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# Integrated process and solvent design for CO, capture using Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD)

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#### Integrated process and solvent design for CO<sub>2</sub> capture using Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD)

#### Proefschrift

ter verkrijging van de graad van doctor aan de Technische Universiteit Delft, op gezag van de Rector Magnificus prof. ir. K.C.A.M. Luyben; voorzitter van het College voor Promoties, in het openbaar te verdedigen op donderdag 06 juli 2017 om 10:00 uur

door

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The work documented in this thesis has been performed within the  $CO_2$  Catch-up R&D programme aimed at demonstrating and optimizing pre-combustion  $CO_2$  capture technology for the energy sector. This programme is executed in a consortium of Vattenfall, the Delft University of Technology and the Energy research Centre of the Netherlands.

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to my mother

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## Summary

The cost of currently available technologies for  $CO_2$  capture should be further reduced to allow for large scale implementation of Carbon Capture and Storage. Solvents for  $CO_2$  capture systems with physical absorption are usually selected based on heuristics, engineering expertise and experimental trials. The performance of the separation system is, however, defined by both the properties of the selected solvent and the process conditions, which should be considered simultaneously. In this thesis, the Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD) framework is extended and applied to the simultaneous optimization of process and solvent for  $CO_2$  capture systems with physical absorption.

In Chapter 2 of the thesis, the CoMT-CAMD framework is applied for a precombustion CO<sub>2</sub> capture system. The problem of simultaneous process and solvent optimization is solved for a reasonably complex process model and for an objective function defining the overall process performance. The solvent is represented as the pure component parameters of the Perturbed Chain Statistical Associating Fluid Theory (PC-SAFT). The optimization is formulated with the pure component parameters of the solvent (PC-SAFT parameters) and with the process variables as degrees of freedom. Preceding studies have shown that process inequality constraints can be problematic for CoMT-CAMD. A constraint for the solvent for example was considered in this chapter. This work proposes a Taylor-expansion of the process constraints in the direction of the parameters of the PC-SAFT model. QSPR models for the prediction of pure component properties (ideal gas heat capacity and molar mass) as function of the PC-SAFT pure component parameters were developed. These models, together with the PC-SAFT equation, enabled predictions of full caloric properties and mass specific process streams inside the CoMT-CAMD framework. Optimal solvents that achieve a minimization of the primary energy consumption in all stages of the capture process were successfully identified.

Chapter 3 presents a method for the prediction of binary interaction parameters  $k_{ij}$  of the PC-SAFT equation of state. The correction required when PC-SAFT is applied to mixtures is linked to the level of asymmetry in the intermolecular potentials of the mixture components. Asymmetry in intermolecular potentials is quantified using relations between the PC-SAFT parameters of the pure components present in the mixture. Estimates of binary interaction parameters  $k_{ij}$  are thus possibly based only on (combinations of) pure component parameters. A QSPR method is employed and estimations of  $k_{ij}$  are obtained independent from experimental mixture data. The method is implemented to mixtures with non-associating and to mixtures with associating components.

Chapter 4 uses and assesses the model for estimating  $k_{ij}$ -values in the CoMT-CAMD framework. Phase equilibria for mixtures of the optimized fluid can be described more accurately. For the assessment of the  $k_{ij}$ -model, the case study of

CoMT-CAMD for polar solvents was examined. For the most promising solvents resulting from the CoMT-CAMD optimization,  $k_{ij}$ -values were individually identified by adjusting to experimental data and the process conditions for these solvents were optimized. That made it possible to compare the results to the CoMT-CAMD calculations with the predictive QSPR-model for  $k_{ij}$ . The comparison shows that CoMT-CAMD with our QSPR-model for  $k_{ij}$  gives good estimates for the results of individually optimized substances. An improvement is found over the model without binary correction ( $k_{ij} = 0$ ).

## Samenvatting

De kosten van de huidige beschikbare technologieën voor de afvang van koolstofdioxide ( $CO_2$ ) moeten verder worden gereduceerd, eerde implementatie van  $CO_2$ afvang en -opslag (Engels, Carbon Capture and Storage) op grote schaalkan worden gerealiseerd. De oplosmiddelen voor  $CO_2$ -afvang systemen door middel van fysische absorptie worden doorgaans geselecteerd op basis van een heuristische methode, technische expertise of experimentele studies. De prestaties vanhet scheidingssysteemworden echter bepaald door zowel de eigenschappen van het gekozen oplosmiddel als de procescondities. Deze dienentegelijkertijd in ogenschouw te worden genomen. In dit proefschrift, wordt de Continuous Molecular Targeting -Computer Aided Molecular Design (CoMT-CAMD) methode uitgebreid en toegepast op de gelijktijdige optimalisatie van het proces en het oplosmiddel voor  $CO_2$ -afvang systemen middels een fysisch oplosmiddel.

In hoofdstuk 2 van het proefschrift wordt de CoMT-CAMD methode aangewend voor een voorverbranding (Engels, pre-combustion) CO<sub>2</sub>-afvang systeem. Het simultaan optimaliseren van het proces en het oplosmiddel is gedaan aan de hand van een tamelijk complex procesmodel en een doelfunctie die de globale procesprestaties definieert. Het oplosmiddel wordt gerepresenteerd door de zuivere component parameters van de geperturbeerde-keten statistische associërende vloeistoftheorie Perturbed Chain Statistical Associating Fluid Theory (PC-SAFT). De optimalisatie wordt opgesteld met de zuivere componenten parameters van het oplosmiddel (PC-SAFT parameters) en de procesvariabelen als vrijheidsgraden. Voorgaande studies hebben aangetoond dat randvoorwaarden in de vorm van ongelijkheden problematisch kunnen zijn voor CoMT-CAMD. In dit hoofdstuk werd bijvoorbeeld een randvoorwaarde voor het oplosmiddel in overweging genomen. Dit werk stelt een Taylor-expansie voor in de vorm van de procesrandvoorwaarden in de richting van de PC-SAFT parameters. QSPR modellen werden ontwikkeld voor het voorspellen van de eigenschappen van dezuivere componenten (warmtecapaciteit van ideaal gas en molaire massa) als functie van de zuivere componenten parameters van PC-SAFT. Deze modellen, samen met de PC-SAFT toestandsvergelijking, maakten het mogelijk om voorspellingen te doen van de volledige calorische eigenschappen en massa specifieke processtromen binnen de CoMT-CAMD methode. De meest optimale oplosmiddelen, die in alle fasen van het afvangproces het primaire energieverbruik minimaliseren, werden op deze manier succesvol geïdentificeerd.

Hoofdstuk 3 presenteert een methode voor het voorspellen van de binaire interactie parameters  $k_{ij}$  van de PC-SAFT toestandsvergelijking. De vereiste correctie, indien PC-SAFT wordt toegepast op mengsels, hangt samen met de mate van asymmetrie in de intermoleculaire potentialen van de mengselcomponenten. De asymmetrie in de intermoleculaire potentialen wordt gekwantificeerd middels verbanden tussen de PC-SAFT parameters van de pure componenten in het mengsel. Schattingen van de binaire interactie parameters  $k_{ij}$  zijn dus mogelijkerwijs alleen gebaseerd op (combinaties van) pure componenten parameters. Een QSPR methode wordt toegepast om  $k_{ij}$  te schatten onafhankelijk van de experimentele data van het mengsel. Deze aanpak wordt geïmplementeerd voor zowel mengsels met niet-associërende als mengsels met associërende componenten.

In hoofdstuk 4 wordt het model toegepast en geëvalueerd voor het schatten van de  $k_{ij}$ -waarden in het CoMT-CAMD kader. Fasenevenwichten van mengsels van het geoptimaliseerde fluïdum kunnenhiermee nauwkeuriger worden beschreven. Voor de beoordeling van het  $k_{ij}$ -model, werd de case study van CoMT-CAMD voor polaire oplosmiddelen onderzocht. Voor de meest veelbelovende oplosmiddelen die uit de CoMT-CAMD optimalisatie voortvloeien, werden individuele  $k_{ij}$ -waarden geïdentificeerddoor ze aan te passen aan de experimentele data. Vervolgens werden de procescondities voor deze oplosmiddelen geoptimaliseerd. Dit maakte het mogelijk om de resultaten van de CoMT-CAMD berekeningen te vergelijken met het voorspellende QSPR-model voor  $k_{ij}$ . De vergelijking toont aan dat CoMT-CAMD met het QSPR-model goede schattingen van  $k_{ij}$  geeft voor de resultaten van de individueel geoptimaliseerde stoffen. Een verbetering is geconstateerd ten opzichte van het model dat geen gebruik maakt van de binaire correctie ( $k_{ij} = 0$ ).

# 

# Introduction

2

Pre-combustion Carbon Capture and Storage (CCS) with physical absorption for CO<sub>2</sub> capture is seen as a cost-competitive low carbon emission concept for power plants. [1, 2] According to public data of the MIT Energy Initiative ('CCS Project Database' [3]): 43% of the power plant CCS projects planned to be operated worldwide consider Integrated Gasification Combined Cycle (IGCC) power plants and employ pre-combustion CO<sub>2</sub> capture with physical absorption. Physical absorption has long since been employed for acid gas removal from industrial gas streams [4-7]. Still, the large-scale implementation of CCS systems requires further reduction in the cost of the currently available technologies for carbon capture. [8] In that light, interrelated environmental and financial performance targets should be considered. In power plants, the performance of the carbon capture system affects directly the production price of electrical power, being crucial to the viability of the entire CCS project. [1, 9–14] Simultaneous process and solvent optimization can lead to lowercost designs for carbon capture systems with physical absorption. The optimization of absorption systems for CO<sub>2</sub> capture has become a vibrant research topic. [8, 15– 181

The Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD) [19] approach enables the simultaneous process and solvent optimization with a single process-driven objective function, utilizing a physically-based thermodynamic model, the Perturbed Chain Statistical Associating Fluid Theory (PC-SAFT) [20–23]. The current thesis proposes extensions to the CoMT-CAMD framework for an overall performance optimization of a pre-combustion CO<sub>2</sub> capture system with physical absorption.

