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# Application of thermodynamics at different scales to describe the behaviour of fast reacting binary mixtures in vapour-liquid equilibrium

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## ABSTRACT

The use of reactive working fluids in thermodynamic cycles is currently being considered as an alternative to inert working fluids, because of the preliminarily attested higher energy-efficiency potential. The current needs to simulate their use in thermodynamic cycles, which may operate in liquid, vapour or vapour-liquid state, are an accurate real-fluid equation of state and ideal gas thermochemical properties of each molecule constituting the mixture, to calculate the equilibrium constant. To this end, the appeal to a multi-scale theoretical methodology is paramount and its definition represents the objective of the present work. This methodology is applied and validated on the system  $N_2O_4 \rightleftharpoons 2NO_2$ . Firstly, the equations solved for simultaneous two-phase and reaction equilibrium are presented. Secondly, ideal gas thermochemical properties of  $N_2O_4$  and  $NO_2$  are computed at atomic scale by quantum mechanics simulations. Then, to apply the selected cubic equation of state, pure-component properties of the species forming the reactive mixture (critical point coordinates and acentric factor) are required as input. However, these properties are not measurable, since  $NO_2$  and  $N_2O_4$  do not exist in nature as pure components. To get around this difficulty, the methodology relies on molecular Monte Carlo simulations of the pure  $N_2O_4$  and  $NO_2$ , as well as on the reactive  $N_2O_4 \rightleftharpoons 2NO_2$ , enabling the determination of those missing pure-component properties and thus the calculation, on a macroscopic scale, of the reactive mixture properties. Finally, the comparison of calculated mixture properties with available experimental data leads to validate the accuracy of the proposed methodology.

## 1. Introduction

There exist few reversible chemical reactions which evolve *very rapidly* towards chemical equilibrium, whether subjected to a modification of their intensive properties, such as temperature and pressure. According to the specific use of such fluids, the high reaction rate can be approximated as being infinite and thus the chemical equilibrium state considered as being instantaneously attained.

One of those few systems is formed by the molecules  $N_2O_4$  and  $NO_2$ , whose proportion is dictated by the chemical equilibrium achieved by the reversible reaction  $N_2O_4 \rightleftharpoons 2NO_2$ , at the temperature and pressure of the system. At present, the  $NO_2/N_2O_4$  gas mixture is used as a powerful hypergolic oxidizer of fuels like hydrazine,  $N_2H_4$ , in space and

military rockets [1–3]. Between the years 1950 and 1990, the possible exploitation of the chemical properties of such a reactive fluid has also been explored in power plants, proposing it as a working fluid of thermodynamic cycles [2–13]. Indeed, the spontaneous, fast and reversible evolution of the chemical reaction when the fluid undergoes a modification of its temperature and pressure, while crossing the unit operations (turbine, heat exchangers, pumps, compressors, etc.), implies the involvement of chemical energy in the thermodynamic transformations, with significant effects on the performance of the thermodynamic cycle and on the sizing of units, such as the turbine [10]. Many studies have been conducted on the effect of using such a working fluid (commonly called “dissociating gas” in the literature) in power cycles, or on the characterisation of its thermochemical and thermophysical properties.

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The above-mentioned works have theoretically demonstrated that the thermodynamic efficiency of supercritical (Brayton) and subcritical (Rankine) cycles operating with reactive working fluids, mainly  $\text{N}_2\text{O}_4$ , is larger than the efficiency of cycles operating with specific inert fluids, such as water, ammonia, helium or  $\text{CO}_2$ . However, the comparison between, for example, the dissociating molecule  $\text{N}_2\text{O}_4$  and the inert molecule  $\text{H}_2\text{O}$  is not straightforward, as multiple molecular aspects should be considered, not only related to the chemical reaction but also to molecular heterogeneity ( $\text{N}_2\text{O}_4/\text{NO}_2$  vs.  $\text{H}_2\text{O}$ ). To enable a fairer comparison between reactive and inert fluids, other more generalised studies have considered fictitious chemical reactions ( $A_n \rightleftharpoons (n/m) A_m$ ) and investigated the effect of the reaction stoichiometry ( $n$ ,  $m$ ) and thermochemistry (enthalpy and entropy of reaction) on the performance of the Brayton power cycles and heat pumps, with respect to pure fluids (reactants or products) [14,15]. Two main conclusions were that the use of reactive working fluids may lead to the improvement of +30 % in the efficiency of power plants [14] and a more than doubled coefficient of performance of heat pumps based on a gaseous inversed Brayton cycle [15]. The reliability and advantages related to the use of  $\text{N}_2\text{O}_4$  have been experimentally validated at the Nuclear Power Institute of the Academy of Science, in Byelorussia, in mock-ups of 100 – 1000  $\text{kW}_{\text{th}}$  [16]. After 1986, with the Chernobyl disaster, Byelorussia stopped activities related to nuclear research and thus those studies on dissociating fluids were discontinued too. Not a single experimental or full-scale power plant operates with  $\text{N}_2\text{O}_4$ , nor with other similarly proposed dissociating gases, such as  $\text{Al}_2\text{Cl}_6 \rightleftharpoons 2 \text{AlCl}_3$  and  $\text{Al}_2\text{Br}_6 \rightleftharpoons 2 \text{AlBr}_3$ . A more complete review of past technological studies about reactive fluids and their applications is provided in Lasala et al. [14].

Theoretical studies on the use or characterization of reactive fluids potentially usable to enhance the performance of unit operations or thermodynamic cycles are nowadays again under development. Heat transfer properties of reactive  $\text{N}_2\text{O}_4$  are investigated by computational fluid dynamics in various heat exchangers [17,18]. One of the main conclusions is that the presence of the  $\text{N}_2\text{O}_4/\text{NO}_2$  chemical reaction in the heat exchange process enhances the heat transfer coefficient by 600 % with respect to non-reactive fluids. The problem underlying the limited spreading of using reactive working fluids in thermodynamic cycles is the scarce availability of similarly reversible fast chemical reactions, other than  $\text{N}_2\text{O}_4$ . Taking that into consideration, a research project named REACHER [19,20], funded by the European Research Council, aims to discover novel working fluids, characterise their thermodynamic and kinetic properties, to optimise the thermodynamic cycle architecture and, finally, to validate cycle's performance calculations on an experimental micro-power plant.

The high number of studies performed in the past has made many thermodynamic data available on the reactive  $\text{N}_2\text{O}_4/\text{NO}_2$ ,  $\text{Al}_2\text{Cl}_6/\text{AlCl}_3$  and  $\text{Al}_2\text{Br}_6/\text{AlBr}_3$ . Most of the measured data are collected in the Thermo Data Engine database (TDE 10.1) [21] and in the Dortmund Data Base (DDB2020) [22]. The thermodynamic modelling of  $\text{N}_2\text{O}_4$  is more investigated than  $\text{Al}_2\text{Cl}_6$  and  $\text{Al}_2\text{Br}_6$ . Calculations of thermodynamic properties of  $\text{N}_2\text{O}_4$  have been performed in different works, with the use of semi-empirical equations of state [23–31] or Monte Carlo simulations [32]. Stai et al. [23] used a modification of the Wohl equation to describe volumetric properties of gaseous  $\text{N}_2\text{O}_4$ , but the specifications for the critical coordinates are not explicitly provided. Seshadri [24] used virial equation of state parametrized over experimental data points and calculated the fugacity coefficients with the model developed by Hougen and Watson [25]. McCarty et al. [26] performed calculations using the Peng-Robinson equation of state, and optimised the coordinates of the critical point of the molecules forming the reactive mixture over available volumetric experimental data and assigned, as a preliminary assumption, the same acentric factor to  $\text{NO}_2$  and to  $\text{N}_2\text{O}_4$ . Also, McCarty [26] optimised the 32 parameters of a modified Benedict-Webb-Rubin equation of state to reproduce experimental P- $\rho$ -T data of the equilibrium mixture, treating it as a pseudo-pure component. With the aim to perform calculations on a power cycle, Binotti et al. [27] and

Manzolini et al. [28] also treated the system as a pseudo-pure component and modelled it with the Peng-Robinson equation of state. Vapor-liquid equilibrium of  $\text{N}_2\text{O}_4/\text{NO}_2$  was calculated by De Souza and Deiters [29], with both a hard sphere attractive model and a semiempirical equation of state optimized over experimental and Monte Carlo data. Then, Belkadi et al. [30] modelled VLE with soft-SAFT equation of state, without considering reactional equilibrium but treating the molecule  $\text{NO}_2$  as a self-associating component.

Moreover, Monte Carlo simulations have been performed on similar reactive mixtures being in phase and reaction equilibrium. Monte Carlo codes including Gibbs and reaction Monte Carlo were introduced by Johnson et al. [33], who treated the equilibrium of the reactive  $(\text{NO})_2/\text{NO}$ , and Smith and Triska [34]. The reactive system  $\text{N}_2\text{O}_4/\text{NO}_2$  system has been previously characterised by MC reaction and Gibbs ensembles by Bourasseau et al. [32], who also provided force field parameters optimized over experimental data.

Recently, Lemmon et al. [31] produced a thorough review work on the thermodynamic modelling and experimental characterisation of this system, and also developed a highly accurate multiparameter equation of state being specific to the reactive  $\text{N}_2\text{O}_4$ . This equation of state also accounts for the occurrence of the higher temperature reaction  $\text{NO}_2 \rightleftharpoons 2\text{NO} + \text{O}_2$ , other than  $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$ . In this model, authors used the pure-component critical temperature and density they determined for pure  $\text{N}_2\text{O}_4$  and pure  $\text{NO}_2$  by Monte Carlo Gibbs ensemble simulations, using the open source code Cassandra 1.2.5 [35] and force-field parameters from Bourasseau et al. [32]. Moreover, the parameters of the considered Helmholtz-based equation of state have been optimised on the basis of a high number of available experimental data that they reviewed in the same work [31].

As a matter of fact, at the basis of the development of equations of state there are experimental data. However, when designing and characterising the thermodynamics of novel fluids, experimental data are not available because not yet measured or not physically measurable. More specifically to this work, the design and characterisation of novel reversible chemical reactions to be used as working fluids in thermodynamic cycles, as an alternative to  $\text{N}_2\text{O}_4$ , requires to set up a predictive methodology.

In this context, this paper presents a methodology, that we have implemented to the mentioned scope, and applied to the well-known system  $\text{N}_2\text{O}_4 \rightleftharpoons 2 \text{NO}_2$ . It is worth noting that, in the presence of these two molecules, this is the only reaction taking place between 300 K and 410 K. However, between 410 K and 1150 K a second chemical reaction,  $2\text{NO}_2 \rightleftharpoons 2\text{NO} + \text{O}_2$ , occurs. In the interval of about 410 K – 600 K these two reactions take place simultaneously. In this preliminary work, the second reaction is not considered because we limit our discussion and calculations to a temperature range where the occurrence of this reaction is negligible. In this work, the definition of a thermodynamic model to enable the characterization of these systems is based on the complementary use of quantum chemistry, force field-based Monte Carlo simulations and equations of state. The only semi-empirical inputs to the methodology here presented are the force fields of  $\text{NO}_2$  and of  $\text{N}_2\text{O}_4$ , which are taken from Bourasseau et al. [32] and, as mentioned above, are optimised to reproduce experimental data.

