E}[Z^T] \right) W^T = W\Sigma W^T.$$
(4)

This implies the constraint $W\Sigma W^T = 1$. As W is invertible, we multiply the W^{-1} and $(W^T)^{-1}$ from the left and right, respectively, and find after inversion

$$W^T W = \Sigma^{-1}.$$
 (5)

This does not determine the whitening matrix W uniquely. Among the infinite possible options of whitening matrices W, a few are commonly used [22]. In this article, four approaches are studied: principle component analysis (PCA), ZCA, Cholesky, and ZCA-cor [13].

The PCA whitening transformation is a widely used sphering approach due to its close relation to PCA [23]. It can be regarded as rescaling variances of all dimensions to one after a PCA procedure that omits the customary dimension reduction. The whitening matrix is

$$W_{\rm PCA} = \Lambda^{-1/2} U^T, \tag{6}$$

where $\Lambda \in \mathbb{R}^{n \times n}$ is a diagonal matrix with the eigenvalues of covariance matrix Σ and the columns of $U \in \mathbb{R}^{n \times n}$ are the corresponding eigenvectors. It is closely related to the ZCA approach, which uses U to transfer the PCA whitened data back to the original coordinate system [13]

$$W_{\rm ZCA} = U\Lambda^{-1/2}U^T.$$
 (7)

ZCA whitening has been used in various applications, such as a data preprocessing step for stochastic gradient decent [24] and image classification with convolutional neural networks [25]. The Cholesky whitening transformation is defined as

$$W_{\rm Chol} = L^T, \tag{8}$$

where $L \in \mathbb{R}^{n \times n}$ is a lower triangular matrix with positive diagonal entries, obtained by Cholesky decomposition of the

precision matrix (inverse covariance matrix): $\Sigma^{-1} = LL^T$. The final sphering approach considered in this article is ZCA-cor *whitening* transformation [13]. It uses the whitening matrix

$$W_{\text{ZCA-cor}} = S^{-1/2} V^{-1/2},$$
 (9)

where $V \in \mathbb{R}^{n \times n}$ is the diagonal variance matrix and $S \in \mathbb{R}^{n \times n}$ denotes the correlation matrix (so that $\Sigma = V^{1/2}SV^{1/2}$). The ZCA-cor whitening approach maximizes the correlation of whitened and original components [13]. Unlike W_{ZCA} , $W_{\text{ZCA-cor}}$ is in general asymmetric.

In this article, we consider both detection and localization performance of the anomaly detector. As the whitening procedure is transparent to the calculation of residual vectors (the squared vector is used), the particular choice of W mostly affects the localization performance. It may also affect the detection performance, albeit indirectly, if whitening is applied to the input data, thus affecting the training of the autoencoder.

2) Input Whitening: The whitening transformation can be utilized to remove correlations from the data used for training and testing. First, this enables the autoencoder network to learn from less redundant inputs, which is generally desirable [15]. But more importantly, we hypothesize that the reduction in the input correlation may propagate to the residuals.

We consider a whitened input data point

$$z_w = W_z(z - \mu_z) \tag{10}$$

with W_z , the z-space whitening matrix, computed from the sample covariance of the training data z. The data is also (optionally) centered on the data mean μ_z . The residual $r_w \in \mathbb{R}^n$ is defined as $r_w = z_w - \hat{z}_w$, where \hat{z}_w is the reconstructed data point. Inverting the whitening procedure gives $\hat{z}_a = W_z^{-1}\hat{z}_w + \mu_z$, which may be compared with the original z. The reconstruction error of the whitened data $||r_w||_2$ can be related to that of $r_a = z - \hat{z}_a$ as

$$|r_w||_2 = ||z_w - \hat{z}_w||_2 = [(z - \hat{z}_a)^T W_z^T W_z (z - \hat{z}_a)]^{1/2}$$

= $[(z - \hat{z}_a)^T \Sigma_z^{-1} (z - \hat{z}_a)]^{1/2} \triangleq ||r_a||_{\Sigma_z^{-1}}.$ (11)

Compared with (2), by taking correlations of original inputs into account, we are effectively measuring the Mahalanobis distance [26] between z and \hat{z}_a instead of their standard Euclidean length. Whitening of the input data, thus, affects both the representation of the training data as well as the loss function used during training.