The process topology of the carbon capture system examined in this work resembles in its' key features the pre-combustion capture pilot plant at the IGCC power plant in Buggenum, the Willem Alexander Centrale (WAC). The current work has been part of the test and R&D program of the  $CO_2$  Catch-up project for the demonstration of pre-combustion  $CO_2$  capture at the site of the IGCC pilot plant in Buggenum. The test and R&D program of the  $CO_2$  Catch-up project has been managed by Vattenfall R&D Projects and performed together with Delft University of Technology and Energy research Center of the Netherlands (ECN).

# **1.1.** Solvents for CO<sub>2</sub> capture using physical absorption at IGCC power plants

Physical absorption is a mature technology and appropriate for the pre-combustion capture of  $CO_2$  at IGCC plants. [10, 16, 24–27] A simplified process scheme for an IGCC pre-combustion capture concept is given in Figure 1.1. An example of an acid

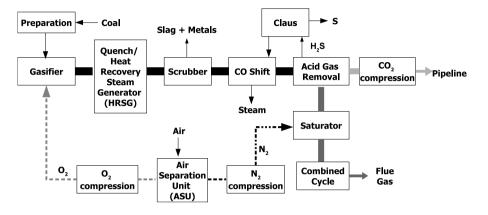


Figure 1.1: Simplified process scheme for an IGCC pre-combustion capture concept (adopted from Kunze and Spliethoff [28]).

gas removal (AGR) process for the pre-combustion capture concept is illustrated in Figure 1.2. The high partial pressure (or better: fugacity) of  $CO_2$  in the shifted syngas stream of an IGCC process allows for high solubility of  $CO_2$  in the solvent (absorption step). The lean solvent can be recovered through pressure reduction in flash drums (desorption step). [29] The desorption step for physical solvents is more energy efficient and cost effective, than the regeneration step of chemical solvents in systems for post-combustion  $CO_2$  capture [15, 30, 31].

The most common industrially applied solvents for the physical absorption of  $CO_2$  are methanol, N-methyl-2-pyrrolidone (NMP), propylene carbonate, 4-formyl-morpholine and mixtures of polyethylene glycols of dimethylethers (DEPEGs). A short review about  $CO_2$  separation processes using these solvents is given in the following.

Methanol is an inexpensive chemical and can achieve sharp separations at high pressures and low absorption temperatures. [33] Methanol is used in the Rectisol process, the earliest commercially applied process for acid gas removal. [4] Due to low operating temperatures, the Rectisol process includes solvent refrigeration steps. This leads to high primary energy consumption and to complex process designs, leading to high operating and investment costs. The Rectisol process was initially implemented in the production of syngas in the chemical industry. [4, 29, 34] For the implementation to CCS systems in IGCC power plants, the original Rectisol process scheme has to be modified. [33] Improved Rectisol-based processes with heat integration have recently been studied by Gatti et al. [34].

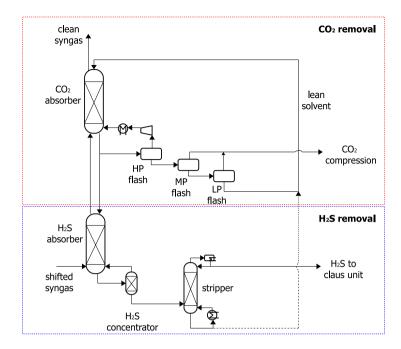


Figure 1.2: Acid gas removal process for the IGCC base case presented in Fig.1.1: Simplified flowsheet of the Selexol process for the removal of  $H_2S$  and  $CO_2$ , as described in ref. [32]. The solvent recovery from the  $CO_2$  capturing step is carried out through pressure reduction in flash drums.

N-methyl-2-pyrrolidone (NMP) is a polar solvent, used in the Purisol process. Due to the higher selectivity of NMP towards  $H_2S$ , the Purisol process has been mainly implemented in natural gas sweetening processes. [4, 29] Additionally, NMP has been studied as a component of hybrid solvents (in mixtures with alkanolamines) for CO<sub>2</sub> capture. [35]

Propylene carbonate, also a polar organic solvent, is used in the Fluor Solvent process. Propylene carbonate has a higher selectivity towards  $CO_2$  than towards light hydrocarbons or  $H_2$ . [4] The Fluor process has been mainly employed in natural gas processing. Recently, propylene carbonate has been studied as solvent for the absorption of  $CO_2$  in a membrane gas absorption process. [36]

4-formylmorpholine, in mixture with N-acetyl-morpholine, is used in the Morphysorb process. The Morphysorb process requires low operating temperatures due to the low boiling point of the solvent. The process has been recently applied and tested for the  $CO_2$  capture for natural gas purification. [37] 4-formylmorpholine has also been studied as solvent in a membrane gas absorption process. [36]

Finally, mixtures of polyethylene glycols of dimethylethers (DEPGs) are used in the Selexol process. The Selexol process has been already implemented for the selective removal of  $H_2S$  from flue gas streams that also contain  $CO_2$ . [4] In order to achieve high purity product streams of  $H_2$ , two Selexol units are usually employed for the sequential removal of  $H_2S$  and  $CO_2$ . Hydrocarbons of high molecular mass

are more soluble in DEPGs than  $CO_2$  and  $H_2S$ . [4] Therefore, the Selexol process is not suitable for acid gas removal from rich hydrocarbon streams. According to a recent study of Kapetaki et al. [38], the implementation of the Selexol process in IGCC power plants may lead to  $CO_2$  capture efficiencies<sup>1</sup> higher than 90%.

The field of research for superior solvents for  $CO_2$  capture with physical absorption is constantly developing. Perfluorinated compounds (PFCs) [39–41] and siloxanes [42, 43] have been studied as promising solvents. Another prominent research field is the design of ionic liquids (IL). [44–49]

Still, for the large-scale implementation of CCS systems a new generation of designs for carbon capture is required . New designs should achieve significant cost reduction for the overall capture process. [31, 50] In this regard, the employed solvents should facilitate high selectivity for absorbing  $CO_2$  against  $H_2$ , while they allow for a minimization of the primary energy consumption in all stages of the capture process. [31]

# **1.2.** Solvent and process optimization with Computer Aided Molecular Design (CAMD)

The selection of physical solvents for  $CO_2$  capture is often based on heuristics: Physical properties of the solvent, like  $CO_2$  solubility,  $CO_2/H_2S$  selectivity, vapor pressure, thermal stability, viscosity, toxicity and corrosivity are evaluated for given process conditions. [39–41] The decision about the appropriate solvent is thus based on engineering expertise, prior knowledge of the process and experimental trials. [51] In industrial practice, the choice of solvents becomes therefore a solvent evaluation procedure rather than a true solvent optimization.

Alternatively, the solvent optimization problem can be addressed as a reverse engineering problem and be solved using Computer Aided Molecular Design (CAMD). [52, 53] The goal of the reverse engineering problem is to identify solvent molecules that meet certain property targets or, more generally, to identify the solvent molecules that achieve optimal performance regarding specified process measures. CAMD provides computational methods and systematic frameworks for the solution of this problem.

#### **1.2.1.** Property models in CAMD

Property models are essential in CAMD for the prediction of pure component parameters<sup>2</sup> and for the prediction of state properties<sup>3</sup> of pure components and mixtures.

<sup>&</sup>lt;sup>1</sup>Carbon capture efficiency =  $\frac{\text{Carbon in } \text{CO}_2 \text{ product}}{\text{Carbon in } \text{coal-Carbon in slag}}$  (according to ref. [38])

<sup>&</sup>lt;sup>2</sup>The term 'pure component parameters' is used here to describe physical properties like molar mass, critical properties, normal boiling and melting points, the standard enthalpy and standard Gibbs energy of formation. [54]

<sup>&</sup>lt;sup>3</sup>Here, the term 'state properties' refers to the thermal, caloric or transport properties of pure components and mixtures (internal energy, enthalpy, entropy, Helmholtz energy and Gibbs energy) and their derivative properties: a) temperature dependent properties (vapor pressure, liquid density, enthalpy of vaporization, ideal gas heat capacity, liquid heat capacity, surface tension and speed of sound) [54], b) transport properties (liquid and vapor viscosity, liquid and vapor thermal conductivity and diffusion coefficients) [54] and c) properties for phase equilibrium calculations (chemical potential, fugacity and

Predicted properties are used to identify the molecules that meet the property targets of the design problem. The accuracy and predictive power of the employed property model(s) define the accuracy and plausibility of the CAMD solution. [55– 58] Therefore, modeling of physical properties plays a critical role in CAMD.

The property models employed in CAMD are mainly Group-Contribution (GC) methods [59–63] or Quantitative Structure Property Relationship (QSPR) models with molecular signature descriptors [64–66].

Strictly speaking, physical properties can be distinguished in pure component parameters and state properties. [54] In the CAMD literature, it is common to speak about 'primary properties' [67], as properties estimated using information only about the molecular structure. 'Primary properties' include pure component parameters and certain temperature dependent state properties at a reference temperature. The GC methods proposed by Joback and Reid [68] have been used in CAMD (e.g. ref. [69, 70]) for the estimation of 'primary properties' of pure components (i.e. the normal boiling and freezing point temperatures, critical properties, the ideal gas heat capacity and the enthalpy of vaporization at boiling point temperature). The GC methods of Joback and Reid are based on first order (UNIFAC) functional groups and were extended by Constantinou and Gani [60]. Constantinou and Gani included second-order functional groups in order to capture the differences between isomers and proximity effects. [71] Further, Marrero and Gani [62] introduced GC methods with third-order functional groups for a better description of complex heterocyclic and large poly-functional acyclic compounds (e.g. ref. [72]). Constantinou et al. [61] developed a GC method for the estimation of acentric factors. GC methods are also available for the prediction of properties that characterize the eco-toxicity of pure components. [73–75]

State properties are calculated from estimated values of 'primary properties', using basic thermodynamic relations or empirical correlations. [71, 76–78] For state properties, some works (e.g. ref. [56, 79]) use the theorem of corresponding states with GC predictions for the acentric factor and the critical properties. For phase equilibrium calculations  $g^{E}$ -models (usually UNIFAC) are often used or, less often, cubic equations of state (e.g. ref. [80, 81]).