The structure of the paper is presented in the following. Section 2.1 introduces the singular thermodynamic behaviour of bi-component reversible reactions, such as  $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$ , being characterized by phase equilibrium features similar to the ones of pure components, such as a unique critical and triple point, and a single vapour-liquid equilibrium (VLE) curve in the pressure-temperature space [36,37]. Sections 2.2 and 2.3 present, respectively, the set of equations applied to solve for chemical equilibrium in the presence of two coexisting phases and one chemical reaction, and the applied predictive equation of state. Section 2.4 introduces the way the ideal gas thermochemical properties (standard enthalpy of formation at 298.15 K, standard molar entropy at 298.15 K, heat capacities) and critical point coordinates of pure  $\text{NO}_2$  and of  $\text{N}_2\text{O}_4$  (required as an input to the equation of state) have been

calculated by Quantum Mechanic (QM) simulations and force field-based Monte Carlo simulations. Section 2.5 presents the methodology applied to perform force field-based Monte Carlo (MC) simulations on the studied reactive binary systems at VLE conditions, with a focus on the reactive  $N_2O_4 \rightleftharpoons 2NO_2$ , to characterize their phase equilibrium and volumetric properties of the coexisting vapour and liquid phases. Finally, section 3 presents the results obtained from QM and MC, and the final exploitation of those results in the application of equations of state, with the aim to characterize the full thermodynamics of binary reactive mixtures. Our findings are finally summarized in Section 4.

## 2. Methodology

Let us consider a binary system (A-B) undergoing the following general reversible reaction at its chemical equilibrium state:



The implementation of mass, energy and entropy balances in thermodynamic cycles operating with reactive working fluids requires (i) the availability of an equation of state for mixtures, (ii) algorithms enabling the resolution of chemical equilibrium, considering the presence of chemical reactions and, eventually, of coexisting vapour and liquid phases, (iii) ideal-gas standard enthalpy of formation at 298.15 K, ideal-gas standard molar entropy at 298.15 K and ideal-gas molar heat capacity as a function of temperature for each of the components present in the mixture. The latter properties are needed to calculate the equilibrium constant at any temperature, while the ideal gas heat capacities are also used to calculate the enthalpy and/or the entropy of a system containing the reactive fluid with an equation of state.

### 2.1. The number of degrees of freedom of the system

By definition, the number of degrees of freedom of a system, or its variance, is the number of intensive independent variables of its phases which must be fixed, in order to characterize all the intensive variables of the phases of the whole system. It can be demonstrated that the variance,  $v$ , of a mixture composed by  $c$ -molecular species,  $r$ -chemical reactions and  $\varphi$ -fluid phases, is given by [38]:

$$v = 2 - \varphi + c - r \quad (2)$$

If we consider binary and reactive systems such as the one considered in this paper,  $N_2O_4 \rightleftharpoons 2NO_2$ , i.e. a system involving only one reaction, it turns out that the variance of the system is equal to:

$$\begin{cases} v = 2 & \text{if } \varphi = 1 \\ v = 1 & \text{if } \varphi = 2 \end{cases}, \quad \text{with } c = 2 \text{ and } r = 1 \quad (3)$$

This result coincides with the variance of a system composed by one single molecular species (where  $c = 1$  and  $r = 0$ ). The latter explains why the pressure–temperature relation of this system in vapour liquid equilibrium conditions is qualitatively similar to the vapor pressure of a pure component (Fig. 1). In addition, other singular features will be shown in section 3.2.2.

### 2.2. Fluid phase and reaction chemical equilibrium

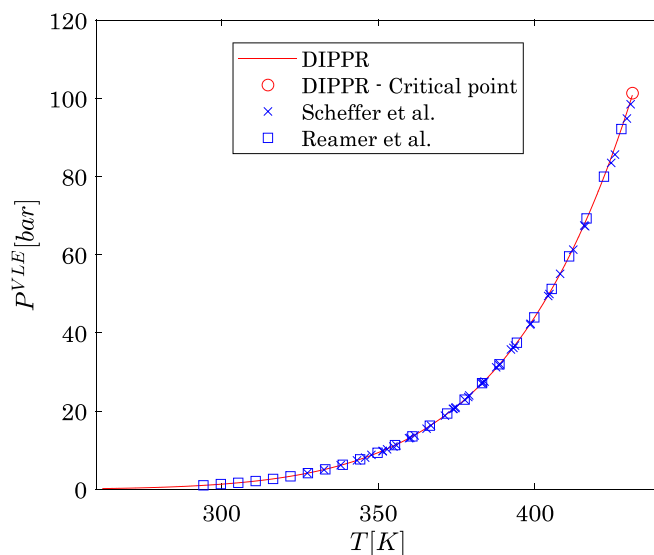
Let us consider the chemical reaction reported in eq. (1). The chemical equilibrium condition states that the Gibbs energy of reaction of the system,  $\Delta_R G$ , equals zero:

$$\Delta_R G \triangleq \sum_{i=A,B} \nu_i \bar{g}_i = 0 \quad (4)$$

That is,

$$\nu_B \bar{g}_B - \nu_A \bar{g}_A = 0 \quad (5)$$

In which  $\bar{g}_i$  is the partial molar Gibbs energy (chemical potential) of



**Fig. 1.** Vapour-liquid equilibrium pressure ( $P^{VLE}$ ) as a function of temperature ( $T$ ) for the reacting binary mixture  $N_2O_4 \rightleftharpoons 2NO_2$ . Blue points are experimental data from Scheffer and Treub [39] and Reamer and Sage [40]; red line and its end critical point (circle) are from DIPPR [41]. As expected, such a curve is very similar to the vaporization curve of a pure component.

species  $i$  and  $\nu_i$  the algebraic stoichiometric coefficient. If the system is single phase, eq. (5) applies to that phase (liquid or vapour) and eq. (5) becomes:

$$\nu_B \bar{g}_B^{liq} - \nu_A \bar{g}_A^{liq} = 0 \quad (6)$$

Or

$$\nu_B \bar{g}_B^{vap} - \nu_A \bar{g}_A^{vap} = 0 \quad (7)$$

In the case the system is in vapor–liquid equilibrium (VLE), the fluid-phase equilibrium condition between the vapour and the liquid phase dictates that the partial molar Gibbs energy of each species is the same in all phases [38]:

$$\begin{cases} \bar{g}_B^{liq} = \bar{g}_B^{vap} \\ \bar{g}_A^{liq} = \bar{g}_A^{vap} \end{cases} \quad (8)$$

As a consequence, equations (6) and (7) are simultaneously satisfied which demonstrates that the chemical reaction takes place in the two phases, simultaneously; indeed, it results:

$$\Delta_R G^{liq} = \Delta_R G^{vap} = 0 \quad (9)$$

In other words, for a two-phase system, the condition  $\Delta_R G^{vap} = 0$  is sufficient to impose that  $\Delta_R G^{liq} = 0$ , and vice-versa.

The expression of the Gibbs energy of reaction,  $\Delta_R G$ , is recalled in the Supplementary Materials (section S1) as a function of:

- ideal gas properties (ideal gas standard molar enthalpy of formation at 298.15 K, ideal gas standard molar entropy at 298.15 K, and ideal gas isobaric heat capacity of each species of the mixture) obtained at the atomic level using ab-initio calculations

and

- real fluid properties (the fugacity of each species) determined by an equation of state.

The system of equations that needs to be solved to determine the chemical equilibrium of the binary reactive system in VLE can be written as follows:

$$\begin{cases} \hat{g}_A^{liq} = \hat{g}_A^{vap} \\ \hat{g}_B^{liq} = \hat{g}_B^{vap} \\ \Delta_R G = 0 \text{ i.e. } K - \mathcal{P} = 0 \end{cases} \quad (10)$$

where,  $\mathcal{P} \triangleq \prod_{i=A,B} \left( \frac{\hat{f}_i}{P^\circ} \right)^{\nu_i}$ ,  $\hat{f}_i$  is the fugacity of component  $i$ ,  $P^\circ$  is the standard pressure,  $P^\circ = 1 \text{ bar}$ , and  $K$  is the reaction equilibrium constant, related as follows to the standard Gibbs energy of reaction,  $\Delta_R G^\circ$ ,

$$\ln K(T) \triangleq - \frac{\Delta_R G^\circ(T)}{RT} \quad (11)$$

In our case, the previous system of equations will be solved by an equation of state so that the uniformity of the chemical potential equation ( $\hat{g}_i^{liq} = \hat{g}_i^{vap}$ ) is simply replaced by the isofugacity equation ( $\hat{f}_i^{liq} = \hat{f}_i^{vap}$ ). However, in doing so, 2 new variables appear: the molar volumes of the liquid ( $v^{liq}$ ) and vapor ( $v^{vap}$ ) phases since the fugacity  $\hat{f}_i$ , derived from an equation of state, depends on temperature, composition and molar volume. It is therefore necessary to add 2 mathematical equations to reflect the fact that the variables  $T$ ,  $P$ ,  $v$  and composition are linked in each phase by the EoS. Finally, we get:

$$\begin{cases} \hat{f}_A^{liq}(T, v^{liq}, \mathbf{x}) = \hat{f}_A^{vap}(T, v^{vap}, \mathbf{y}) \\ \hat{f}_B^{liq}(T, v^{liq}, \mathbf{x}) = \hat{f}_B^{vap}(T, v^{vap}, \mathbf{y}) \\ K(T) - \mathcal{P} = 0 \\ P - P_{EoS}(T, v^{liq}, \mathbf{x}) = 0 \\ P - P_{EoS}(T, v^{vap}, \mathbf{y}) = 0 \end{cases} \quad (12)$$

In eq. (12),  $\mathcal{P}(T, v, \mathbf{z})$  can be calculated for either the liquid or gas phase since  $\mathcal{P}^{vap} = \mathcal{P}^{liq}$ .  $\mathbf{x}$  and  $\mathbf{y}$  denote the composition of the liquid  $\mathbf{x} = \{x_A, x_B = 1 - x_A\}$  and vapor phase  $\mathbf{y} = \{y_A, y_B = 1 - y_A\}$  respectively.  $P_{EoS}(T, v, \mathbf{z})$  is the pressure of the system, calculated as a function of temperature,  $T$ , molar volume,  $v$  and molar composition,  $\mathbf{z}$ , either of the liquid ( $\mathbf{z} = \mathbf{x}$ ) or of the vapour phase ( $\mathbf{z} = \mathbf{y}$ ) with a specifically selected EoS. The EoS model applied in this work is presented in the section 2.3. To conclude this section, we recall that the reactive system in VLE is monovariant. It is therefore necessary to specify an intensive variable before solving the system of equations. As an example, if the temperature is specified, the 5 equations make it possible to calculate  $P$ ,  $v^{liq}$ ,  $v^{vap}$ ,  $x_A$  and  $y_A$ .