3) Residual Whitening: In contrast with applying whitening transformation before feeding data into the neural network, residual whitening reshapes the distribution of residuals for a given trained autoencoder. Concretely, the raw residual $r = [r_1, \ldots, r_n]^T$ is whitened as

$$r_s = W_r(r - \mu_r). \tag{12}$$

Here, the whitening matrix $W_r \in \mathbb{R}^{n \times n}$ is computed on the sample covariance of residuals from the *validation* data, because the training dataset is used to train the autoencoder itself. μ_r represents the mean of raw residuals in the validation set, which should be approximately zero if the RMSE loss function was used during training. Accordingly, the reconstruction error is

given by

$$||r_s||_2 = [(r - \mu_r)^T \Sigma_r^{-1} (r - \mu_r)]^{1/2} \triangleq ||r - \mu_r||_{\Sigma_r^{-1}}.$$
 (13)

Slightly different from (11), the reconstruction error in (13) denotes the Mahalanobis distance of a residual r from a set of residuals with mean μ_r and covariance matrix Σ_r .

B. Anomaly Localization Metrics

In many scenarios, when a likely anomaly has been detected, it is important to also identify, which observation(s) triggered the anomaly detector. They may indicate a component malfunction or source of the physical disturbance. In the case study that follows, we will show that with a well-chosen whitening procedure, the values of the residual vector can be used to pinpoint the anomaly: the highest absolute residuals are the most likely locations of anomalies.

To quantify the dependability of the localization performance, we propose three metrics. The first of these is the root mean square (RMS) ratio, which denotes the ratio of root mean square value of anomalous dimensions to that of normal dimensions in residual vectors. This is given by

RMS Ratio

$$= \frac{1}{m} \sum_{l=1}^{m} \left\{ \left[\frac{1}{|\mathcal{A}|} \sum_{j \in \mathcal{A}} (r_{j}^{(l)})^{2} \right]^{\frac{1}{2}} / \left[\frac{1}{|\mathcal{N}|} \sum_{j \in \mathcal{N}} (r_{j}^{(l)})^{2} \right]^{\frac{1}{2}} \right\},$$
(14)

where $r_j^{(l)}$ denotes the *j*th element of the residual of the *l*th test data point. \mathcal{A} is the set of anomalous dimensions (e.g., malfunctioning devices), and \mathcal{N} represents the set of nonanomalous dimensions. Moreover, *m* refers to the total number of records in the test set. The RMS ratio can be used to estimate if the anomalous stand out on average. A second, more stringent metric is introduced as well: gap ratio, which measures the average ratio of the smallest anomalous dimension to the largest normal dimension (absolute value). It is defined as

Gap Ratio =
$$\frac{1}{m} \sum_{l=1}^{m} \left\{ \min_{j \in \mathcal{A}} |r_j^{(l)}| / \max_{j \in \mathcal{N}} |r_j^{(l)}| \right\}.$$
 (15)

The third metric, ordinal consistency rate (OCR), calculates the proportion of samples for which the smallest absolute value of an *anomalous* dimension exceeds the largest absolute value of a *nonanomalous* dimension

$$\text{OCR} = \frac{1}{m} \sum_{l=1}^{m} \mathbb{1}_{\min_{j \in \mathcal{A}} |r_j^{(l)}| > \max_{j \in \mathcal{N}} |r_j^{(l)}|}.$$
 (16)

C. Design of the Anomaly Detector

We integrate the anomaly detection mechanism and whitening schemes to give data processing options as well as explain, which data is used in different stages. The proposed data flow and its transformation processes in the autoencoder neural networkbased anomaly detector are depicted in Fig. 3 with the following five steps.