Methods that use topological indices (TI) as descriptors in QSPR models are employed for the prediction of both pure component parameters and state properties. Topological indices are a particular category of molecular signature descriptors, which are derived from molecular graphs. According to Faulon et al. [82]: "The (molecular) signature is a systematic codification system over an alphabet of atom types, describing the extended valence (i.e. neighborhood) of the atoms of a molecule." Topological indices based on molecular signature take into account the molecular architecture and serve as suitable descriptors for a QSPR model for property prediction. [64] Raman and Maranas [64] implemented such QSPR models for the prediction of the boiling point temperature and the critical properties and for the prediction of the molar volume, the enthalpy of vaporization, the molar refractivity and the surface tension at a given temperature. Chemmangattuvalappil and Eden [65] used QSPR models with topological indices for the prediction of the molar

fugacity coefficients, activity and activity coefficients) [54].

volume [83] and the toxic limit concentration [84], while Patel et al. [66] proposed a QSPR model with topological indices for the prediction of flash point in CAMD. A thorough review on the QSPR methods using topological indices in CAMD can be found in the work of Harini et al. [57].

A combination of QSPR models with topological indices and GC methods, the GC<sup>+</sup> method [67], has been also implemented in CAMD. The GC<sup>+</sup> method improves property predictions for complex molecules and is implemented in a way similar to the original GC methods. For example, Samudra and Sahinidis [76] used GC<sup>+</sup> for the prediction of 'primary properties' and external property models for the calculation of heat conductivities and the volumetric heat capacity. In the work of Conte et al. [85] the GC<sup>+</sup> method was used for the prediction of surface tension and viscosity. Gonzalez et al. [86] used GC<sup>+</sup> to predict properties relevant to phase equilibrium calculations. Based on the GC<sup>+</sup> method, Hukkerikar et al. [87] proposed estimation methods for environment-related properties.

O'Connell et al. [56] classified the property models in CAMD according to the way these models are obtained and the level of empiricism they implicate (Figure 1.3). GC and QSPR models use information about the molecular structure in a sys-

Empiricism	Enlightened Empiricism	Theory →
Polynomial & other simplified formulations	Rational relations with regressed parameters based in fundamentals	Direct use of <i>ab initio</i> quantum & statistical mechanics

Figure 1.3: Iterative steps of property model development (adopted from O'Connell et al. [56]).

tematic way. Still, they are correlations with parameters adjusted to experimental data. As stated by Raman and Maranas [64], the QSPR models used in CAMD "do not necessarily have a casual relationship with the correlated property". In complex CAMD problems, depending on the required properties, the combination of different (GC or QSPR) models may be necessary as well. In that case, the model assumptions, the validity range of the employed models and combined uncertainties should be carefully examined. A recent review on the advantages and limitations of the various fluid property models used in CAMD is given by van Speybroeck et al. [88].

Physically-based thermodynamic models have been recently introduced in CAMD frameworks. Physically-based thermodynamic models (for example, SAFT-type models [89]) originate in statistical mechanics and have a theoretical background (right end of the scale in Figure 1.3) but also parameters. Due to the physical background of their molecular parameters, SAFT-type models give a sharp representation of the optimized molecule inside CAMD frameworks. SAFT-type models can be better extrapolated and therefore can provide safer predictions for state properties than (other) GC methods and QSPR models. With a SAFT-type equation of state (EoS) residual static state properties can be derived directly from the residual Helmholtz energy. Adjiman et al. [90] illustrate the expanding potential of the implementation

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of SAFT-type models in CAMD. A more detailed discussion about the key-role of the PC-SAFT [20–23] model as a unified framework for property prediction in CAMD is given in Sections 1.2.4 and 1.3.1 of the current thesis.

#### **1.2.2.** The integrated solvent and process optimization problem

Solvent optimization problems are particularly demanding due to the strong correlations between the optimal properties of the solvent and the optimal process conditions. In order to achieve an optimal performance for the  $CO_2$  capture process, the solvent design problem should thus not be decoupled and solved separately from the process design. [19, 52, 90] The solvent and the process conditions have to be optimized simultaneously. An integrated process and molecular design approach is essential.

The fully integrated process and solvent design problem is in its original formulation a mixed integer non-linear optimization program (MINLP) [53]:

$$\min_{\overline{x},\overline{p}} f(\overline{x},\overline{p})$$
s.t.  $h(\overline{x},\overline{p}) = 0$ 
 $g(\overline{x},\overline{p}) \le 0$ 
(1.1)

where  $\overline{x}$  denotes the vector of process variables defined in  $\mathbb{R}^m$  and  $\overline{p} = [p_1, ..., p_D]$  denotes the vector of molecular parameters of the optimized solvent. The molecular parameters  $p_i$  are parameters required by the employed property model: the functional groups of a GC property model, the descriptors of a QSPR model or the molecular parameters of a physically-based (SAFT-type) thermodynamic model. The vector of molecular parameters  $\overline{p}$  is unique for each real substance and is defined over a discrete vector space,  $P^{D\times N}$ , where D is the number of molecular parameters  $p_i$  and N is the number of all real substances. The non-linear objective function  $f(\overline{x}, \overline{p})$  is a representative measure of the overall process performance. The non-linear constraints of the problem  $h(\overline{x}, \overline{p})$  and  $g(\overline{x}, \overline{p})$  represent the equations of the property model and the constraints on  $\overline{x}$  and  $\overline{p}$ .

The non-linear objective function  $f(\overline{x}, \overline{p})$ , the non-linear property models in  $h(\overline{x}, \overline{p})$  and the high dimensionality of the discrete vector space  $P^{D \times N}$  lead to a mixed-integer non-linear program of prohibitive size for rigorous and large process models. Therefore, a solution of problem (1.1) is attainable only through problem relaxation. CAMD methods can be distinguished according to the relaxation strategy they employ in order to handle problem (1.1).

**1.2.3.** CAMD methods for solvent selection and solvent design In solvent design, most CAMD approaches treat the process and the molecular design problems separately. Some approaches start with a pre-selection of suitable candidate species (e.g. ref. [91] and [92]). In a subsequent step, the process is optimized individually for each candidate solvent, in order to identify the best

### **1.2.** Solvent and process optimization with Computer Aided Molecular Design (CAMD)

performing solvent. In other CAMD approaches [59, 60, 62, 93] the property targets and the property constraints are defined for given process conditions. The molecular structures that meet the thus defined property targets and constraints are identified through database screening. The considered property databases include either already existing components or molecular structures generated using a GC method [53]. In order to avoid the mixed-integer formulation of the molecular design problem, these approaches decouple the solution of the process design from the solution of the molecular design problem. All aforementioned CAMD approaches involve heuristic decisions, either in the step of pre-selection or by the definition of property targets. The joint search space of the optimal solution of problem (1.1) is then decomposed, leading inevitably to loss of information and sub-optimal solutions.

Eden et al. [52] introduced the concept of property integration in a CAMD approach for the simultaneous optimization of separation processes and solvents. Property integration allows for process-specific property targets and establishes an indirect link between the two sub-problems of process and molecular design. [19] A description of the approach proposed by Eden et al. [52] is given in Figure 1.4. CAMD approaches based on the concept of property integration preserve the mixed-

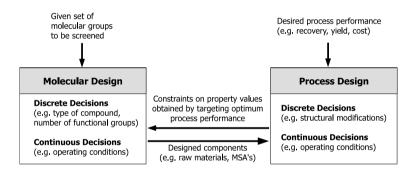


Figure 1.4: Reverse problem formulation with property integration for simultaneous separation process and product design (adopted from Eden et al. [52]).

integer formulation of the molecular design problem in (1.1). Still, the solution of the MINLP in (1.1) requires a problem relaxation. Problem (1.1) is therefore further relaxed, in order either to handle the non-linearity of the process design problem, or in order to reduce the dimension of the discrete molecular search space. Auxiliary objective functions (e.g. ref. [94]) or simplified process and property models (e.g. ref. [52]) are implemented to relax the high non-linearity in  $f(\bar{x}, \bar{p})$ ,  $h(\bar{x}, \bar{p})$  and  $g(\bar{x}, \bar{p})$ . A reduction of the discrete molecular search space through pre-selection of certain candidate species (molecules or the functional groups of a GC model, e.g. ref. [95]). Finally, many approaches turn to advanced algorithmic techniques for the solution of the modified MI(N)LP. A detailed discussion on these approaches is given in Chapter 2.

Consider, however, the level of complexity in industrial separation processes,

like the process of capturing  $CO_2$  for a CCS application. The implementation of simplified process models and auxiliary objective functions may neglect important interactions between the various process steps. Thereby, critical aspects of the full process performance will be missed, which may lead to fallacious property targets and consequently to sub-optimal or even erroneous solutions for the molecular design problem. Moreover, by implementing an *a-priori* reduction of the molecular search space, superior solvents may be omitted.