### 2.3. The proposed predictive equation of state

The cubic Peng-Robinson equation of state [42], given by eq. (13), is used in this work to estimate the fugacities of each component:

$$P(T, v, z) = \frac{R \cdot T}{v - b_m} - \frac{a_m}{v(v + b_m) + b_m(v - b_m)} \quad (13)$$

where  $\mathbf{z}$  is the vector of the molar composition,  $T$  is the temperature,  $R$  is the universal gas constant and  $a_m$  and  $b_m$  are the mixing energy and co-volume parameters. The latter are calculated in this work with advanced mixing rules [43]:

$$\begin{cases} b_m = \sum_{i=1}^{NC} z_i b_i \\ \frac{a_m}{b_m} = \sum_{i=1}^{NC} z_i \frac{a_i}{b_i} + \frac{a_{res}^{E,\gamma}}{\Lambda_{EoS}} \end{cases} \quad (14)$$

where,  $a_{res}^{E,\gamma}$  is the residual part of an excess Helmholtz energy model calculated from an activity coefficient ( $\gamma$ ) model,  $\Lambda_{EoS}$  is a numerical parameter being a function of the considered equation of state [43], the pure component energy and co-volume parameters, i.e.  $a_i$  and  $b_i$ , respectively, are calculated using eq. (15).

$$\begin{cases} R = 8.314472 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1} \\ X = \left[ 1 + \sqrt[3]{4 - 2\sqrt{2}} + \sqrt[3]{4 + 2\sqrt{2}} \right]^{-1} \approx 0.253076587 \\ b_i = \Omega_b \frac{RT_{c,i}}{P_{c,i}} \text{ with: } \Omega_b = \frac{X}{X+3} \approx 0.0777960739 \\ a_{c,i}(T) = a_{c,i} \alpha_i(T) \text{ with } \begin{cases} a_{c,i} = \Omega_a \frac{R^2 T_{c,i}^2}{P_{c,i}} \text{ and } \Omega_a = \frac{8(5X+1)}{49-37X} \approx 0.457235529 \\ \alpha_i(T) = \left[ 1 + m_i \left( 1 - \sqrt{\frac{T}{T_{c,i}}} \right) \right]^2 \end{cases} \\ \text{if } \omega_i \leq 0.491 \text{ then } m_i = 0.37464 + 1.54226\omega_i - 0.26992\omega_i^2 \\ \text{if } \omega_i > 0.491 \text{ then } m_i = 0.379642 + 1.48503\omega_i - 0.164423\omega_i^2 + 0.016666\omega_i^3 \end{cases} \quad (15)$$

More precisely, a zero-residual excess Helmholtz energy part,  $a_{res}^{E,\gamma}$ , is considered for this work. In other words, the  $\text{NO}_2/\text{N}_2\text{O}_4$  binary system is assumed to be athermal because the intermolecular forces between non-polar  $\text{N}_2\text{O}_4$  molecules are weak, as well as between  $\text{N}_2\text{O}_4$  and  $\text{NO}_2$ . Clearly, the interaction between  $\text{NO}_2$  radicals is strong at low temperature and gives rise to the association reaction, which is indeed accounted for as being a chemical reaction in the system. The use of a zero residual excess Helmholtz energy leads to a model free of semi-empirical binary interaction parameters to be adjusted (otherwise present in the residual excess Helmholtz energy model) and will thus work in a predictive way.

### 2.4. The determination of thermochemical and thermophysical properties of pure fluids ( $\text{N}_2\text{O}_4$ and $\text{NO}_2$ )

It is worth recalling that while the use of an equation of state is sufficient to perform VLE calculations, the ideal gas heat capacity,  $c_{p,i}^{ig}(T)$ , of each species is needed for the determination of derived thermodynamic properties, such as the enthalpy or the entropy of a given phase [44]. Moreover, as recalled in eq. (S7) of the Supplementary Materials, the calculation of the ideal-gas standard enthalpy and entropy of reaction requires the knowledge – for each species – of the standard enthalpy of formation at 298.15 K,  $\Delta_f H_{i,298.15K}^\circ$ , the molar entropy at 298.15 K,  $S_{i,298.15K}^\circ$ , and the heat capacity as a function of temperature.

The temperature-dependent ideal gas heat capacity, the standard enthalpy of formation and the standard molar entropy of the pure components can be obtained by QM calculations, as explained in section 2.4.1, where the case of  $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$  is considered as an example.

Also, as shown in the previous section 2.3, the application of the Peng-Robinson equation of state (eqs. (13)-(15)) requires the knowledge of the temperature and pressure of the critical point of the two species forming the mixture,  $T_{c,i}$  and  $P_{c,i}$ , and their acentric factors,  $\omega_i$ . Since the species forming any fast and reversible chemical reaction, i.e.  $\text{N}_2\text{O}_4$  and  $\text{NO}_2$  in the  $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$  system, do not exist in their pure form, the experimental measurement of such properties is physically not feasible. To overcome this problem, force field-based Monte Carlo simulations have been performed in this work, with two available MC softwares, Brick-Continuous-Fractional-Component-Monte-Carlo (CFCMC) [45] and Monte Carlo GIBBS [46], to determine  $P$ - $\rho$ - $T$  properties of the pure  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  and, thus, to deduce their critical point properties and acentric factors, as explained in section 2.4.2.

#### 2.4.1. Quantum mechanics simulations

The thermochemical properties of  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , i.e. the ideal gas standard enthalpy of formation at 298.15 K, standard molar entropy at 298.15 K, and heat capacity, have been calculated using software Gaussian 09 (revision B.01) [47] and the GPOP post-processing software suite from Miyoshi [48].



QM calculations were performed at the CBS-QB3 level of theory [49]. A conformational analysis was performed for  $N_2O_4$  at the B3LYP/6-31G(d) level [50], to determine the most stable conformer, that is the conformer corresponding to the lowest electronic energy. The conformational analysis consists in varying the considered dihedral angle by a step of  $10^\circ$  and re-optimizing all degrees of freedom except the dihedral angle, at each step. Also, internal modes are treated as harmonic oscillators in Gaussian; the conformational analysis enables to understand the validity of the Gaussian's harmonic oscillator assumption for internal rotation of moieties around simple bonds, such as the N–N bond in the  $N_2O_4$  molecule. In general, if the conformational analysis shows that the highest energy gap between adjacent maximum and minimum energies, represented as an example in Fig. 2, is lower than  $R \cdot T$  (where  $R$  is the universal gas constant), then the harmonic oscillator model is not valid because internal rotation can occur. In such a case, the results have to be corrected accounting for the hindered rotor model [51]. In this work, this treatment is done with GPOP and requires as an input the Gaussian's rotational hindrance potential. The post-processing is also performed with GPOP and enables the estimation of the standard enthalpy of formation and of the standard molar entropy.

To determine the equilibrium constant of the reactive system, and thus perform Monte Carlo simulations for the reactive system as shown in section 2.5, it is necessary to calculate the partition function of the isolated molecules. Those can be obtained from available thermochemistry data (JANAF tables) or from quantum mechanical calculations (with Gaussian), from which it is possible to determine the atomisation energy and the rotational and vibrational temperatures used as an input to the calculation of the partition function of the isolated molecules.

#### 2.4.2. Monte Carlo simulations with Brick-CFCMC software

To perform Monte Carlo simulations of  $N_2O_4$  and  $NO_2$ , a classical force field is used in which interatomic interactions are described by both Lennard-Jones (LJ) and electrostatic interactions.  $NO_2$  is treated as a rigid molecule. Concerning the  $N_2O_4$  molecule, this molecule is rigid as well, except when the rotation of  $NO_2$  moieties is considered and the rotational hindrance potential is then required as additional input for the MC simulations. The potential is deduced by optimising the parameters of a cosine series, on the rotation energy scan obtained with Gaussian.

Lennard-Jones interactions are truncated at  $12 \text{ \AA}$  and analytic tail corrections are used [52]. Electrostatics are computed using the Ewald

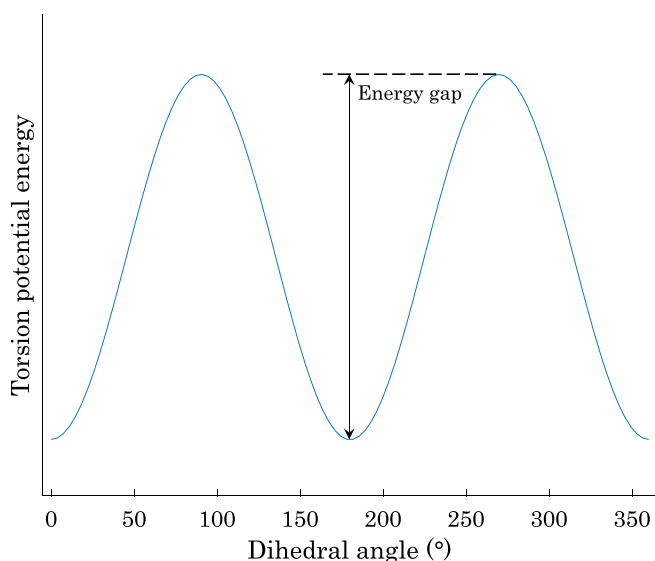


Fig. 2. Example of correlated torsion potential energy obtained in Gaussian by varying the dihedral angle of the molecule.

summation technique with a relative precision of  $10^{-5}$ . The force field parameters of  $NO_2$  and  $N_2O_4$  are taken from Bourasseau et al. [32] and are also listed in Table S1 of the Supplementary Materials. For atoms that are not identical, the Lorentz-Berthelot mixing rules [52,53] are used. The intermolecular coordinates of  $NO_2$  and  $N_2O_4$  are respectively listed in Table S2 and Table S3 of the Supplementary Materials. Three-dimensional systems with periodic boundary conditions are considered in all simulations.

Pure component Gibbs ensemble simulations using the Continuous Fractional technique [54–56] were performed using the Brick-CFCMC software [45,57]. In the constant volume-constant temperature (NVT) version of the Gibbs ensemble [52,53], there are two simulation boxes that can exchange volume, energy, and molecules, in such a way that the simulation boxes resemble the coexisting phases at equilibrium. Molecule transfers between both simulation boxes are facilitated using a single fractional molecule per component [58]. The interactions of such a fractional molecule are determined by an order parameter  $\lambda$ , with  $\lambda = 0$  when the fractional molecule has no interactions with the surrounding molecules, and  $\lambda = 1$  when the fractional molecule has full, unaltered, interactions with the surrounding molecules. Besides thermalization trial moves (molecule translations, molecule rotations, and volume changes), the simulation requires three additional trial moves [58]: (1) attempts to change the value of  $\lambda$ ; (2) attempts to transfer a fractional molecule from one simulation box to the other one; (3) attempts to transform the fractional molecule into a whole molecule, and simultaneously, transform a “whole” molecule in the other simulation box into a fractional molecule, at the same value of  $\lambda$ . Biasing using the Wang-Landau algorithm [59] is needed to ensure that the probability distribution of  $\lambda$  is flat in both boxes, and that fractional molecules are equally likely to be in the simulation boxes. The chemical potential of component  $i$  in simulation box A follows directly from [45,57,60]:

$$\mu_i^A = k_B T \left( - \ln \left( \frac{q_i}{\Lambda_i^3 \rho_0} \right) + \ln \left( \frac{\rho_i^A}{\rho_0} \right) - \ln \left( \frac{p(\lambda_i^A = 1)}{p(\lambda_i^A = 0)} \right) \right) \quad (16)$$

in which  $k_B$  is the Boltzmann constant,  $T$  is the absolute temperature,  $q_i$  is the intramolecular part of the isolated molecule partition function of molecule type  $i$  (excluding the translational part),  $\Lambda_i$  is the thermal wavelength of molecule type  $i$ ,  $\rho_0$  is an arbitrary reference density set to 1 molecule per cubic Angstrom,  $\rho_i^A$  is the number density of component  $i$  in simulation box A, and  $p(\lambda_i^A)$  is the Boltzmann probability distribution of the value of  $\lambda$  of component  $i$  in simulation box A. The term  $q_i/\Lambda_i^3$  can be obtained either from QM simulation or thermochemical tables (e.g. the JANAF tables), see Refs. [45,57,61] for details. At phase equilibrium, chemical potentials of component  $i$  are equal in both simulation boxes. As the Brick-CFCMC software does not compute pressures, a series of simulations in the constant temperature–pressure (NPT) ensemble are carried out around the density of the gas phase box. The coexistence pressure is calculated by matching the gas phase density to the NPT simulations via interpolation. For more details on the simulation technique and the derivation of the accepted probabilities of the trial moves, the reader is referred to Refs. [45,57,58].