Fig. 3. Proposed framework of data flow in the autoencoder neural network-based anomaly detector.

1) Data Partition: Given the historical dataset X, the first step is to divide observations into training, validation, and test dataset as X_t , X_v , and X_e with a specific ratio.

2) Input Preprocessing: In this step, statistics of the training data (mean, range, covariance) are computed, and these values are used for input processing of training, validation, and test data according to the selected method, e.g., input whitening shown in (10).

3) Training and Reconstruction: The weight matrices K and bias vectors b are updated iteratively to minimize the reconstruction loss in (2). Afterwards, the trained autoencoder neural network is utilized to reconstruct the validation and test set to \hat{X}'_v and \hat{X}'_e . Then, the corresponding residual sets r'_v and r'_e are calculated, such as r_w in (11).

4) Residual Postprocessing: If residual whitening is employed, the validation residuals are used to compute the whitening transformation. After executing residual whitening transformation shown in (12), the reconstruction errors of the validation set \tilde{R}_v and test set \tilde{R}_e are calculated as (13).

5) Detection Performance Evaluation: The anomaly threshold $\tilde{\tau}_v^{\alpha}$ is obtained as a quantile of the reconstruction errors \tilde{R}_v , corresponding to the desired TN rate $\alpha\%$. The test data are classified by comparing reconstructions \tilde{R}_e with the threshold $\tilde{\tau}_v^{\alpha}$. Consequently, the performance of the anomaly detector is assessed by calculating the evaluation metrics based on the predicted normal, anomalous states, and the actual states.

IV. CASE STUDY: SNAPSHOT DATA

In this section, the impacts of different data processing options, neural network configurations, and whitening matrix selections on anomaly detection and localization capacity of an autoencoder-based detector were investigated. To do so, we conducted a case study on the power generation from distributed wind farms. Although introduced anomalies are synthetic, the wind farm output is based on reanalysis data of historical wind speeds. This use of maximally realistic high-dimensional data ensures that the data won't be easily compressed into a low-dimensional manifold by an autoencoder.

To do so, we first described the process of modeling normal data patterns and then formulated anomalous scenarios. For these scenarios, we made anomaly detection performance comparisons by implementing various combinations of data transformations including whitening. Next, anomaly locating capacity evaluation was conducted by comparing four whitening transformations: PCA, Cholesky, ZCA, and ZCA-cor.

A. Experiment Scenario Formulation

Renewable power generation from spatially distributed wind farms is an increasingly relevant source of energy. The power output of each wind farm is highly variable due to variations in wind speed, but this may obscure other factors causing reduced performance. Given this, experiments were conducted to test if our proposed mechanism can detect and localize anomalies in the power output of wind farms with satisfactory capacity. Notably, without knowing any model-related information about wind farms and relying on the neural network-based data-driven methodology only, our proposed anomaly detection mechanism was trained on historical operation data and tested on both normal and anomalous scenarios. In this article, we generated anomalous scenarios as reductions in power output of one or more wind farms. These could reflect unexpected malfunctions, disturbances, unscheduled outages, or unreported maintenance activities (from the perspective of system operators).

A realistic wind power dataset was constructed as follows. We virtually placed a 100 MW wind farm at each center of the 99 municipalities located in the North and South Holland provinces of the Netherlands. The wind power output was simulated on the basis of historical wind speeds at the 99 locations, obtained by MERRA-2 reanalysis and available from renewables.ninja [27]. After obtaining the historical wind data [28], the associated generated power outputs were calculated as described in [29]. For the purpose of this study, observations were snapshots of instantaneous power production. Ultimately, the whole generated dataset $X \in \mathbb{R}^{87648 \times 99}$, which includes 10 years' (2009–2018) hourly outputs of 99 wind farms, was divided into the training set X_t , validation set X_v , and test set X_e with the proportion of 6, 2, and 2 years.