# **1.2.4.** The Continuous Molecular Targeting (CoMT) - CAMD method

Continuous Molecular Targeting (CoMT), established by Bardow et al. [19], is an alternative CAMD method for the solution of the integrated solvent and molecular optimization problem (1.1). CoMT-CAMD circumvents the mixed-integer formulation of the molecular optimization problem in problem (1.1). The discrete molecular search space of the thermodynamic model representing real molecules  $P^{D\times N}$  is regarded as a continuous molecular search space of real and hypothetical molecules  $\mathbb{R}^N$ . The molecular and process optimization variables are all defined in the continuous domain  $\mathbb{R}^{m+N}$  and they can be optimized simultaneously. Problem (1.1) is thereby formulated as a non-linear program (NLP) and it can be solved using gradient based optimization algorithms. CoMT is empowered by the use of a physically-based thermodynamic model. In this work, the CoMT-CAMD approach is implemented with the Perturbed Chain - Statistical Associating Fluid Theory (PC-SAFT) model [20–23]. The PC-SAFT molecular parameters are used as variables for the molecular optimization.

Process and molecular optimization take place simultaneously using a single, well-defined objective function for the process (like annual costs or primary energy consumption). Individual property targets and auxiliary objective functions are not required. A single, process-based objective function simultaneously evaluates the impact of changes in the molecular structure of the solvent and of the process conditions to the overall process performance. Additionally, the transformation of problem (1.1) to a non-linear program (NLP) allows for rigorously considering (reasonably complex) process models.

The optimal solution obtained in the CoMT step is the vector of the PC-SAFT molecular parameters of the optimal, hypothetical, molecule and the corresponding optimal process conditions. The molecular design is completed by identifying the real components (or more generally the feasible molecular structures), which give the best achievable performance, closest to the optimal one. The efficiency of the molecular design step in CoMT-CAMD is founded on the strong physical background of the PC-SAFT molecular parameters: In PC-SAFT, similar molecular parameters correspond to similar thermodynamic properties. The performance of real components is estimated by an approximation of the objective function around the optimum of the CoMT step. The objective function is approximated using a Taylor series of 2<sup>nd</sup> order as function of the molecular parameters. The best performing real molecules are expected to lie close to the local optimum of problem (1.1) in the joint search space of process variables and molecular parameters. The set of real

components that are considered during the step of molecular design are either existing components with known molecular parameters (database mapping) [96, 97] or molecular structures generated using a GC method for the PC-SAFT parameters like GPC-SAFT [98] (feasible structure mapping [99]). In the case that molecular structures are generated using a GC method, a molecular design algorithm with feasibility constraints has to be implemented. [99] The generic procedure of CoMT-CAMD is illustrated in Figure 1.5.

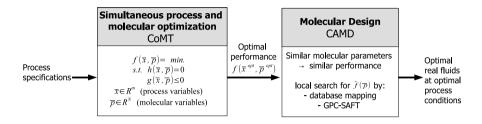


Figure 1.5: Continuous Molecular Targeting - Computer Aided Molecular Design for integrated process and fluid optimization.

#### **1.3.** The Perturbed Chain - SAFT (PC-SAFT) thermodynamic model

# **1.3.1.** A unified framework for the calculation of physical properties in CAMD

The PC-SAFT equation of state (EoS) [20–23] formulates the residual Helmholtz energy. Any other residual (static) state property can be derived from the residual Helmholtz energy. For the calculation of full caloric properties, an ideal gas contribution is additionally required. In process simulation problems, the ideal gas heat capacity  $c_p^{\rm ig}$  can be obtained directly from property databases, since the system components are known. During the Continuous Molecular Targeting, values of  $c_p^{\rm ig}$  for the optimized (hypothetical) molecule are not available in databases. Further, the molecular mass of the optimized fluid is required in process calculations that include mass-specific process streams. The QSPR models developed in the course of the current thesis for the estimation of  $c_p^{\rm ig}$  and the molecular mass of pure substances as function of the PC-SAFT pure component parameters are given in Chapter 2.

Beyond the calculation of caloric properties, the PC-SAFT model can be utilized for the prediction of several static and dynamic state properties: Surface tension for pure components and mixtures can be predicted with PC-SAFT in the framework of density functional theory (DFT). [100-102] Viscosity of pure fluids and fluid mixtures can be predicted using Rosenfeld's entropy-scaling [103, 104] and a GC method for the PC-SAFT parameters. [105] On-going work focuses on the development of models for the prediction of thermal conductivity [106, 107] and

#### self-diffusion coefficients.

The implementation of PC-SAFT EoS to mixtures often demands the adjustment of a binary interaction parameter,  $k_{ij}$ , to experimental data of phase equilibria. Since experimental mixture data are not accessible during molecular design,  $k_{ij}$  needs to be predicted from pure component parameters. This thesis shows that the binary interaction parameter  $k_{ij}$  can be predicted from the pure component PC-SAFT parameters using a QSPR model (Chapter 3).

The PC-SAFT EoS originates in statistical mechanics and accounts explicitly for polar and associating intermolecular interactions. [20, 21] PC-SAFT provides good predictions of pure component and mixture properties and gives better predictions in phase equilibrium calculations for complex and high pressure systems than cubic EoS or g<sup>E</sup>-models. [108, 109] Due to the theoretical background of the model parameters, PC-SAFT links thermodynamic properties of pure fluids to molecular structure. Further, full static and dynamic state properties required in process systems' calculations can be derived from residual properties. Thereby, PC-SAFT serves as a unified framework for the calculation of thermodynamic properties in the CoMT-CAMD framework.

#### **1.3.2.** The PC-SAFT equation of state

The PC-SAFT EoS belongs to the SAFT family of equations of state. SAFT-type EoS are algebraic approximations of the residual Helmholtz energy. SAFT-type EoS are based on statistical mechanics and more specifically on Wertheim's thermodynamic perturbation theory of first-order (TPT1) [110, 111]. Perturbation theories provide models for fluid properties based on intermolecular potentials. [112, 113] A reference fluid is considered in order to describe fluid behavior resulting from repulsive intermolecular forces. Attractive intermolecular forces are treated as perturbation to the behavior of the reference fluid. Molecular distribution functions characterizing the repulsive part of the intermolecular potential are used. In the thermodynamic perturbation theory (TPT) of Wertheim the residual Helmholtz energy is expanded in a series of integrals of molecular distribution functions for the reference fluid and the association potential. [112] Chapman et al. [114] applied Wertheim's theory to mixtures and derived the Statistical Associating Fluid Theory (SAFT) EoS. In their work, Chapman et al. [114] use a reference fluid of homonuclear hard-sphere chains. The contribution to the residual Helmholtz energy due to association is derived from Wertheim's perturbation theory of first order (TPT1). In the same work [114], the effects due to dispersive forces and induction are accounted through a mean field perturbation term [112].

PC-SAFT [20–23] also utilizes the reference fluid of hard-sphere chains. Gross and Sadowski [20] applied the perturbation theory of Barker and Henderson [115] to chain molecules, to calculate the contribution to the residual Helmholtz energy due to dispersive forces. The contribution due to associating interactions is applied in a similar way as in the work of Chapman et al. [112] and Huang and Radosz [116]. The contribution of quadrupole-quadrupole, dipole-dipole and dipole-quadrupole interactions to the residual Helmholtz energy are accounted for, as described in the work of Gross [22], Gross and Vrabec [23] and Vrabec and Gross [117] respectively.

PC-SAFT is implemented to mixtures using the one-fluid (van der Waals) mixing rules.

In the PC-SAFT model, the molecules are represented as chains of spherical segments. Each pure substance is identified by a vector of molecular parameters characterizing the shape of the chain and the dispersive, associating and polar intermolecular potentials. Non-polar and non-associating molecules are characterized by the number of segments per chain molecule *m* (segment number), the segment diameter  $\sigma$  and the dispersive energy parameter  $\varepsilon/k$ . Associating molecules need two additional parameters, the association energy parameter  $\varepsilon^{AB}/k$  and the association volume  $\kappa^{AB}$ . Polar molecules require the dipole moment  $\mu$  and the quadrupole moment Q as parameters.

The equations of the PC-SAFT model, that are required for calculation of thermophysical properties in the present work, are given in the following.

#### Helmholtz Energy

The following equations are summarized in form of the residual Helmholtz energy related to the number of chain molecules N and their kinetic energy kT as

$$\tilde{a} = \frac{A}{NkT} \tag{1.2}$$

where k is the Boltzmann constant and T the temperature. The reduced Helmholtz energy of a real fluid is therefore written as

$$\tilde{a} = \tilde{a}^{\rm ig} + \tilde{a}^{\rm res} \tag{1.3}$$

The reduced Helmholtz energy for a mixture in the ideal gas state is given as

$$\tilde{a}^{ig} = \sum_{i} x_i \left[ \ln \left( \Lambda^3 \cdot \rho_i \right) - 1 \right] = \frac{1}{\rho} \cdot \sum_{i} \rho_i \left[ \ln \left( \Lambda^3 \cdot \rho_i \right) - 1 \right]$$
(1.4)

where  $\Lambda$  is the de Broglie wavelength,  $x_i$  is the mole fraction of species *i* in the mixture,  $\rho_i$  the molecular density of species *i* and  $\rho$  the density of the mixture. The residual term of the Helmholtz energy is calculated with PC-SAFT. The reduced residual Helmholtz energy  $\tilde{a}^{\text{res}}$  is expressed as a sum of terms due to the hard-chain reference contribution  $\tilde{a}^{\text{hc}}$  and the terms expressing the contribution due to attractive interactions: the dispersive  $\tilde{a}^{\text{disp}}$ , associating  $\tilde{a}^{\text{assoc}}$ , quadrupolar  $\tilde{a}^{\text{qq}}$  and dipolar  $\tilde{a}^{\text{dd}}$  contribution terms, according to

$$\tilde{a}^{res} = \tilde{a}^{hc} + \tilde{a}^{disp} + \tilde{a}^{assoc} + \tilde{a}^{qq} + \tilde{a}^{dd}$$
(1.5)

The equations for the calculation of the various contributions to the residual Helmholtz energy are adopted from ref. [20-23, 112] and they are given in Appendix A.1.