#### 2.4.3. Monte Carlo simulations with GIBBS software

In this paper, other Monte Carlo results are presented for  $N_2O_4$  and  $NO_2$ . These molecular simulations have been performed using NVT Gibbs ensemble Monte Carlo (MC) [62], with the “GIBBS Monte Carlo” code [46], to determine the saturation densities and pressures of pure  $N_2O_4$  and pure  $NO_2$ . In this MC algorithm, the sampling of the configurational space is ensured by three Monte Carlo moves: rigid body translations or rotations of molecules, and volume changes. More specifically, differently with respect to the calculations performed in this work with Brick-CFCMC software,  $NO_2$  and  $N_2O_4$  molecules have been both represented as rigid molecules. Thus, in these simulations,  $N_2O_4$  is not allowed to make torsional rotations, while in Brick the torsional potential is modelled as determined from Quantum Mechanics

simulations. However, the force field parameters in these simulations coincide with the ones from Bourasseau et al. [32], like in settings used in Brick. In all simulations performed with GIBBS code, a cutoff for LJ intermolecular interactions equal to the half of the simulation box length has been used to reduce the computing time. Beyond the cutoff, standard long-range corrections have been employed. For more details on the simulation technique or on the molecular models used to determine these latter MC results, the reader is invited to refer to some previous works [32,63–65].

#### 2.4.4. The derivation of critical coordinates and acentric factors

The determination of the critical point properties by MC is not straightforward, since the Gibbs ensemble is not applicable in the vicinity of the critical region [52]. To localize the critical point, we have proceeded as described below.

Once  $P$ - $\rho$ - $T$  properties in saturation conditions are calculated by MC, the critical temperature  $T_{c,i}$  of the pure compounds,  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , are obtained by extrapolation from the sub-critical simulation points, assuming the following scaling law:

$$\rho_i^{\text{liq}}(T) - \rho_i^{\text{vap}}(T) = B_i(T_{c,i} - T)^\beta \quad (17)$$

where  $\rho_i^{\text{liq}}(T)$  and  $\rho_i^{\text{vap}}(T)$  are the densities of component  $i$  at temperature  $T$  in the liquid and the vapor phases, respectively, calculated with Monte Carlo simulations, while  $\beta$  is the critical exponent, equal to  $0.32 \pm 0.01$  [66]. The critical temperature of each  $i$ -th component,  $T_{c,i}$ , and its parameter  $B_i$ , also component-dependent, have been regressed by least square method minimizing the following objective function,  $O.F.$ :

$$O.F.: \min_{T_{c,i}, B_i} \left\{ \sqrt{\sum_{k=1}^{NP} \left( \rho_k^{\text{liq},MC}(T_k) - \rho_k^{\text{vap},MC}(T_k) - B_i(T_{c,i} - T_k)^\beta \right)^2} \right\} \quad (18)$$

where  $NP$  is the number of data points. The critical density,  $\rho_{c,i}$ , is then calculated with the application of the law of rectilinear diameter,

$$\frac{\rho^{\text{liq}}(T) + \rho^{\text{vap}}(T)}{2} = \rho_{c,i} - A_i(T_{c,i} - T) \quad (19)$$

and the least square optimization,

$$O.F.: \min_{\rho_{c,i}, A_i} \left\{ \sqrt{\sum_{k=1}^{NP} \left( \frac{\rho_k^{\text{liq},MC}(T_k) + \rho_k^{\text{vap},MC}(T_k)}{2} - \rho_{c,i} + A_i(T_{c,i} - T_k) \right)^2} \right\} \quad (20)$$

Moreover, from the calculated  $P$ - $T$  saturation points of the two pure fluids, a correlation  $P_i^{\text{sat}}(T)$  is determined

$$\ln P_i^{\text{sat}}(T) = \alpha_i + \frac{\beta_i}{T} \quad (21)$$

where, parameters  $\alpha_i$  and  $\beta_i$  are determined by minimizing:

$$O.F.: \min_{\alpha_i, \beta_i} \left\{ \sqrt{\sum_{k=1}^{NP} \left( \exp\left(\alpha_i + \frac{\beta_i}{T_k}\right) - P_i^{\text{sat}}(T_k) \right)^2} \right\} \quad (22)$$

and  $P_{c,i}$  can be finally calculated from the optimized correlations, eq. (21), as a function of  $T_{c,i}$ .

Once  $T_{c,i}$  and  $P_{c,i}$  are obtained, the acentric factor  $\omega_i$  is calculated from its definition:

$$\omega_i = -\log_{10} P_{r,i}^{\text{sat}} - 1 \quad (23)$$

where  $P_{r,i}^{\text{sat}}$  is the reduced vapor pressure ( $P_i^{\text{sat}}/P_{c,i}$ ) at a reduced temperature ( $T/T_{c,i}$ ) equal to 0.7.

#### 2.5. The determination of thermodynamic properties of the reactive $\text{N}_2\text{O}_4 \rightleftharpoons 2 \text{NO}_2$

To study the VLE phase coexistence of the reactive system  $\text{N}_2\text{O}_4 \rightleftharpoons 2 \text{NO}_2$ , Monte Carlo simulations in the reactive Gibbs Ensemble [33,34,60,67,68] are performed with Brick-CFCMC [45]. In these simulations, the constant-volume Gibbs Ensemble setup of section 2.4.2 is coupled to a grand-canonical reservoir of molecules of  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ . The imposed chemical potentials of  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  are set such that the system is at chemical equilibrium so  $\mu_{\text{N}_2\text{O}_4} = 2 \cdot \mu_{\text{NO}_2}$  and the exchanges from the reservoir are such that the total number of atoms of each type in the system is conserved. A fractional group is added to the vapor box of the Gibbs Ensemble, which contains fractional molecules of either the reactants or the reaction products [60]. Note that this group of fractional molecules is completely independent from the fractional molecules required for molecule transfers between the simulation boxes (as used in the CFCMC version of the Gibbs Ensemble described in section 2.4.2). In addition to the trial moves of the CFCMC version of the Gibbs Ensemble (section 2.4.2), the following trial moves (which all operate in the vapor box) are used for the molecules in the fractional group: (1) attempts to change the order parameter  $\lambda_R$  for the molecules in the fractional group.  $\lambda_R = 0$  means that the molecules in the fractional group have no interaction with the surrounding molecules, and  $\lambda_R = 1$  means that the molecules in the fractional group have full, unaltered interactions with the surrounding molecules; (2) attempts to transform the molecules in the fractional group from reactants into reaction products, or vice-versa. This requires the terms  $q_i/\Lambda_i^3$  for  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ ; (3) attempts to transform the fractional molecules in the group into “whole” molecules, and simultaneously, transform “whole” molecules into a fractional group, in such a way that the fractional group changes from reactants to reaction products (or vice versa). In this trial move, the value of  $\lambda_R$  is unchanged. Biasing is needed to ensure that it is equally likely that the fraction group contains a single fractional molecule of  $\text{N}_2\text{O}_4$ , or two fractional molecules of  $\text{NO}_2$ , and that each value of  $\lambda_R$  is equally likely. At combined chemical equilibrium and phase equilibrium, we have  $\mu_{\text{N}_2\text{O}_4} = 2 \cdot \mu_{\text{NO}_2}$  for both simulation boxes A and B, and  $\mu_i^A = \mu_i^B$  for both  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ . The coexistence pressure is obtained by performing a series of NPT simulations at the average composition of the gas phase box, and use interpolation to match the simulated gas phase density from the Gibbs ensemble simulation in the reaction ensemble. For more details about the simulation setup and the derivation of the acceptance rules, the reader is referred to Refs. [45,60]. The isolated molecule partition function for both  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  were obtained in this work both from QM simulations, by using Gaussians outputs reported in Table S4 of the Supplementary Materials, and the thermochemical results reported in JANAF tables [45]. The calculated partition functions are shown in Fig. 3, where  $V_0 = 1 \text{ \AA}^3$ . Two correlations that correlate the JANAF values are proposed below,

$$\ln \left( \frac{qV_0}{\Lambda^3} \right)_{\text{NO}_2} = \frac{110983.613}{T} + 16.403 \quad (24)$$

$$\ln \left( \frac{qV_0}{\Lambda^3} \right)_{\text{N}_2\text{O}_4} = \frac{228591.177}{T} + 23.218 \quad (25)$$

### 3. Results

This section presents the results obtained from molecular simulations, as well as the calculations performed with the cubic equation of state and enabled by the calculated equation of state's input critical temperature, pressure and acentric factor of the pure fluids  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ .

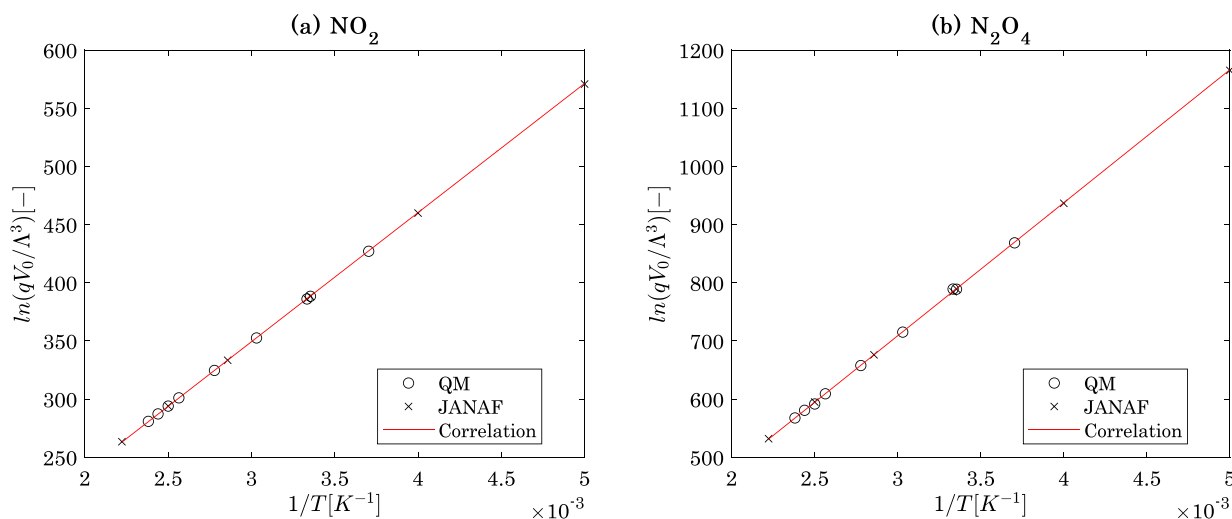


Fig. 3. Natural logarithm of the partition functions,  $q$ , divided by the thermal wavelength, for  $NO_2$  (fig. (a)) and  $N_2O_4$  (b). Data obtained from the JANAF tables. Correlations are eqs. (24) and (25).

### 3.1. Thermochemical and thermophysical properties of $N_2O_4$ and $NO_2$

#### 3.1.1. Quantum Mechanics results

Fig. 4 shows the geometries of  $NO_2$  and  $N_2O_4$ , optimised with Gaussian as discussed in section 2.4.1. It is worth noting that the length of N = O bonds and the N = O = N angles are very similar in both  $NO_2$  and  $N_2O_4$ , which indicates that very limited rearrangements occur in moieties when  $N_2O_4$  splits into two  $NO_2$  moieties. The main specificity of  $N_2O_4$  is the length of the N-N bond which is particularly long for such a bond: 1.797 Å compared to 1.487 Å for the N-N bond in hydrazine (value obtained at the CBS-QB3 level of theory with software Gaussian) and which can be attributed to an inductive effect of the vicinal oxygen atoms. This has consequently an impact on the energy of that particular bond as discussed further. Fig. 5 shows the result of the conformational analysis that was performed to verify that the optimized geometry obtained for  $N_2O_4$  corresponds well to the conformer with the lowest energy. The optimal coefficients for the torsion potential  $N_2O_4$  are shown in Table S5 of the Supplementary Materials. As expected, two distinct stable conformations exist for  $N_2O_4$ : a planar one with the lowest energy, and a skew one with an energy ca. 30 kJ/mol higher than that one the planar conformer. As it will be confirmed by MC simulation results considering the torsion of  $N_2O_4$  (see section 3.1.2), the calculated potential barrier shows that the actually observed conformations are plane or almost plane. Some studies [69] focused on the origin of the greater stability of the planar conformer, but this is beyond the scope of the present work.