The autoencoder encoded and decoded the 99-dimensional data from the input to output layer. Both encoder and decoder were fully connected networks with 3 hidden layers with 200 neurons each, connected to a bottleneck layer with variable size. The bottleneck size is indicated as B_n , where *n* is the number of neurons in the bottleneck layer. The rectified linear activation function (ReLU) activation function was used, and the Adam Optimizer [30] was utilized to iteratively optimize the value of weight matrices *K* and bias vectors *b*. In this research, 5×10^3

TABLE I DATA PROCESSING METHOD COMBINATIONS

	Input pre-processing	Residual post-processing
P _{NN}	None	None
$P_{\rm SN}$	Standardization	None
$P_{\rm WN}$	Whitening	None
P _{NW}	None	Whitening
$P_{\rm SW}$	Standardization	Whitening
Pww	Whitening	Whitening



Fig. 4. Correlation coefficient matrices of normal testing residuals \tilde{r}_e when utilizing four data processing combinations. The dimensions shown correspond to nine virtual wind farms (B_{64} is utilized).

training epochs were used, and the learning rate for training was 5×10^{-5} . Training and testing of the autoencoder were conducted using tensorflow.

For a comparative study of anomaly detection and localization performance, we made use of different combinations of input preprocessing methods and residual postprocessing. The combinations, denoted as P_{xy} , are listed in Table I.

B. Impact of Whitening Transformation

Fig. 4 depicts the correlation coefficients of the testing residuals \tilde{r}_e for 9 out of the 99 dimensions, for a variety of data processing methods. When the input data is standardized, but no whitening is performed ($P_{\rm SN}$), high correlations among different dimensions are visible, which implies "elliptically" distributed residuals according to the analysis in Section II-C.

As expected, whitening effectively reduces these correlations. Whitening of the input data (P_{WN}) drastically reduces correlations between the residuals. Correlations are slightly lower still when whitening is applied directly to the residuals (P_{SW}). Note

that the pairwise correlations are not zero due to differences between the validation set (used to determine the postwhitening matrix) and the test set. Finally, applying whitening on the inputs and the outputs (P_{WW}) produces similarly small correlations.

C. Anomaly Detection Performance Evaluation

Both the processing methods (P_{xy}) and the autoencoder configuration (B_x) influence the sensitivity of anomaly detection. This impact will be quantified in this section. For these tests, anomalies were generated by modifying the test data as follows. For each data point, we randomly selected one wind farm out of 99 and reduced its power output by a given amount (the *anomaly magnitude*, abbrev. *am*). This approach yields an anomalous test set consisting of 17,544 nonanomalous data points and an equal number of anomalous data points.

1) Receiver Operating Characteristic (ROC) Curves: ROCs and the corresponding area under the curve (AUC) were used to quantify the sensitivity and specificity of anomaly detection, as a function of the autoencoder structure, data processing method, and anomaly magnitude. ROC curves were constructed by varying the threshold τ_v^{α} . For all cases, ZCA was selected as the whitening matrix, and an anomaly magnitude of 10% was used.

For the first experiment, we used default processing $P_{\rm SN}$: standardizing the input data and detecting anomalies from unprocessed residuals. Comparing the performance of all layer dimension configurations B_x , we can observe in Fig. 5(a) that autoencoder networks configured as B_{32} , B_{64} , and B_{96} have better detection performance. Specifically, at each FP rate, the TPR (sensitivity) of these detectors are higher than others'. Accordingly, they also have larger AUC. This indicates that optimal detection is achieved with fairly wide autoencoders. The configuration B_{64} was used for all following experiments.

A comparison of the anomaly detection performance of all data processing approaches P_{xy} is shown in Fig. 5(b). The following can be observed:

- 1) detectors equipped with whitening transformation (P_{WN} , P_{NW} , P_{SW} , and P_{WW}) have higher anomaly detection sensitivity than the others;
- 2) performing whitening only on the inputs (P_{WN} and P_{WW}) renders higher detection sensitivity than whitening approaches performed to the residuals (P_{NW} and P_{SW});
- 3) the detector using combined whitening (P_{WW}) slightly outperforms the detector just utilizing input whitening (P_{WN}) .