Derived thermodynamic properties from the Helmholtz energy

**Compressibility factor.** The compressibility factor *Z* is written as:

$$Z = Z^{ig} + Z^{hc} + Z^{disp} + Z^{assoc} + Z^{qq} + Z^{dd} = 1 + \eta \left(\frac{\partial \tilde{a}^{res}}{\partial \eta}\right)_{T,\overline{x}}.$$
 (1.6)

where  $\eta$  is the packing fraction defined in Appendix A.1. The equations for the calculation of the various contributions to the compressibility are given in ref. [20–23, 112].

**Pressure.** The total pressure *P* of the system can be calculated as:

$$P = ZkT\rho \tag{1.7}$$

using the compressibility factor Z given in Eq. (1.6).

**Chemical potential,**  $\mu_i$ . The chemical potential  $\mu_i$  of species *i* is the partial derivative of the Helmholtz energy *A* to the mole number  $n_i$  for constant temperature *T* and volume *V*:

$$\mu_i(T, V, \overline{n}) = \left(\frac{\partial A}{\partial n_i}\right)_{T, V, n_j \neq i}.$$
(1.8)

For the chemical potential  $\mu_i$  of species *i* Eq.(1.8) leads to the following formulation:

$$\frac{\mu_i(T,\overline{\rho})}{kT} = \left(\frac{\partial \left(\tilde{a} \cdot \rho\right)}{\partial \rho_i}\right)_{T,\rho_i \neq i}$$
(1.9)

where  $\overline{\rho}$  is the vector of component molar densities  $\rho_i = x_i \cdot \rho$  of all species *i* of the system. For the full chemical potential of a species *i* holds

$$\frac{\mu_i}{kT} = \frac{\mu_i^{\rm 1g}}{kT} + \frac{\mu_i^{\rm res}}{kT}.$$
 (1.10)

From Eq.(1.4) and Eq.(1.8), for  $\Lambda^3 = 1$ , the chemical potential of species *i* in the ideal gas state is calculated by

$$\frac{\mu_i^{\text{ig}}}{kT} = \ln(\Lambda^3 \cdot \rho_i) = \ln(\rho_i).$$
(1.11)

The residual chemical potential  $\mu_i^{\rm res}$  of species i is calculated with the PC-SAFT EoS according to

$$\frac{\mu_i^{\text{res}}}{kT} = \rho \cdot \left(\frac{\partial \tilde{a}^{\text{res}}}{\partial \rho_i}\right)_{T,\rho_j \neq i} + \tilde{a}^{\text{res}}.$$
(1.12)

**Fugacity coefficient**  $\ln \phi_i$ . The fugacity coefficient of species *i* is expressed as function of the temperature *T* and the pressure *P* as

$$\ln \phi_i(T, P, \overline{x}) = \frac{\mu_i^{\text{res}}(T, P, \overline{x})}{kT} = \frac{\mu_i^{\text{res}}(T, \overline{\rho})}{kT} - \ln Z.$$
(1.13)

**Residual molar entropy,**  $\hat{s}^{\text{res}}$ . In the following, molar thermodynamic properties  $\hat{w}$  are related to the dimensionless properties as

$$\frac{\hat{w}}{RT} = \tilde{w} = \frac{W}{NkT}.$$
(1.14)

From the Maxwell relations the entropy *S* is given as the partial derivative of the Helmholtz energy *A* over the temperature *T* for constant volume *V* and constant composition  $\overline{x}$  of the mixture

$$\left(\frac{\partial A}{\partial T}\right)_{V,\overline{x}} = -S. \tag{1.15}$$

Eq.(1.15) can be reformulated on the reduced Helmholtz energy  $\tilde{a}$  as

$$\left(\frac{\partial (A/Nk)}{\partial T}\right)_{\overline{\rho}} = -\frac{S}{Nk} \quad \text{which gives} \quad \left(\frac{\partial (\tilde{a} \cdot T)}{\partial T}\right)_{\overline{\rho}} = -\frac{\hat{s}}{R}. \tag{1.16}$$

The residual molar entropy of a mixture of molar volume v is given by

$$\frac{\hat{s}^{\text{res}}(v,T,\bar{x})}{R} = \frac{\hat{s}^{\text{res}}(T,\bar{\rho})}{R} = -T \cdot \left(\frac{\partial \tilde{a}^{\text{res}}}{\partial T}\right)_{\bar{\rho}} - \tilde{a}^{\text{res}} =$$
$$= -T \cdot \left[\left(\frac{\partial \tilde{a}^{\text{res}}}{\partial T}\right)_{\bar{\rho}} + \frac{\tilde{a}^{\text{res}}}{T}\right]$$
(1.17)

and

$$\frac{\hat{s}^{\text{res}}(P,T,\overline{x})}{R} = \frac{\hat{s}^{\text{res}}(T,\overline{\rho})}{R} + \ln Z.$$
(1.18)

**Molar enthalpy**,  $\hat{h}$ . The molar enthalpy of the mixture  $\hat{h}$  is given as the summation of the ideal gas term  $\hat{h}^{ig}$  and the residual term  $\hat{h}^{res}$ :

$$\hat{h} = \hat{h}^{\text{ig}} + \hat{h}^{\text{res}}.$$
(1.19)

The enthalpy of the mixture in the ideal gas state, for a reference temperature  $T^{o}$ , is given according to classical thermodynamics by

$$\hat{h}^{ig}(T,\overline{x}) = \sum_{i} x_i \hat{h}_i^{ig}(T)$$
(1.20)

with 
$$\hat{h}_{i}^{ig}(T) - \hat{h}_{i}^{ig}(T^{o}) = \int_{T^{o}}^{T} \hat{c}_{p,i}^{ig} dT.$$
 (1.21)

The residual molar enthalpy  $\hat{h}^{\text{res}}$  is calculated from the reduced residual Helmholtz energy and the compressibility factor. The relation between the enthalpy *H* and the Helmholtz energy *A* written for residual properties is

$$H^{\rm res} = A^{\rm res} - TS^{\rm res} + (PV)^{\rm res} = A^{\rm res} - TS^{\rm res} + \left[ PV - (PV)^{\rm ig} \right].$$
(1.22)

Eq.(1.7) and (1.22) result to the following expressions for the residual molar enthalpy:

$$\frac{\hat{h}^{\text{res}}}{RT} = \frac{H^{\text{res}}}{NkT} = \tilde{a}^{\text{res}} - \frac{\hat{s}^{\text{res}}}{R} + (Z-1)$$
(1.23)

and

$$\frac{\hat{h}^{\text{res}}}{RT} = -T \cdot \left(\frac{\partial \tilde{a}^{\text{res}}}{\partial T}\right)_{\overline{\rho}} + (Z-1).$$
(1.24)

#### Phase equilibrium calculations

For a system with K components and M phases in equilibrium, the equilibrium conditions write:

$$T^{\mathrm{I}} = T^{\mathrm{II}} = \dots = T^{\mathrm{M}} \tag{1.25}$$

$$P^{\mathrm{I}} = P^{\mathrm{II}} = \dots = P^{\mathrm{M}} \tag{1.26}$$

$$\mu_i^{\mathrm{I}} = \mu_i^{\mathrm{II}} = \dots = \mu_i^{\mathrm{M}} \quad \forall i.$$
(1.27)

The chemical potential  $\mu_i$  may be expressed by the fugacity  $f_i$ . [54] For a reference pressure  $P^o$ 

$$\mu_i(T, P, \bar{x}) = \mu_i^{\text{ig,pure}}(T, P^o) + RT \ln \frac{f_i(T, P, x)}{P^o}.$$
 (1.28)

Then, the equilibrium condition in Eq.(1.27) can be expressed by means of fugacity as

$$f_i^{\mathrm{I}} = f_i^{\mathrm{II}} = \dots = f_i^{\mathrm{M}} \quad \forall i.$$
(1.29)

Using the definition of the fugacity coefficient  $\phi_i$  of species *i* [118]

$$\phi_i = \frac{f_i}{x_i P} \tag{1.30}$$

the isofugacity relations in Eq.(1.29) can be written as

$$x_{i}^{\mathrm{I}}\phi_{i}(T,P,x_{i}^{\mathrm{I}}) = x_{i}^{\mathrm{II}}\phi_{i}(T,P,x_{i}^{\mathrm{II}}) = \dots = x_{i}^{\mathrm{M}}\phi_{i}(T,P,x_{i}^{\mathrm{M}}) \quad \forall i.$$
(1.31)

In phase equilibrium calculations the equations (1.31) are solved iteratively using the PC-SAFT EoS for the calculation of the fugacity coefficients (Eq.(1.12) and (1.13)).

The application of PC-SAFT to highly asymmetric mixtures (mixtures of components with considerably different intermolecular potentials) requires the adjustment of a binary correction parameter  $k_{ij}$  to experimental mixture data.

Figure 1.6 shows results of phase equilibrium calculations with PC-SAFT for the binary systems  $CO_2$  - acetophenone and  $H_2$  - cyclohexane. In both examples, we observe a good description of the vapor phase. An accurate description of the liquid phase is obtained when the model is corrected with  $k_{ij}$  adjusted to experimental mixture data. However, experimental data are not available for mixtures considered during molecular design. A method for the estimation of  $k_{ij}$  as a function of the PC-SAFT pure component parameters is proposed and implemented with CoMT-CAMD in the current thesis.

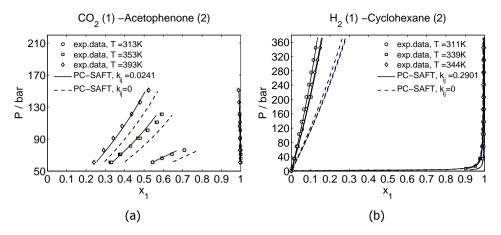


Figure 1.6: Results of vapor-liquid equilibrium calculations with PC-SAFT for asymmetric binary systems: a)  $CO_2$  - acetophenone [119] and b) H<sub>2</sub> - cyclohexane [120, 121]. Phase equilibrium calculations are compared to isothermal (P-xy) experimental data. Solid lines denote phase equilibrium calculations with binary interaction parameter  $k_{ij}$  adjusted on the experimental data and dashed lines are for  $k_{ij} = 0$ .