As enthalpies provided by the Gaussian software are relative to a reference that is specific to the method used, they need to be rescaled. For  $NO_2$ , we considered in the present work the fictive reaction (2)  $NO_2 + N_2$

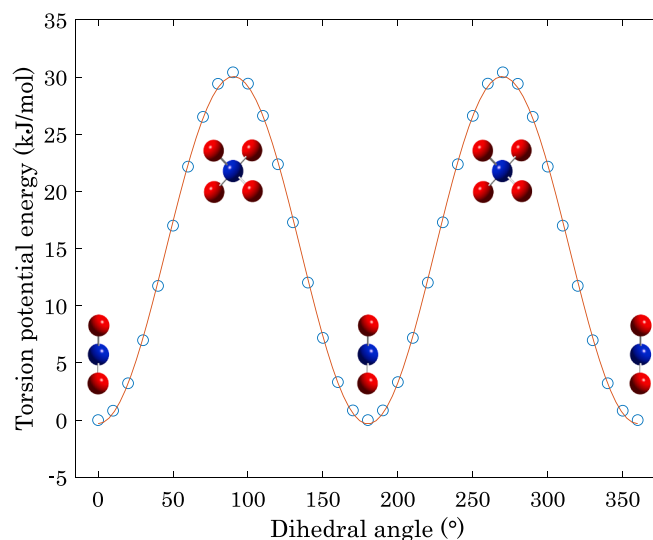


Fig. 5. Conformational analysis of  $N_2O_4$ . The points in the figure represent Gaussian results, while the line is the cosine series fitted to the QM results.

$\rightleftharpoons 4 NO$  leading to  $\Delta_f H_{i,298.15K}^\circ$  equal to 34.20 kJ/mol, which compares well to the data available in the NIST database [70] (33.1 kJ/mol). For  $N_2O_4$ , the fictive reaction considered was  $N_2O_4 \rightleftharpoons 2 NO_2$  leading to  $\Delta_f H_{i,298.15}^\circ$  equal to 9.99 kJ/mol, to be compared with the value of 9.08 kJ/mol provided in the NIST database. This leads to an enthalpy of reaction of 56.2 kJ/mol for

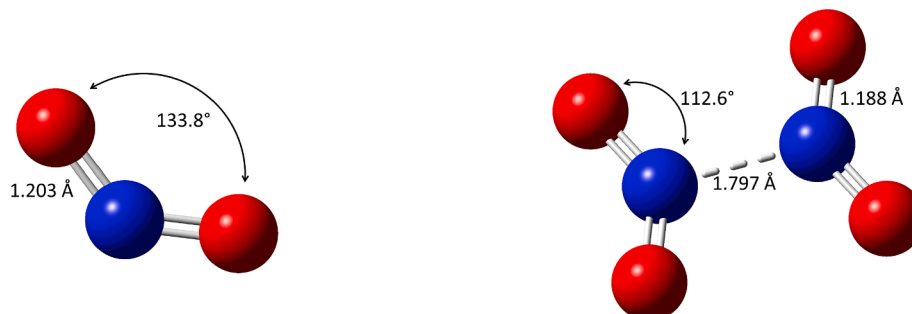


Fig. 4. Optimal geometry of  $NO_2$  and  $N_2O_4$ . Atomic coordinates are reported in Table S2 and S3 the Supporting Information.



the reaction of dissociation of  $\text{N}_2\text{O}_4$  into two  $\text{NO}_2$  moieties (57.12 kJ/mol using the NIST data), confirming that the value of the N-N bond is unusually low and in line with the bond length of 1.797 Å.

For the ideal-gas standard molar entropy,  $S_{i,298.15\text{K}}^\circ$ , assuming an external symmetry number of 2 for  $\text{NO}_2$ , the value derived with post-processing Gaussian results with GPOP, as briefly described in section 2.4.1, is 240.03 J/mol/K which compares very well to the data in the NIST database (240.04 J/mol/K). For  $\text{N}_2\text{O}_4$ , assuming an external symmetry number of 4, the calculated standard entropy is 297.65 J/mol/K, which is a bit lower than the data provided in the NIST database (304.38 J/mol/K) but still within the acceptable range. At such a low temperature, the difference in entropy for the  $-\text{NO}_2$  rotor is only 0.54 J/mol/K between the harmonic oscillator approximation and the hindered rotor one, as a consequence of the fact that the highest energy gap between adjacent maximum and minimum energy (i.e., the torsional barrier) is higher than  $R \cdot T = 2.47$  kJ/mol at 298.15 K and thus the harmonic oscillator assumption is still valid (see section 2.4.1). The results obtained are summarised in Table 1.

Another result obtained from the postprocessing step is the ideal gas isobaric specific heat capacity, which has been correlated to the DIPPR correlation n. 107:

$$c_{p,i}^{\text{ig}}(T) = c_0 + c_1 \left( \frac{c_2/T}{\sinh(c_2/T)} \right)^2 + c_3 \left( \frac{c_4/T}{\cosh(c_4/T)} \right)^2 \quad (26)$$

The coefficients optimised in this work for  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  are reported in Table 2 and shown in Fig. S1 and S2 of the Supplementary Materials.

### 3.1.2. Monte Carlo results

The MC simulations performed with Brick-CFCMC enabled the computation of coexisting densities and saturation pressures of the two pure compounds,  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , at different temperatures. Results are presented in Table 3 and Table 4 as well as in Figs. 6–9. MC simulations of  $\text{N}_2\text{O}_4$  have shown that the most probable conformer is the planar one, according to the potential barrier calculated in Fig. 5.

More precisely, Fig. 6 and Fig. 7 show the densities of the liquid and vapour phase of, respectively,  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , as a function of temperature. A comparison between the results of the two different sets of simulations show an excellent agreement between the two methods. Main quantitative differences between the results of Brick-CFCMC and GIBBS may derive from slightly different implementation of the Ewald summation, or from a different cutoff and from the additional consideration (in Brick-CFCMC calculations) of torsion potential of  $\text{N}_2\text{O}_4$ . Moreover, these figures show the predicted critical points ( $T_{c,i}$ ,  $\rho_{c,i}$ ) of both  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , optimized over the two sets of data. It can be observed that despite simulations performed with Brick-CFCMC did not converge close to the critical point, the prediction of the critical point obtained from this set of data is acceptably similar to the one obtained with GIBBS code which better converges close to the critical point. It is highlighted that the uncertainties of MC simulations from Brick-CFCMC and GIBBS are not shown in Fig. 6 and Fig. 7, for the sake of simplicity, but are reported in Table 3 and in Table 4.

The calculated saturation pressures for the pure components are shown in Fig. 8 and Fig. 9, for  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  respectively. As described in section 2.4.4, the correlation in eq. (21) has been optimized for both components, over the experimental data obtained by Brick-CFCMC, and this is also reported in these figures. Coefficients of the correlations are

**Table 1**

Ideal gas standard properties at 298.15 K, obtained in this work by quantum mechanics.

	$\text{NO}_2$	$\text{N}_2\text{O}_4$
$\Delta_f H_{i,298.15}^\circ$ (kJ/mol)	34.20	9.99
$S_{i,298.15\text{K}}^\circ$ (J/mol/K)	240.03	297.65

**Table 2**

Coefficients for the calculation of the isobaric specific heat capacity of  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  by eq. (26).

	$c_0$ [J/mol/K]	$c_1$ [K]	$c_2$ [K]	$c_3$ [K]	$c_4$ [K]
<b><math>\text{NO}_2</math></b>					
QM, this work	33.631	24.566	1.1684	10.4065	0.6063
DIPPR [41]	33.261	24.919	1.1122	9.2534	0.5592
<b><math>\text{N}_2\text{O}_4</math></b>					
QM, this work	67.574	56.723	0.72373	13.722	2.0934
DIPPR [41]	65.796	58.428	0.69602	11.887	2.0748

**Table 3**

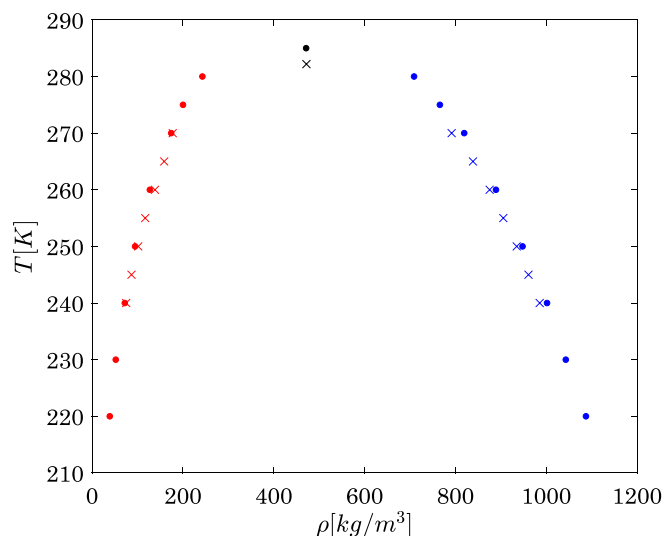
Results of MC simulations obtained for pure  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , obtained in this work by the use of Brick-CFCMC. “u” denotes the uncertainty of the calculated variables. These uncertainties correspond to the standard deviation between the results of MC simulations performed at each temperature to calculate saturation densities and pressures.

$T$ [K]	$p^{\text{sat}}$ [bar]	$u(P)$ [bar]	$\rho_{\text{liq}}$ [kg/m <sup>3</sup> ]	$\rho_{\text{vap}}$ [kg/m <sup>3</sup> ]	$u(\rho_{\text{liq}})$ [kg/m <sup>3</sup> ]	$u(\rho_{\text{vap}})$ [kg/m <sup>3</sup> ]
<b><math>\text{NO}_2</math></b>						
240	25.07	0.45	985.6	74.9	1.3	1.9
245	28.60	0.31	960.9	86.6	1.6	1.5
250	32.82	0.84	935.0	101.4	2.3	4.1
255	37.11	0.52	905.5	116.8	1.9	2.9
260	42.42	1.01	875.4	138.3	3.5	6.2
265	47.39	1.33	838.7	158.6	3.5	8.9
270	52.10	0.92	791.7	177.3	6.2	7.0
<b><math>\text{N}_2\text{O}_4</math></b>						
260	0.107	0.020	1537.6	0.454	1.9	0.085
270	0.175	0.036	1516.5	0.72	1.3	0.15
280	0.332	0.026	1494.1	1.31	1.1	0.10
290	0.457	0.038	1472.2	1.75	0.7	0.15
300	0.752	0.101	1449.0	2.80	0.5	0.38
310	1.046	0.093	1424.8	3.79	1.1	0.34
320	1.55	0.12	1401.8	5.47	1.1	0.43
330	2.23	0.20	1377.4	7.71	1.0	0.72
340	2.90	0.17	1352.3	9.85	0.3	0.63
350	4.11	0.14	1326.0	13.8	1.0	0.52
360	5.04	0.12	1299.3	16.6	0.7	0.45
370	6.67	0.13	1269.40	21.8	0.73	0.48
380	8.51	0.31	1240.68	27.6	2.40	1.13
390	10.63	0.35	1210.22	34.5	1.50	1.30
400	13.17	0.38	1176.49	42.4	1.66	1.48
410	16.55	0.18	1141.44	52.9	0.99	0.71
420	19.76	0.35	1098.91	63.2	1.39	1.47
430	22.97	0.40	1050.68	73.8	5.37	1.67
440	26.54	0.68	989.79	85.8	6.12	2.89

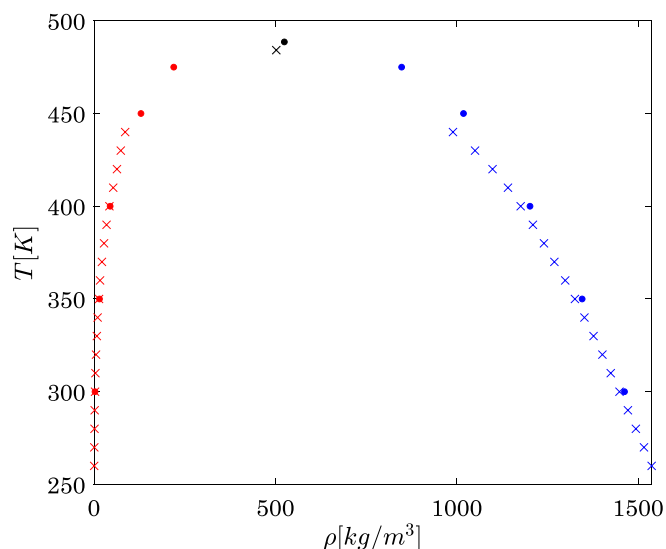
**Table 4**

Results of MC simulations obtained for pure  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$ , obtained with GIBBS code. “u” denotes the uncertainty of the calculated variables. These uncertainties correspond to the standard deviation between the results of MC simulations performed at each temperature to calculate saturation densities and pressures.