It can be concluded that the combined whitening approach P_{WW} is the best choice to improve overall anomaly detection sensitivity.

Moreover, we investigated the ability to detect anomalies of various magnitudes, using the selected processing strategy P_{WW} . Fig. 5(c) shows that, as the anomaly rate increases from 1% to 30%, the ROC curves and AUC improve, reaching very high levels from 10%.

2) Detection Performance Evaluation by Multiple Metrics: In addition to the detection sensitivity (TPR), we evaluated



Fig. 5. Test set receiver operating characteristics of spatial data, using different configurations (B_x) , data processing methods (P_{xy}) , and anomaly magnitudes.

TABLE IIDETECTION PERFORMANCE COMPARISON BY MULTIPLE METRICS ($\alpha = 99$,
ANOMALY MAGNITUDE = 10%, AND B_{64} IS UTILIZED)

Processing method	TNR	TPR	PPV	F_1 -score
P _{NN}	98.89%	56.26%	98.07%	71.50%
P _{SN}	98.77%	40.58%	97.06%	57.23%
$P_{\rm WN}$	98.98%	84.06%	98.80%	90.83%
P _{NW}	98.86%	71.81%	98.44%	83.04%
P _{SW}	98.80%	66.52%	98.22%	79.32%
$P_{\rm WW}$	98.88%	85.14%	98.70%	91.42%

the performance of the anomaly detector by multiple metrics, namely true positive rate (TNR), positive predictive value (PPV), and F_1 -score. Interested readers can refer to [31] for a detailed introduction to the metrics. For all cases, we used an anomaly magnitude of 10%, $\alpha = 99$, and layer configuration B_{64} . The experimental results are shown in Table II. The bold values indicate the best results for each column. In all cases, the TNR is close to 99%, consistent with the choice of the threshold $\alpha = 99$. Similarly, the PPV scores are high across all processing methods, but a closer look at the TPR and F_1 metrics shows that—perhaps surprisingly—the P_{SN} processing scheme is least dependable, by a large margin. The schemes using whitening of input data outperform all others, with a slight edge for the combined whitening procedure (P_{WW}) over the prewhitening only procedure (P_{WN}).

To investigate the stability of the stochastic training process, model training was performed 15 times, and the variability of the sensitivity was monitored (results not shown). Whitening at the preprocessing stage resulted in higher sensitivity *and* a narrower range of results.

3) Detection Performance of Different Anomaly Types: In the next experiment, the performance of detecting different anomaly types was investigated. The total anomaly magnitude (i.e., power reduction) was fixed at 10% and 30%, respectively, but distributed over 1, 2, 5, or 10 observations. The experimental results are shown in Table III. Under each total anomaly magnitude, more concentrated anomalies (i.e., $1 \times 10\%$ and $1 \times 30\%$)

TABLE IIIDETECTION PERFORMANCE COMPARISON BY DIFFERENT ANOMALY TYPES $(\alpha = 99, P_{WW}, \text{ And } B_{64} \text{ Are Utilized})$

Anomaly types	TNR	TPR	PPV	F_1 -score
$1 \times 10\%$	98.88%	85.14%	98.70%	91.42%
$2 \times 5\%$	98.88%	80.20%	98.62%	88.46%
$5 \times 2\%$	98.88%	67.84%	98.38%	80.30%
$10 \times 1\%$	98.88%	53.72%	97.96%	69.39%
$1 \times 30\%$	98.88%	95.35%	98.84%	97.06%
$2 \times 15\%$	98.88%	95.06%	98.84%	96.91%
$5 \times 6\%$	98.88%	91.95%	98.80%	95.25%
$10 \times 3\%$	98.88%	87.92%	97.74%	93.02%

render higher TPR and F_1 -scores, but these decrease for more diffuse anomalies, as might be expected. TNR and PPV remain high for all anomaly patterns.

D. Anomaly Localization Performance Evaluation

In addition to quantifying the ability to detect anomalies (a binary classification), we next investigated the ability to localize the source of an anomaly, and how this depends on the configuration of the detector.