#### **1.4.** Outline of the thesis

An overall performance optimization of  $CO_2$  capture systems with physical absorption is attainable when all major process trade-offs are taken into account. For this, the solvent should be optimized simultaneously with the process conditions, using a single, process-based objective function.

In this work the solution of the integrated solvent and process optimization problem is approached with the CoMT-CAMD framework, using PC-SAFT. In CoMT-CAMD, the optimization problem is formulated as a non-linear program. The process and the solvent are described through continuous variables and are optimized simultaneously. The optimal solution of the process and solvent optimization problem is obtained without pre-selection of candidate solvents and heuristic objectives.

The work in the current thesis unfolds in two levels: a) the implementation of the CoMT-CAMD framework for the solution of the problem of optimal solvent selection for a pre-combustion  $CO_2$  capture system and b) the development and implementation of correlation models for the prediction of auxiliary properties of the solvent, aiming to enhance the accuracy in calculations inside CoMT-CAMD.

In Chapter 2, the CoMT-CAMD method is presented in detail. The implementation and application of CoMT-CAMD is developed for the case of simultaneous solvent and process optimization of a CO<sub>2</sub> capture process with physical absorption for an IGCC power plant. Calculation of full caloric properties in CoMT-CAMD requires predictions of the ideal gas heat capacity  $c_p^{\rm ig}$  of the optimized solvent. The calculation of mass specific quantities, such as specific density, requires predictions of the molar mass. QSPR models for  $c_p^{\rm ig}$  and the molar mass as function of the PC-SAFT pure component parameters were developed and integrated in the CoMT-CAMD framework. With CoMT-CAMD, a set of optimal solvents is identified from a large database of organic molecules, without pre-selection of candidates and for a reasonably complex process model. The set of optimal solvents include both state-of-the-art and new solvents, a fact underlining the validity and the strength of the CoMT-CAMD method.

The accuracy of PC-SAFT in calculations of state properties is decisive to the plausibility of the CoMT-CAMD solution. Especially for mixtures with highly unlike components, a correction  $(k_{ij})$  of the PC-SAFT EoS is usually required. A new method for the prediction of  $k_{ij}$ , independent of experimental mixture data and based solely on the PC-SAFT parameters of the pure components of the mixture, is presented in Chapter 3.

Chapter 4 analyzes the effect of predicted binary interaction parameter  $k_{ij}$  on the resulting list of promising candidate solvents from the CoMT-CAMD approach. The evaluation is done for the case of  $CO_2$  capture as detailed in Chapter 2. The result of the mapping step ('mapping list') obtained using  $k_{ij}$  predictions is compared to the result of the mapping step when no correction is used for the binary mixtures of the solvent ( $k_{ij} = 0$ ). Further, the result of the CoMT-CAMD is also compared to results from individual process optimizations with  $k_{ij}$  values adjusted to experimental data.

Chapter 5 assesses the results of the current work and discusses some ideas for further extensions to the CoMT-CAMD framework.

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# 2

Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD) for Simultaneous Process and Solvent Design for CO<sub>2</sub> Capture

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Solvent-based separation systems have a substantial potential for improvement when the solvent and the process conditions are optimized simultaneously. The fully integrated design problem, however, leads to an optimization problem of prohibitive size and complexity due to the many discrete degrees of freedom in selecting a solvent and the nonlinear nature of the process models. We here implement and extend the method of Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD) for the solvent and process optimization of a pre-combustion CO<sub>2</sub>-capture system with physical absorption. CoMT-CAMD is a deterministic procedure that does not require a pre-selection of solvent molecules. The process topology considered in our study includes all major process operations of an existing CO<sub>2</sub>-capture system: multi-stage absorption, desorption (two flash desorption stages with gas recycle) and CO<sub>2</sub> compression. We measure the process performance with a single economic objective function. The objective function captures the process trade-offs and evaluates potential process-solvent on a common basis. The solvent is represented as the pure component parameters of the Perturbed-Chain Statistical Associating Fluid Theory (PC-SAFT). The optimization problem is formulated with the pure component parameters of the solvent (PC-SAFT parameters) and with the process variables as degrees of freedom. Necessary auxiliary properties of the optimized solvent like the ideal gas heat capacity and the molar mass are predicted with Quantitative Structure Property Relationship (QSPR) models, based on the pure component PC-SAFT parameters. As a result, one gets a unified thermodynamic framework for fluid properties based on the PC-SAFT model. With CoMT-CAMD we obtain a list of the best performing physical solvents for the considered CO<sub>2</sub>-capture application. The resulting list of best performing solvents contains state-of-the-art solvents and new green solvent molecules.

#### **2.1.** Introduction

Identifying an optimal solvent for a specific process is a demanding task since the solvent selection cannot be decoupled from process design. The solvents for carbon capture by absorption, in particular, are known to critically determine the costs of possible processes. [1, 2] In pre-combustion carbon capture, for example, very different types of solvents are used in the main commercially installed processes (Selexol, Rectisol, Purisol and Fluor Solvent) [3]. On the one hand, the selected solvent determines the optimal operating point of the separation system [4-8]. On the other hand, specifications of process and operating conditions are decisive for the selection of new candidate solvents [9-12]. Wilcox et al. [13] recently revisited film theory for the mass transfer of carbon dioxide and illustrated the strong coupling between process parameters and solvent properties. In summary, the selection of an optimal solvent cannot be decoupled from the optimal selection of process conditions. The optimal performance of a solvent-based separation system is determined by both the solvent properties and the operating conditions. An integrated process and product design approach is needed. A full integration of the solvent and process optimization problems results however, in a mixed-integer non-linear programming (MINLP) problem

$$\begin{split} \min_{\overline{x},\overline{p}} f(\overline{x},\overline{p}) \\ \text{s.t.} \\ h(\overline{x},\overline{p}) &= 0 \\ g(\overline{x},\overline{p}) &\leq 0 \\ \overline{x} \in \Re^m, \overline{p} &= [p_1, \dots, p_D] \in \mathcal{P}DxN \end{split} \tag{2.1}$$

where  $f(\overline{x}, \overline{p})$  denotes the objective function of the optimization problem,  $h(\overline{x}, \overline{p})$ is the set of nonlinear equations representing the process model,  $g(\overline{x}, \overline{p})$  are the nonlinear process constraints and  $\overline{x}$  is the vector of the process variables. The process model  $h(\overline{x}, \overline{p})$  and the process constraints  $q(\overline{x}, \overline{p})$  include equations of the physical property model, in which a solvent is characterized by a parameter vector  $\overline{p}$ . Each candidate solvent species *i* is represented by the parameter vector  $\overline{p}_i$  in the discrete space  $\mathcal{P}^{DxN}$  where D is the number of model parameters to represent a solvent and N is the number of all real species considered in the problem. The choice of a solvent species i is therefore an integer decision in the N-dimensional search space. The mathematical formulation, Eq.(2.1), shows that solving the full MINLP problem for reasonably complex practical tasks is of prohibitive dimensionality N, determined by the number of conceivable molecules. Any attempt to solve the integrated optimization problem of Eq.(2.1) has to consider a mathematical or conceptual relaxation step to allow for practical (approximate) solutions. The various methods to circumvent or simplify the full MINLP problem in Eq.(2.1) can be used to classify the vivid research in the field of process and product design. A comprehensive overview of recent developments has been given by Adiman et al. [14].

One can thereby distinguish between methods that define auxiliary objective

functions  $\check{f}(\bar{p})$  to (pre)select solvents and methods that preserve the objective function  $f(\bar{x},\bar{p})$  on the process level. Note that an auxiliary objective function is usually defined such that  $\check{f}(\bar{p})$  does not depend on process variables  $\bar{x}$ , allowing the minimization of  $\check{f}(\bar{p})$  as an independent subproblem. Another class of approaches introduces simplified process models  $h(\bar{x},\bar{p})$  in order to make the problem solvable. One can further differentiate methods that limit the search space  $\check{N}$  to certain chemical structures in advance and methods that require no pre-selection. Another level of approximation decomposes the MINLP into an optimization problem with continuous parameter vector  $\bar{p}$  and a subsequent integer problem of identifying the optimal solvent.

In this regard, the structure of the MINLP problem in Eq.(2.1) was maintained in ref. [15, 16], but in order to ensure a feasible mathematical solution, either simplified process models are employed or the size of the considered integer (molecular) search space is limited. Sahinidis et al. [17] proposed an advanced global optimization strategy for the solution of the MINLP problem in Eq.(2.1). As objective function, their approach considered particular fluid properties as performance measures of the optimized fluid.

Many approaches decompose the full MINLP problem into two sub-problems, which are solved independently: First, a short-listing of the solvents is conducted based on heuristic, predefined performance measures or solvent properties  $\check{f}(\bar{p})$ ; subsequently, the process conditions are optimized for the pre-selected solvent(s). [18–20] Pre-selection based on heuristics requires, however, practical experience and process know-how. This decomposition approach has been shown to be powerful, when expert knowledge of the process is available [21, 22]. This knowledge, however, is not always available when new designs and processes are examined.