$T$ [K]	$p^{\text{sat}}$ [bar]	$u(P)$ [bar]	$\rho_{\text{liq}}$ [kg/m <sup>3</sup> ]	$\rho_{\text{vap}}$ [kg/m <sup>3</sup> ]	$u(\rho_{\text{liq}})$ [kg/m <sup>3</sup> ]	$u(\rho_{\text{vap}})$ [kg/m <sup>3</sup> ]
<b><math>\text{NO}_2</math></b>						
220	13.1	0.29	1087.5	38.7	1.02	2.77
230	17.7	0.4	1043.1	51.9	1.49	3.43
240	24.1	0.43	1001.8	71.8	1.83	3.98
250	31.2	0.53	947.9	94.4	2.54	4.86
260	40.3	0.68	889.3	127	3.42	6.13
270	51.0	0.84	819.4	174	4.83	6.84
275	56.5	0.73	765.8	200	5.91	9.41
280	63.8	0.66	708.9	242.7	7.31	18.53
<b><math>\text{N}_2\text{O}_4</math></b>						
300	0.7	0.04	1462.8	2.7	0.17	5.49
350	4.4	0.11	1346.0	15	0.45	3.7
400	13.6	0.46	1202.2	44.4	1.71	5.11
450	35.9	1.05	1018.8	129.4	6.12	8.57
475	52.8	1.39	848.2	219.8	11.62	30.35



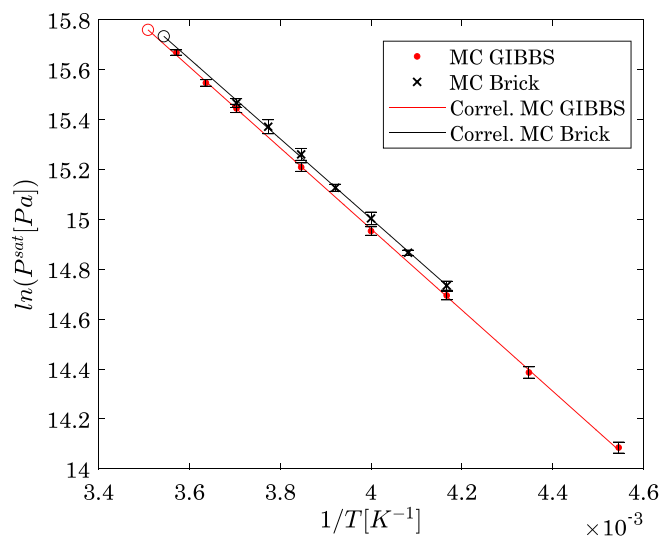
**Fig. 6.** Liquid–vapor coexisting densities of pure NO<sub>2</sub> obtained by MC simulations in this work. Crosses denote the results obtained with Brick-CFCMC as described in section 2.4.2 and reported in Table 3, while points denote the results obtained with GIBBS reported in Table 4. Black symbols represent the critical point predicted as detailed in section 2.4.4, using the two sets of data.



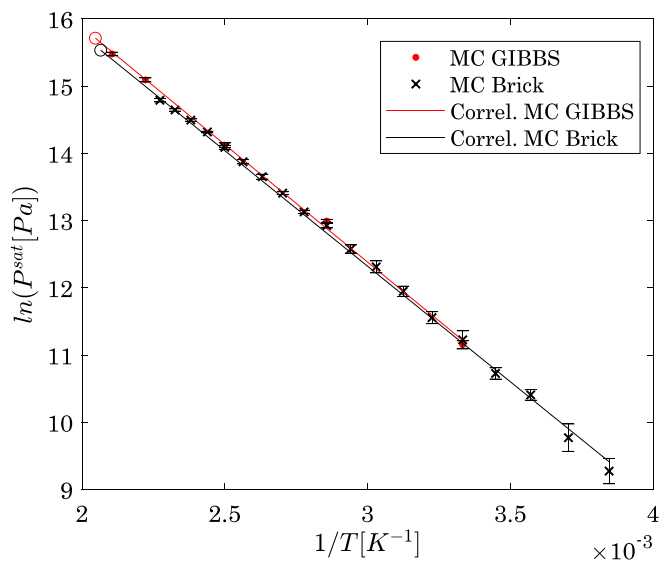
**Fig. 7.** Liquid–vapor coexisting densities of pure N<sub>2</sub>O<sub>4</sub> obtained by MC simulations in this work. Crosses denote the results obtained with Brick-CFCMC as described in section 2.4.2 and reported in Table 3, while points denote the results obtained with GIBBS reported in Table 4. Black symbols represent the critical point predicted as detailed in section 2.4.4, using the two sets of data.

shown in Table S6 of the Supplementary Materials. With those correlations, the critical pressure could then be determined (see section 2.4.4), and this is reported in these figures too.

The critical coordinates and acentric factors calculated as described in section 2.4.4 are reported in Table 5. It can be observed that the values determined in this work are very different with respect to the critical coordinates previously obtained by McCarty et al. [26], also reported in Table 5, who made the assumption of equal acentric factor between the two molecules.



**Fig. 8.** Vapor pressures of pure NO<sub>2</sub> obtained by MC simulations and the resulting correlations. The empty circles represent the critical point predicted as detailed in section 2.4.4, using the set of data obtained in this work.



**Fig. 9.** Vapor pressures of pure N<sub>2</sub>O<sub>4</sub> obtained by MC simulations and the resulting correlation. The empty circles represent the critical point predicted as detailed in section 2.4.4, using the set of data obtained in this work.

**Table 5**

Critical coordinates and acentric factor of NO<sub>2</sub> and N<sub>2</sub>O<sub>4</sub> obtained from the molecular simulation results.

	$T_c$ [K]	$\rho_c$ [kg/m <sup>3</sup> ]	$P_c$ [bar]	$\omega$ [-]
NO <sub>2</sub> / This work, from results of MC Brick	282.2	471.80	68.2	0.0565
N <sub>2</sub> O <sub>4</sub> / This work, from results of MC Brick	484.2	502.44	55.9	0.3212
NO <sub>2</sub> / This work, from results of MC GIBBS	285.0	471.20	69.9	0.0611
N <sub>2</sub> O <sub>4</sub> / This work, from results of MC GIBBS	488.6	524.79	66.7	0.3306
NO <sub>2</sub> / Results from McCarty et al. [26]	239.3	–	103.3	0.01413
N <sub>2</sub> O <sub>4</sub> / Results from McCarty et al. [26]	547.5	–	221.0	0.01413

### 3.2. Thermodynamic properties of $N_2O_4 \rightleftharpoons 2 NO_2$

#### 3.2.1. Monte Carlo results

The thermodynamic properties of the reactive mixture determined by MC simulations with Brick-CFCMC, as detailed in section 2.5, are presented in Table 6 and in Figs. 10–12. Fig. 10 shows that the calculated VLE pressure of the reactive system is in very good agreement with available experimental data and with the correlation provided by DIPPR. The same consideration is valid for the other calculated properties: the composition of the vapour and liquid phase, in Fig. 11, which is compatible with the MC results obtained by Bourasseau et al. [32], and the  $T - \rho_{liq} - \rho_{vap}$  data points reported in Fig. 12, are also in good agreement with the experimental data.

It is worth noting that the  $P$ - $\{x,y\}$  diagram reported in Fig. 11 has two unique features that derive from the mono-variance of this binary reactive system in VLE (see section 2.1): (i) The diagram is a *unique* and *non-isothermal*  $P$ - $\{x,y\}$  diagram for this system; indeed, at each specified pressure (between the triple point pressure and the critical pressure of the reactive system) corresponds a different temperature and different mole fractions in each phase. (ii) The diagram is not closed at the lowest pressure (the triple point pressure of the reactive fluid), because the condition of pure  $N_2O_4$  ( $x_{NO_2} = 0$ ) is not compatible with the occurrence of the chemical reaction, whose extent of reaction is non-zero at those pressure levels.

#### 3.2.2. Thermodynamic calculations

The determination of the ideal gas standard enthalpy of formation (at 298.15 K), standard molar entropy (at 298.15 K) and isobaric heat capacity (as a function of temperature) of  $NO_2$  and of  $N_2O_4$ , by quantum mechanics (see sections 2.4.1 and 3.1.1), as well as their critical point coordinates and acentric factors by force-field based Monte Carlo simulations (see sections 2.4.2, 2.4.4, and 3.1.2) allows the further application of a predictive thermodynamic model to fully characterize the properties of this system: the equation of state presented in section 2.3.

The first computed results are shown in Fig. 13, where the global phase equilibrium diagram (GPED) [76] is represented for this system, and is calculated with two sets of critical coordinates: the solid lines represent the results of the equation of state with the critical coordinates obtained from MC simulations of Brick-CFCMC (see Table 5), also called in the following “EoS 1”, while the dashed lines are results of calculations performed with the critical coordinates obtained from MC data obtained from GIBBS, also called in the following “EoS 2”. Moreover, the GPED shows:

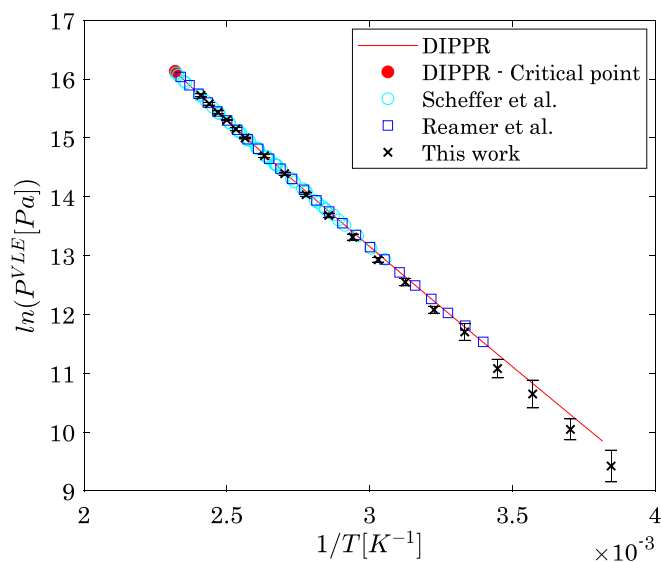


Fig. 10. VLE pressures of the coexisting vapour and liquid phases of the reactive mixture containing  $N_2O_4$  and  $NO_2$ . Crosses are points calculated by MC with Brick-CFCMC. Data of Scheffer and Treub [39] and Reamer and Sage [40] are also shown for comparison.