1) Visual Comparison of Localization Performance: We first considered an illustrative example of anomaly localization, in which the output of three wind farms (numbers 41, 52, and 76) was reduced by 5%. The input data is shown in Fig. 6 (top panel), where the anomalous locations are indicated in yellow. Looking at the residuals of standardized data (P_{SN} , middle panel), it can be seen that the residuals of the three anomalous dimensions stand out. In the bottom panel, we can observe that the four whitening approaches affect the residual signals in different ways. PCA whitening mixes all coordinates and fully obscures the connection between the original perturbations and residuals. As a result, it will not be considered in the follow-up analysis. In contrast, the Cholesky, ZCA, and ZCA-cor whitened residuals all have peaks that are consistent with the actual anomalous dimensions, but the Cholesky method also produces residuals in nonanomalous locations (e.g., a peak at dimension number 40). This result



Fig. 6. Illustrative example that depicts the effect of different whitening approaches on anomaly locating capacity (anomaly magnitude = 5%; P_{SN} , P_{SW} , and B_{64} are utilized).



Fig. 7. RMS ratios of the anomalous to normal dimensions for data processing/whitening combinations (B_{64} is utilized).

is consistent with the fact that ZCA whitening maximizes the average cross-covariance between the original and whitened data and ZCA-cor maximizes their cross-correlation [13].

2) Statistical Localization Performance Comparison: For each point in the test set, we randomly selected 3 out of 99 wind farms and applied power reductions to generate anomalous test vectors, resulting in test sets of 17,544 data points for each anomaly rate. Fig. 7 depicts the RMS ratio for various data processing schemes, as a function of anomaly magnitude, and Table IV shows numerical results for all three anomaly metrics for a fixed anomaly magnitude of 5%.

The most striking observation is that methods that perform whitening at the preprocessing stage (P_{Wx}) scored significantly worse on all localization metrics. Apparently, mixing of features before encoding helps to improve detection sensitivity (previous section), but is detrimental to localization performance. Moreover, for any data processing combination, both ZCA processing schemes scored higher than the *Cholesky* whitening scheme, and the best scores were obtained when the ZCA and ZCA-cor schemes are used for postprocessing, in combination with standardization for preprocessing (P_{SW}). Here, ZCA scored very slightly higher on the RMS ratio and *gap ratio* metrics (typical

TABLE IVLocalization Capacities of Using Different Data Processing
Methods (Anomaly Magnitude = 5% and B_{64} Is Utilized)

Processing method	Whitening matrix	RMS ratio	Gap ratio	OCR
P _{NN}	/	7.32	1.60	73.18%
$P_{\rm SN}$	/	8.05	1.97	78.48%
$P_{\rm WN}$	Cholesky	2.98	0.37	7.17%
$P_{\rm WN}$	ZCA	3.98	0.68	23.40%
$P_{\rm WN}$	ZCA-cor	3.82	0.61	18.22%
$P_{\rm NW}$	Cholesky	6.55	1.39	68.04%
P _{NW}	ZCA	7.81	1.65	75.98%
$P_{\rm NW}$	ZCA-cor	7.81	1.65	75.74%
P _{SW}	Cholesky	8.58	1.59	71.78%
P _{SW}	ZCA	9.68	1.98	82.23%
P _{SW}	ZCA-cor	9.62	1.97	82.60%
$P_{\rm WW}$	Cholesky	2.65	0.30	2.44%
$P_{\rm WW}$	ZCA	3.90	0.65	20.52%
$P_{\rm WW}$	ZCA-cor	3.82	0.61	18.27%
P _{SW}	ZCA-c	9.72	2.07	84.65%
Psw	ZCA-cor-c	9.67	2.06	85.08%



Fig. 8. Localization performance as a function of whitening offset c.

separation), and ZCA-cor attained the highest scores on the OCR metric (ordering).