Marcoulaki and Kokossis [23] emphasized the significance of approaches that are unbiased from pre-selection procedures and thus maintain the potential for novel solutions. They proposed a framework that allows a maximum number of chemical structures to be considered for the molecular representation and they applied a stochastic algorithm for the solution of the optimization problem. They defined the objective function either on certain physical properties of the optimized molecule or on individual process streams. [23, 24]

Recent approaches in Computer Aided Molecular Design (CAMD) reduce the initial molecular search space using elegant mathematical or algorithmic techniques: Bommareddy et al. use enhanced enumeration techniques of higher order groups in a group-contribution approach. The process design problem is first solved to identify ranges of property targets, which are further used as process property constraints in a molecular design problem. [25] Samudra and Sahinidis [26] consider a simplified property model and allow for the solution of a mixed-integer linear problem (MILP) to define the initial molecular composition. In a following step, they use molecular graph techniques to define the exact molecular structures. Papadopoulos and Linke [27] implement multi-objective optimization and an iterative molecular clustering approach to confine the initial molecular search space. For the demanding case of reactive systems, Chemmangattuvalappil and Eden [28] implement the concept of molecular signature descriptors and the principles of molecular graph theory in property based molecular design. All the above methods are very elaborate but they still use auxiliary objective functions for the evaluation of the process performance, in order to reduce the problem complexity on the process level. Lampe et al. [29], however, showed that the dependence of process performance on molecular properties is not smooth due to process constraints. Such non-smooth objective functions of the full problem cannot be captured by auxiliary objective functions  $\check{f}(\bar{p})$  that are solved independent of the process model. Pereira et al. [30, 31] proposed a Computer Aided Molecular and Process Design (CAMPD) methodology for solvent selection among alkane-blends. This method uses a physically based thermodynamic model (SAFT-VR [32]). Thereby, variables describing the molecular structure can be directly embedded into the process model calculations. The overall performance is then evaluated with a single objective function measuring process performance.

The method of Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD), introduced by Bardow et al. [33], solves the molecular design problem simultaneously to the process optimization without pre-selection of candidate substances. CoMT-CAMD uses a physically based thermodynamic model to enable the direct coupling of the molecular structure to the process performance. In problem Eq.(2.1), the CoMT-CAMD approach relaxes the parameter vector  $\bar{p}$  from discrete values to continuous space. The resulting subproblem is a non-linear optimization problem, where solvent parameters  $\bar{p}$  and process variables  $\bar{x}$  are optimized simultaneously. In a subsequent step, a list of best real solvents is obtained from the optimized solvent parameters  $\bar{p}^{opt}$ . Lampe et al. [34] successfully implemented the CoMT-CAMD method for the simultaneous process and working fluid optimization for Organic Rankine Cycles.

Bardow et al. [33] presented a first conceptual implementation of the CoMT-CAMD method using a simplified topology for the  $CO_2$  capture. In the present work, we describe the further development of CoMT-CAMD and a comprehensive application of the method on the solvent and process optimization in separation systems using physical absorption. The further development concerns on the one hand a method for predicting the ideal gas heat capacity and the solvents' molar mass based solely on the solvent molecular parameters  $\overline{p}$ . This development enables the modeling of all thermal and full caloric properties of a target fluid within the CoMT-CAMD approach. On the other hand, we introduce a method to approximate non-equality process constraints during the mapping step. Further, a detailed process topology for the pre-combustion capture of carbon dioxide is now examined. We implement an economic objective function accounting for the various trade-offs in the absorption, desorption and CO<sub>2</sub> compression stage. We intend to show how CoMT-CAMD can be successfully performed for process models that include complex phase equilibrium calculations of multi-component streams. We demonstrate that CoMT-CAMD delivers accurate results and identifies the most promising solvents in a fully deterministic procedure.

## **2.2.** Continuous Molecular Targeting (CoMT)-CAMD for solvent selection

The CoMT-CAMD method for the integrated process and solvent design is founded on physically based thermodynamic models. In a physically based thermodynamic model, the pure component parameters are meaningful for identifying the structure of the molecules. In CoMT-CAMD, these parameters are used as optimization variables. Thereby, the solvent optimization is integrated into the process optimization level. In this work, we use CoMT-CAMD with the PC-SAFT (Perturbed Chain Statistical Associating Fluid Theory) thermodynamic model [35–38]. The pure component parameters of PC-SAFT describe the geometry, the van der Waals attractive energy, the strength of hydrogen bonds (association) and the multipole moments of a molecule. Each real substance is uniquely represented by a set of molecular parameters. Thus N real substances define a discrete parameter vector space  $\mathcal{P}^{(D \times N)}$ . As a result, any attempt to iterate the discrete parameter vector  $\overline{p}$  of real solvents together with the process equations leads to a mixed-integer optimization problem (cf. Eq.(2.1)). In order to circumvent the mixed-integer formulation, we relax the discrete vector space of the molecular parameters to a continuous domain. This relaxation strategy allows for the use of the parameters  $\overline{p}$  of the thermodynamic model as continuous optimization variables, along with the process degrees of freedom  $\overline{x}$ . In CoMT-CAMD, the integrated process and product design problem is therefore formulated as a constrained, non-linear optimization problem with an objective function f to evaluate the overall process performance.

The CoMT-CAMD method is generic and its accuracy is determined by the choice of the thermodynamic model. With this study, we intend to show that the PC-SAFT equation of state allows for a comprehensive description of thermodynamic properties of real fluids with good accuracy. Traditionally, PC-SAFT describes only residual quantities; i.e. quantities in departure of the ideal gas contribution. In this work we go beyond this scope: by applying Quantitative Structure Property Relationship (QSPR) methods, we correlate various auxiliary physical properties using only the pure component parameters of the PC-SAFT model. We achieve a thermodynamically consistent description of fluids based on a single set of parameters.

CoMT-CAMD proceeds in two steps: In the first step ('CoMT step') we solve an overall performance optimization problem to define the (hypothetical) optimal molecule with parameter vector  $\overline{p}^{opt}$  at optimal process conditions  $\overline{x}^{opt}$ . The best performing real molecules have parameter vectors  $\overline{p}$  similar to  $\overline{p}^{opt}$  due to the physical basis of PC-SAFT. In the second step of the method ('mapping step') we identify these real molecules with the best overall performance.

## **2.2.1.** Continuous Molecular Targeting: Simultaneous process and molecular optimization

The simultaneous optimization of process variables and molecular parameters is performed in the first step of the CoMT-CAMD method ('CoMT step', Figure 2.1). The integrated design problem, written as a non-linear optimization problem, is solved with a gradient based non-linear programming algorithm. The mathematical

c = -

problem is here formulated in a slightly more detailed form, compared to problem (2.1), as

(process model)	
(process inequality constraints)	
(convex hull on solvent parameters)	
	(2.2)
	(process inequality constraints)

As opposed to Eq.(2.1), where  $\overline{x}$  denoted all process variables, we here make a distinction between the process variables  $\overline{x}$  that are defined as degrees of freedom of the optimization problem and the remaining process variables  $\overline{\gamma}$ . We minimize a single process objective function f which depends on  $\overline{x}, \overline{y}$ , and the molecular parameters of the solvent  $\overline{p}$ . Degrees of freedom for the integrated problem are the process variables  $\overline{x}$  and the molecular parameters of the solvent  $\overline{p}$  in the continuous domain  $\mathcal{R}^n$  (with n = m + D according to Eq.(2.1)). The solution of the optimization problem is a vector with the optimal molecular parameters of the solvent and the corresponding optimal process conditions. In order to avoid extreme hypothetical molecules, we constrain the search space of the molecular parameters in the CoMT step to a region which is plausible. For this purpose, we confine the parameter space to the convex hull formed by the molecular parameters of real molecules in our database (Figure 2.2). In problem Eq.(2.2) the convex hull is written as a set of linear inequality constraints [39, 40] describing the planes of the convex hull fronts. Process constraints are considered in the problem formulation of Eq.(2.2) as non-linear inequality constraints,  $g(\overline{x}, \overline{p}, \overline{z})$ .

## **2.2.2.** Mapping step: Identification of the best performing components

The second step in the CoMT-CAMD method ('mapping step', Figure 2.1) identifies the real substances with similar behavior as the optimal molecule. Similarity in behavior is thereby measured by the objective function.

For every real substance i included in a database of molecular parameters ('mapping database'), we approximate the value of the objective function  $f_i$  by a second order Taylor series expansion around the optimal (hypothetical) molecular parameters  $\overline{p}^{opt}$ , as

$$f_i \approx f^{opt} + J(\overline{p}^{opt}) \cdot (\overline{p}_i - \overline{p}^{opt})^T + \frac{1}{2} \cdot (\overline{p}_i - \overline{p}^{opt})^T \cdot H(\overline{p}^{opt}) \cdot (\overline{p}_i - \overline{p}^{opt})$$
(2.3)

Every real substance in the database is represented by a known vector of molecular parameters  $\overline{p}_i$ . Here,  $f^{opt}$  is the optimal value of the objective function, the



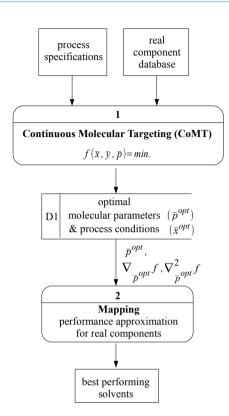


Figure 2.1: Data flow diagram of the CoMT-CAMD method.

Jacobian  $J(\overline{p}^{opt})$  and the Hessian  $H(\overline{p}^{opt})$  are the first and second derivatives of the objective function  $f^{opt}$  with respect to the molecular parameters at the optimum, respectively. Both,  $J(\overline{p}^{opt})$  and  $H(\overline{p}^{opt})$  are calculated in a subsequent step as described in section 2.3.2.