- the vaporisation curves of the pure  $NO_2$ , ending at their critical point (represented by the circle mark) – pink lines;
- the vaporisation curves of the pure  $N_2O_4$ , ending at their critical point – black lines;
- the locus of critical points of the binary non-reactive mixture formed by  $N_2O_4$  and  $NO_2$  – green lines;
- the VLE pressure of the reactive binary mixture, which is a line instead of a surface because of the mono-variance of this system (see section 2.1), ending at their critical point – blue lines; moreover, the red line and the light blue points on it represent, respectively, the DIPPR correlation and the experimental VLE pressures for the reactive system already shown in Fig. 1. Black crosses are the MC results obtained with Brick-CFCMC (see Table 6 and Fig. 10).
- the triple temperature of the system – the light blue dashed line.

Table 6

Results of MC simulations obtained for reactive  $N_2O_4 \rightleftharpoons 2 NO_2$ , obtained in this work by the use of Brick-CFCMC. “u” denotes the uncertainty of the calculated variables. These uncertainties correspond to the standard deviation between the results of MC simulations performed at each temperature to calculate saturation densities and pressures. Molar fraction uncertainties are determined from the calculated standard deviations of molecules number in the simulation boxes resulting from each simulation, by applying the propagation error law.

$T$ [K]	$P^{sat}$ [bar]	$u(P)$ [bar]	$\rho_{liq}$ [kg/m <sup>3</sup> ]	$\rho_{vap}$ [kg/m <sup>3</sup> ]	$u(\rho_{liq})$ [kg/m <sup>3</sup> ]	$u(\rho_{vap})$ [kg/m <sup>3</sup> ]	$x_{NO_2}$ [-]	$y_{NO_2}$ [-]	$u(x)$ [-]	$u(y)$ [-]
260	0.124	0.033	1537.59	0.47	1.01	0.13	0.000025	0.023	0.000037	0.012
270	0.230	0.041	1515.67	0.85	0.82	0.16	0.000088	0.045	0.000069	0.013
280	0.42	0.10	1493.65	1.43	0.68	0.35	0.00030	0.115	0.00012	0.014
290	0.65	0.10	1471.78	2.11	0.57	0.36	0.00082	0.205	0.00021	0.017
300	1.21	0.17	1448.61	3.77	1.07	0.59	0.00192	0.275	0.00024	0.018
310	1.76	0.10	1424.68	5.19	1.20	0.33	0.00358	0.3483	0.00010	0.0082
320	2.82	0.18	1400.51	7.92	1.06	0.59	0.00557	0.385	0.00018	0.013
330	4.12	0.16	1375.94	11.15	0.77	0.50	0.00820	0.4066	0.00036	0.0067
340	6.06	0.31	1348.55	15.52	0.99	0.96	0.01312	0.4577	0.00045	0.0093
350	8.75	0.33	1320.12	21.71	1.03	1.00	0.01960	0.4875	0.00070	0.0074
360	12.45	0.38	1290.56	30.23	1.14	1.15	0.02793	0.5060	0.00077	0.0032
370	17.81	0.45	1257.53	42.41	1.70	1.44	0.04080	0.5309	0.00170	0.0057
380	24.10	0.70	1219.54	56.36	1.00	2.27	0.05746	0.5573	0.00085	0.0076
390	32.63	0.55	1178.09	76.73	1.90	2.07	0.0784	0.5636	0.0014	0.0046
395	37.95	1.01	1152.09	89.27	2.20	3.68	0.0952	0.5768	0.0025	0.0080
400	44.34	0.24	1128.36	104.85	2.03	0.87	0.1096	0.5834	0.0014	0.0011
405	50.45	1.39	1096.56	121.37	3.27	6.79	0.1295	0.586	0.0038	0.012
410	58.34	1.26	1062.98	141.98	5.36	5.79	0.1511	0.5861	0.0051	0.0085
415	67.35	1.77	1029.43	170.26	3.90	9.75	0.1718	0.580	0.0030	0.012

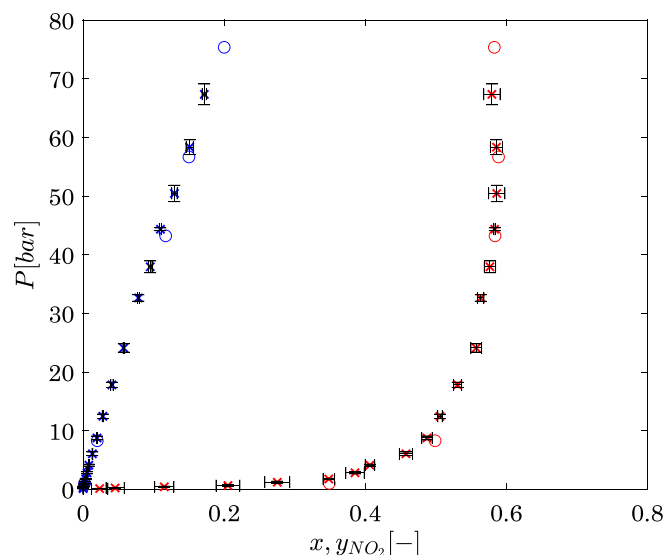


Fig. 11.  $P$ - $\{x,y\}$  diagram of the reactive mixture containing  $N_2O_4$  and  $NO_2$ . Crosses are the points determined with Brick-CFCMC, with the relative uncertainties; circles are points from MC simulations published in Bourasseau et al. [32].

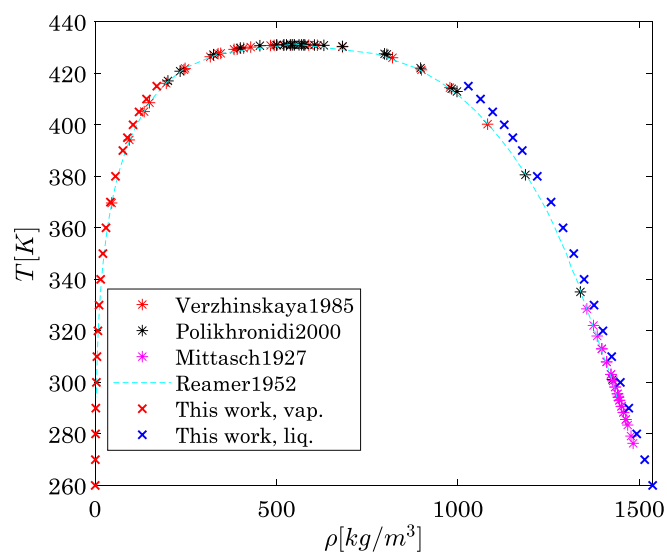


Fig. 12. Vapour and liquid densities of the coexisting phases of the reactive mixture containing  $N_2O_4$  and  $NO_2$ , as a function of temperature. Crosses represent results from Brick-CFCMC while the other are experimental data from the literature [40,71–75].

Considering the fact that not a single mixture parameter has been optimised in the used equation of state for this work and that the model works in purely predictive form, the saturation pressure of the reactive mixture is appropriately represented.

Furthermore, although the quantitative representation of the Monte Carlo results on the  $P$ - $\{x,y\}$  diagram in Fig. 14 is not well reproduced by the equation of state, the qualitative assessment of the phase behaviour of this system by the use of such a non-optimised equation of state is highly satisfactory. As shown in Fig. 15, the modelling of vapour and liquid-phase densities is also acceptable, considering that the representation of the liquid phase density by cubic equations of state -without a translation term [77,78]- is known to be inaccurate.

To conclude, the comparison of the results obtained by the two sets of critical coordinates and acentric factors leads to the observation that the impact of their accuracy on the  $P$ - $\rho$ - $T$ - $\{x,y\}$  is non-negligible and that

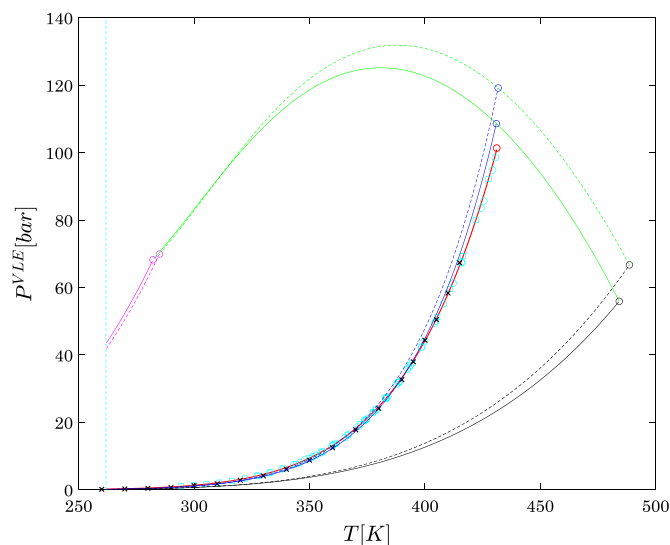


Fig. 13. Global phase equilibrium diagram of the reactive mixture. The legend of this plot is detailed in the main text.

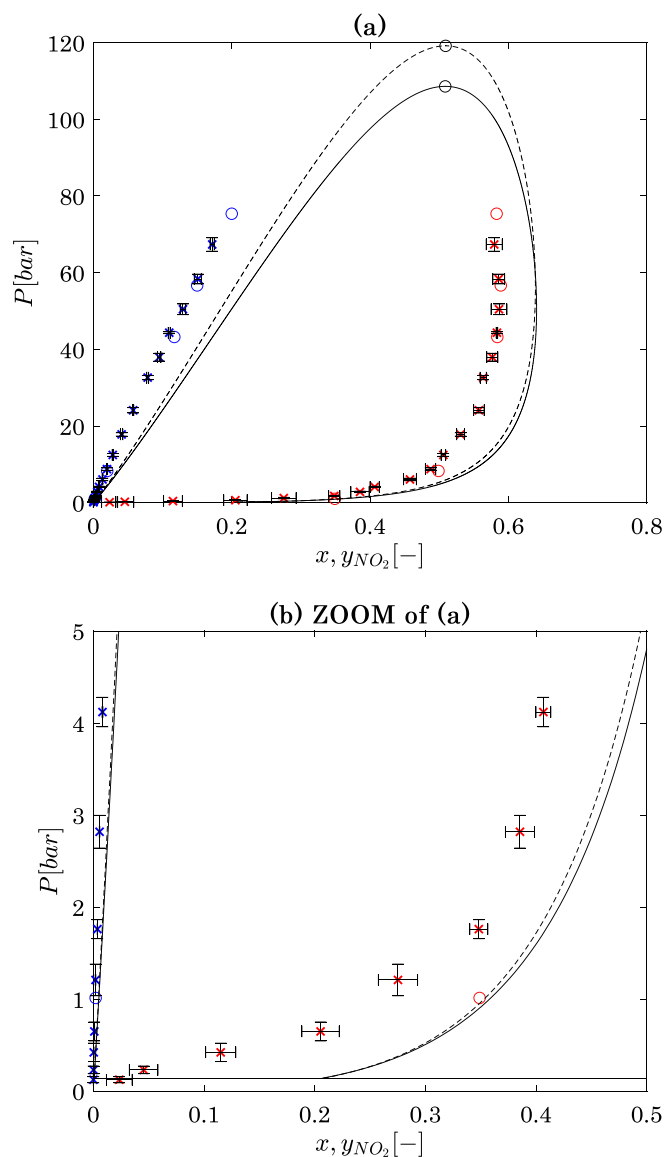
their further optimisation over both pure component and mixture data is suggested. However, it is possible to observe that the impact on derived properties such as entropy (Fig. 16) and enthalpy (Fig. 17) is lower and that the energy and entropy balances will probably be less affected by the uncertainty on the critical coordinates of the pure components forming the mixture.