Finally, an additional enhancement of the method was introduced. The residual whitening transformation (12) mixes signals between dimensions. This may cause a peak (positive or negative) in one or more dimensions to affect the average value of other dimensions. In order to better separate this signal from the background, we applied a constant offset to the whitening matrix (12) as follows:

$$r_{s(c)} = (W_r - c\mathbb{1})r.$$
 (17)

Here, 1 is a matrix of ones and c is a constant to be defined, so that a multiple of the sum-of-residual values $(\sum_i r_i)$ is subtracted from the whitened feature vector. The change of localization performance as a function of c is shown in Fig. 8. An overall improvement is obtained for values larger than zero, although RMS ratio decreases after an initial increase. Results for the value c = 5 are included in Table IV.

V. CASE STUDY: TIME-SERIES DATA

A. Experiment Scenario Formulation

Apart from detecting anomalies in data "snapshots" that correspond to spatially distributed locations, we further validate



Fig. 9. Test set receiver operating characteristics of time series data using different data processing methods (P_{xy}) and anomaly magnitudes.

the anomaly detection performance of the whitening-enhanced autoencoder using a time-series dataset. This dataset contains half-hourly load profiles of 4,173 customers in London collected between 2011 and 2014 [32]. A total of 4,000 customers were randomly selected, and data from 2013 (the most complete year) were used to create daily load profiles for groups of 100 customers. The resulting dataset $X \in \mathbb{R}^{14,600 \times 48}$ was randomly divided into training, validation, and testing sets in blocks of one week with the proportion of 2:1:1. The dimensions of hidden and bottleneck layers were set as 96 and 32, respectively. The batch size was 16, the learning rate was 1×10^{-5} , and 350 training epochs were used. Other settings were kept the same as those in Section IV-A. Anomalous load profiles were created by modifying the test set. Specifically, 3 randomly selected data points out of each 48-dimensional load profile were reduced by a certain amount.

B. Anomaly Detection Performance

Fig. 9(a) compares the results obtained with different whitening methods, for a given anomaly magnitude of 30% [comparable with Fig. 5(b)]. It is evident that also in this case, whitening-enhanced autoencoders (P_{NW} , P_{WN} , P_{SW} , and P_{WW}) outperform nonwhitening-enhanced ones (P_{NN} and P_{SN}). A detector equipped with combined whitening (P_{WW}) has higher anomaly detection sensitivity than detectors equipped with signal whitening transformation (P_{NW} , P_{SW} , P_{WN}).

In addition, the detection performance of the P_{WW} method was investigated for different anomaly magnitudes. As expected, and shown in Fig. 9(b), the ROC curves and AUC improve as the anomaly magnitudes increase. When comparing the results with Fig. 5(c) for similar signal reductions, it is notable that detection performance is reduced, despite reductions occurring at three observed data points simultaneously instead of one. This is due to the larger stochasticity of electricity demand profiles compared to the highly correlated wind power snapshots, making it harder to distinguish normal and anomalous data, particularly at low anomaly magnitudes.

VI. CONCLUSION

Autoencoder neural networks are a powerful tool for the detection of unknown anomalies. A threshold for the (Euclidean)

length of the residuals is used to identify anomalous states of a system. In this article, we investigated how whitening-based decorrelation of the input features and residuals can improve the performance of the anomaly detector, for use cases of wind power generation at 99 different locations and daily electricity load profiles. Whitening of the *input* data was found to be most beneficial for detection performance, across multiple metrics, and a small further enhancement was obtained when both input data and the residuals were whitened (combined whitening). However, input whitening was found to reduce the ability to locate the source of anomalies. Three metrics were formulated to quantify this ability, and the best performance was obtained using standardization of the input data and whitening of the residuals using the ZCA or ZCA-cor whitening matrix with a small offset. In future work, we aim to extend the method to analyze spatial-temporal signatures and include contextual information. Further refinement of the neural network itself is also a promising research direction: applying batch normalization or modifying the objective function used during training may indirectly improve detection performance by smoothing the distribution of values of the nonanomalous data within the latent space or hidden network layers.

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