To conclude, Fig. 18 shows the unique and non-isothermal phase equilibrium diagram of the reactive  $NO_2 + N_2O_4$  system (the black line – also shown in Fig. 14 with the continuous line) and 5 isothermal phase equilibrium diagrams of the binary mixture of  $NO_2 + N_2O_4$  without reaction, calculated at 5 different temperatures (the coloured lines). This plot also shows isobaric lines corresponding to the saturation pressure of the reactive system at the 5 different temperatures at which the isotherms of the inert mixture have been traced. It can be seen that the phase diagram of the reactive system and each of the phase diagrams of the non-reactive system intersect in two points at equal pressure (the relative saturation pressure of the non-reactive isothermal system). Those two points are, respectively, the bubble and the dew point whose compositions are the solution of reactive system under vapour-liquid equilibrium at the considered temperature (and corresponding calculated pressure). For completeness, it is also specified that the equation of state used to generate all these diagrams is the model described in section 2.3, while the critical coordinates are the ones obtained in this work from results of MC Brick-CFCMC and reported in Table 5.

#### 4. Conclusion

This work introduces a methodology enabling the assessment of the VLE and energetic properties of reactive fluids being characterised by one reversible reaction at chemical equilibrium, for example  $N_2O_4 \rightleftharpoons 2NO_2$ . These systems are known to be highly specific because, the reaction reaching instantaneously the chemical equilibrium composition dictated by the system's temperature and pressure, it is never possible to characterise experimentally the pure  $N_2O_4$  and the pure  $NO_2$  at pre-defined conditions. We have initially recalled in this paper some singular thermodynamic behaviours of these systems (such as the uniqueness of its single  $P$ - $T$  curve in VLE condition and thus its unique critical point) and related that to the equal variance of such a binary and mono-reaction system with respect to a mono-component (inert) fluid.

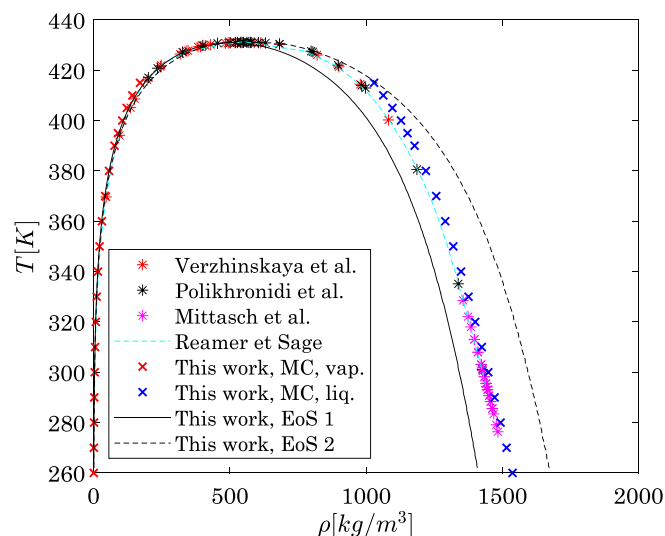
To calculate thermodynamic properties, the Peng-Robinson equation of state associated to the predictive advanced mixing rules  $EoS + a_{res}^{E,\gamma}$ , with a zero- $a_{res}^{E,\gamma}$  term characterising athermal solutions, is applied. The



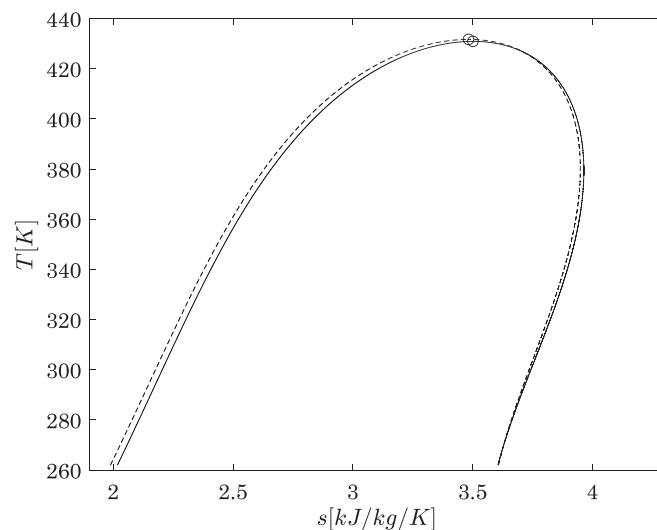
**Fig. 14.**  $P$ - $\{x,y\}$  diagram of the reactive mixture containing  $N_2O_4$  and  $NO_2$ . Fig. (a) represents the entire figure, Fig. (b) represents the ZOOM of Fig. (a). In the figures, crosses are the points determined with Brick-CFCMC, with the relative uncertainties; circles represent points published by Bourasseau et al. [32]; lines represent calculations with the equation of state associated to the two different sets of critical coordinates, solid lines represent EoS 1, while the dashed line represent EoS 2.

required input critical temperature, pressure and acentric factors of the pure  $N_2O_4$  and  $NO_2$ , being their experimental determination impossible, have been optimised in this work from force field-based Monte Carlo results of Gibbs and NPT ensemble simulations, using the force field-based simulation codes Brick-CFCMC and GIBBS. The comparison of the two sets of simulation results obtained with the two codes has proved their high compatibility. Although GIBBS allows performing simulations closer to the critical point than CFC methods, the impact on the prediction of the critical point remains limited.

Moreover, using reaction ensembles, Brick-CFCMC has also enabled the determination of reactive mixture properties, that we have then used to assess the capability of Monte Carlo calculations to reproduce experimental data. Considering the reported uncertainty of MC simulations, this comparison has resulted in a highly satisfactory reproduction of experimental data points. The calculation of energetic properties for this reactive system (enthalpies and entropies) requires the



**Fig. 15.**  $T$ - $\rho^{vap}$ - $\rho^{liq}$  diagram of the reactive mixture containing  $N_2O_4$  and  $NO_2$ . Crosses are the points determined with Brick-CFCMC, with the relative uncertainties; lines represent calculations with the equation of state associated to the two different sets of critical coordinates. The other data points are the same already reported in Fig. 12.



**Fig. 16.**  $T$ - $s$  diagram of the reactive mixture containing  $N_2O_4$  and  $NO_2$ , calculated with the thermodynamic model defined in this work.

calculation of the thermochemical properties of the molecules forming the reactive mixture (ideal gas standard enthalpy of formation, molar standard entropy and heat capacity). Those properties have been determined from ab-initio quantum mechanics simulations.

Furthermore, thermodynamic calculations have been finally performed on the reactive system, with the selected predictive equation of state, and its input  $T_c$ ,  $P_c$  and  $\omega$  of  $NO_2$  and of  $N_2O_4$  optimised on MC results of the two respective systems, with the required  $\Delta_f H_{i,298.15K}^\circ$ ,  $S_{i,298.15K}^\circ$  and the ideal-gas heat capacity temperature-dependent correlation obtained from Quantum Mechanics. The comparison with available  $P$ - $\rho$ - $T$  experimental data of the reactive system in VLE conditions has shown a very good agreement. However, a high sensibility of the accuracy of the equation of state to the critical coordinates used in this work, either obtained from MC simulations performed with Brick-CFCMC or with GIBBS, has been observed. That paves the way to a future investigation, intended to explore the possibility to optimise



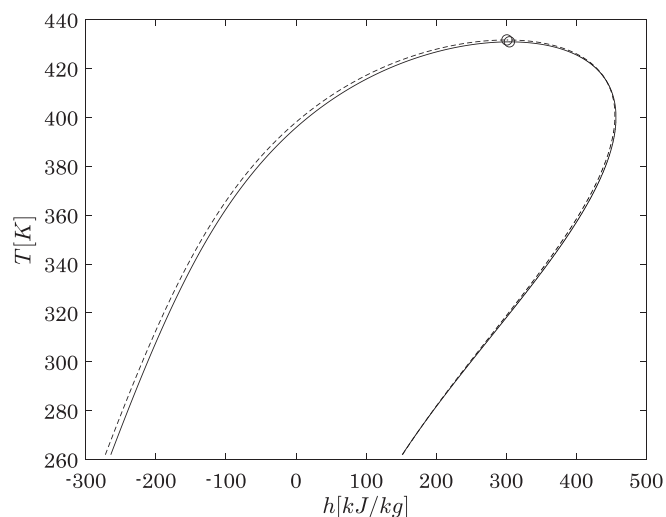


Fig. 17.  $T$ - $h$  diagram of the reactive mixture containing  $\text{N}_2\text{O}_4$  and  $\text{NO}_2$ , calculated with the thermodynamic model defined in this work.

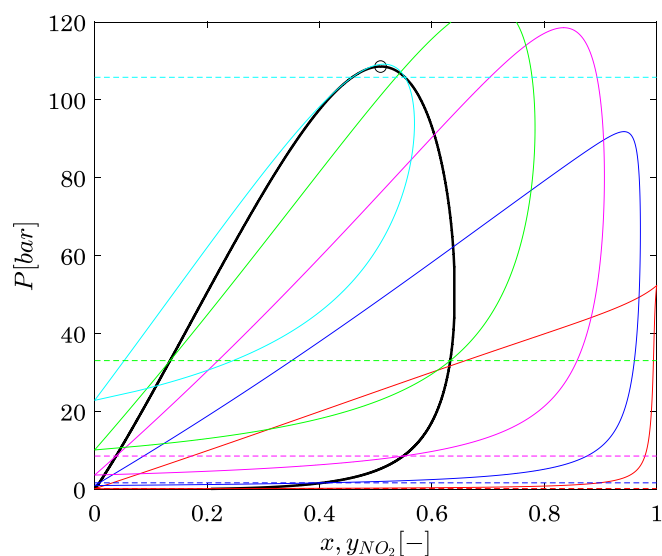


Fig. 18. Phase equilibrium diagrams (solid lines) of the reactive  $\text{NO}_2$ - $\text{N}_2\text{O}_4$  mixture (unique non-isothermal phase equilibrium diagram) - black line; the inert  $\text{NO}_2$ - $\text{N}_2\text{O}_4$  mixture at 270 K (red), 310 K (blue), 350 K (magenta), 390 K (green), 430 K (light blue). Isobars (dashed lines) corresponding to the VLE pressures calculated for the reactive system at the 5 temperatures above considered to build the phase equilibrium diagrams of the inert mixture.

critical coordinates of  $\text{NO}_2$  and  $\text{N}_2\text{O}_4$  on MC of both pure components and reactive mixture data.

To conclude, the presented methodology has proven to be able to accurately determine the chemical equilibrium properties of  $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$ , and is thus proposed to preliminarily predict the thermodynamic properties of other similar reactive systems.

#### CRediT authorship contribution statement

**Silvia Lasala:** Writing – original draft, Visualization, Validation, Supervision, Software, Project administration, Methodology, Funding acquisition, Formal analysis, Conceptualization, Investigation, Data curation. **Konstantin Samukov:** Visualization, Software. **H. Mert Polat:** Software, Supervision. **Véronique Lachet:** Writing – review & editing, Software, Investigation, Data curation. **Olivier Herbinet:**

Writing – review & editing, Methodology, Investigation. **Romain Privat:** Supervision, Software, Conceptualization, Formal analysis. **Jean-Noël Jaubert:** Writing – review & editing, Supervision, Conceptualization, Formal analysis. **Othonas A. Moulτος:** Software. **Kevin De Ras:** Writing – review & editing. **Thijs J. H. Vlugt:** Writing – review & editing, Writing – original draft, Supervision, Software.

#### Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Silvia Lasala reports financial support was provided by European Commission. If there are other authors, they declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

Data will be made available on request.

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#### Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.cej.2024.148961>.

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