However, the derivatives of the objective function do not contain information about how changes of the molecular parameters affect the process constraints  $g(\bar{x}, \bar{y}, \bar{p}) \leq 0$  in Eq.(2.2). Even constraints that are not active at the optimum can be violated for small changes of the optimal parameters. In order to account for possible violations of process constraints, we approximate values of the inequality constraints  $g_i$  from a Taylor series of 1st order around the value of  $g^{opt}$  at optimum, as

$$g_i \approx g^{opt} + J_g(\overline{p}^{opt}) \cdot (\overline{p}_i - \overline{p}^{opt})^T \le 0$$
(2.4)

where  $J_g(\overline{p}^{opt})$  is the derivative of g with respect to  $\overline{p}$  at the optimum. The components that do not violate the constraints, according to their approximation with Eq.(2.4), are further evaluated for their performance with Eq.(2.3). Thereby, the components are ranked according to the approximated value of the objective function in the so called "mapping list". The best performing components in the mapping

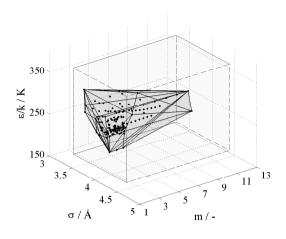


Figure 2.2: Convex hull defined by real molecules with respect to three molecular parameters  $(m, \sigma, \varepsilon/k)$ . Real molecules (spherical symbols) define a physically attainable search space. The optimization is allowed within the convex hull (grey-shaded volume). The fronts of the convex hull (planes defined by the continuous lines) are represented in the mathematical problem of Eq.(2.2) through linear inequality constraints.

list (i.e. components with lowest values of  $f_i$  in Eq.(2.3)) should be rigorously optimized. Finally, they should be examined for their toxicity, corrosivity, flammability or any health risks if required.

## **2.2.3.** Prediction of physical properties using PC-SAFT The PC-SAFT thermodynamic model

The SAFT (Statistical Associating Fluid Theory) equation-of-state (EoS) proposed by Chapman et al. [41] led to a family of theoretically based engineering equationsof-state, originating in statistical mechanics and based on Wertheim's perturbation theory [42, 43]. The Perturbed Chain Statistical Associating Fluid Theory (PC-SAFT) equation-of-state (EoS) introduced by Gross and Sadowski [35] is one of the variants of the SAFT-family of models (for a review see ref. [44]). PC-SAFT is based on a coarse-grained molecular model representing each molecule as a chain of spherical segments interacting with other chain molecules.[45] PC-SAFT is formulated as a residual Helmholtz energy, as function of temperature (*T*) and the vector  $\overline{\rho}$  of component molar densities  $\rho_i = \rho \cdot x_i$  of all species *i* of the system, according to

$$\alpha^{\rm res}(T,\overline{\rho}) = \alpha^{\rm hc}(T,\overline{\rho}) + \alpha^{\rm disp}(T,\overline{\rho}) + \alpha^{\rm assoc}(T,\overline{\rho}) + \alpha^{\rm polar}(T,\overline{\rho})$$
(2.5)

where  $\rho$  is the molar density and  $x_i$  here denotes the molar fraction of species *i*. The first term  $\alpha^{hc}$  of the residual Helmholtz energy in Eq.(2.5) describes the contribution of the hard-chain reference fluid. The additional terms account for various attractive parts of the intermolecular potential, namely contributions due to dispersive (van der Waals), associating (hydrogen bonding) and polar attractions.

Any other residual (static) thermodynamic property can be derived directly from the residual Helmholtz energy. For a full description of the PC-SAFT EoS we refer to the original literature [35–38]. We here refer to the polar version of the model, which was earlier also termed PCP-SAFT [37, 38], simply as PC-SAFT.

In PC-SAFT non-associating molecules are characterized by three pure-component parameters: the number of segments per chain molecule (m), the segment diameter parameter  $(\sigma)$ , and the dispersion energy parameter  $(\varepsilon/k)$ . For the description of polar molecules, the dipole moment  $(\mu)$  and the quadrupole moment (Q) are also required. Associating interactions are determined by two additional pure-component parameters: the association energy parameter  $(\varepsilon^{AB}/k)$  and the effective association volume  $(\kappa^{AB})$ . In this work, we do not include association parameters of the PC-SAFT model as degrees of freedom.

Correlation of auxiliary physical properties based on PC-SAFT parameters For process calculations with PC-SAFT we need to determine full caloric properties, such as enthalpies. For this purpose, we need a fundamental equation for the Helmholtz energy for the fluid phase region, with

$$\alpha(T,\overline{\rho}) = \alpha^{ig}(T,\overline{\rho}) + \alpha^{res}(T,\overline{\rho})$$
(2.6)

Thus, an expression for the residual Helmholtz energy  $\alpha^{\text{res}}$  from PC-SAFT is not sufficient; an ideal gas contribution is required. The ideal gas term is fully defined through the specific isobaric heat capacity  $c_p^{\text{ig}}$  of all involved species in pure state. While many alternative ways of defining the ideal gas contribution are possible, the route of specifying the ideal gas isobaric heat capacities  $c_p^{\text{ig}}$  of pure species is appropriate, because  $c_p^{\text{ig}}$  is available as primary measurement data for many components.

Our process calculations additionally require knowledge of the solvent's molecular mass  $M_i$ , since equipment sizing, cost functions and emission limits are often based on mass-averaged stream properties.

For known substances, the physical properties  $c_p^{ig}$  and M can easily be drawn from property databases. During molecular design in the CoMT step, this is not possible, since the iterated solvent molecule is hypothetical and only characterized by its PC-SAFT parameters. We therefore propose relations for estimating  $c_p^{ig}$  and M based only on the pure component parameters of the PC-SAFT model.

Correlations between the molar mass and the dispersive pure-component parameters of PC-SAFT ( $m, \sigma, \varepsilon/k$ ) have been investigated by other authors in the past. Gross and Sadowski [35] examined the underlying correlations for the homologous series of n-alkanes. Tihic et al. [46] demonstrated the near-linear dependencies between molar mass and combinations of the dispersive parameters for various component families, Grenner et al. [47] individually for glycols and Nannan et al. for polyethyleneglycol dimethylethers [48]. Mac Dowell et al. have also proposed relations between the pure component molecular parameters and the molecular mass of n-alkyl-1-amines for the SAFT-VR model. [49] Based on these findings, we use the four PC-SAFT parameters  $m, \sigma, \varepsilon/k$  and  $\mu$  as descriptors in a quantitative

structure property relationship (QSPR) model to predict the molar mass.

$$(M)^{\text{pred}} = \beta_1 \cdot (m^{\varepsilon/k}) + \beta_2 \cdot (m\sigma^3) + \beta_3 \cdot (m\sigma^{3\varepsilon/k}) + \beta_4 \cdot (m\sigma^3\mu)$$
(2.7)

For the prediction of  $c_p^{\text{ig}}$ , the QSPR descriptors are combinations of the three PC-SAFT parameters:  $m, \sigma$  and  $\varepsilon/k$ .

$$(c_p^{\text{ig}})^{\text{pred}} = \gamma_0 + \gamma_1 \cdot (m\varepsilon/k) + \gamma_2 \cdot (m\sigma^3) + \gamma_3 \cdot (m\sigma^3\varepsilon/k)$$
(2.8)

The heat capacity of pure substance in the ideal gas state accounts for the energy of the molecule due translation, rotation and all internal vibrations or excitations. Values of  $c_p^{ig}$  therefore strongly depend on the molecular structure. Although the PC-SAFT pure component parameters characterize intermolecular interactions, we argue that they should still be meaningful QSPR-descriptors for intramolecular energy states: The parameters *m* and  $\sigma$  should be suitable descriptors for rotational energies because they reflect a molecules' geometry in a coarse-grained manner, while  $\varepsilon/k$  measures the effective electron correlation among two sites and the parameter should thus serve as a sensible descriptor for vibrational energies.

## **2.3.** Application of CoMT-CAMD to solvent selection for CO<sub>2</sub> capture with physical absorption

#### 2.3.1. Process description and process specifications

The CoMT-CAMD method is here implemented for the integrated solvent and process optimization of a carbon capture system with physical absorption. We examine the pre-combustion carbon dioxide  $(CO_2)$  capture from the syngas stream of a coal-fired Integrated Gasification Combined Cycle (IGCC) power plant [50-52]. The process topology resembles in its key features the 'CO<sub>2</sub> Catch-up' pilot plant in Buggenum, the Willem Alexander Centrale (WAC), operated by NUON-Vattenfall. [53] The syngas feed includes three components: hydrogen (H<sub>2</sub>), carbon dioxide ( $CO_2$ ) and water ( $H_2O$ ). We particularly account for the presence of water in the system, since water has a significant impact on the phase equilibrium calculations. The mole fractions of hydrogen  $x_{H_2}^{sg}$  and water  $x_{H_20}^{sg}$ , as well as the temperature  $T^{sg}$  and the pressure  $P^{sg}$  of the syngas feed (Table 2.2) considered here are the same as for the syngas stream that enters the carbon capture pilot plant in Buggenum. The full process topology includes the major unit operations of the absorption, the desorption and the carbon dioxide compression stage (Figure 2.3). The solvent make-up stream consists of pure solvent at ambient pressure and temperature. All four substances regarded in the flowsheet (CO<sub>2</sub>, H<sub>2</sub>, H<sub>2</sub>O and the solvent) are present in the gas stream exiting the absorber ('hydrogen outlet') and the gas stream after compression ('pipeline gas'). The absorber is defined with a fixed number of 7 equilibrium stages  $N_{abs}$ , with a constant pressure of 2 MPa on the same pressure-level as the syngas stream, and with a constant CO<sub>2</sub> capture rate of 90% in the absorber. The value of 7 equilibrium stages is the result of a sensitivity analysis, where we observed little response of both, the optimal solvent parameters  $\overline{p}^{opt}$ , optimal process settings  $\overline{x}^{opt}$ , together with only a moderate decline of the objective function for  $N_{abs} > 7$  (see Appendix B.1.1). The desorption includes a first flash stage which feeds a hydrogen-rich gas back to the absorber, followed by an additional desorption flash. Both desorption stages are adiabatic (pressure-reduction) flash units.

For the rich gas and the pipeline compressors we consider a polytropic, adiabatic compression model as described in Smith [54]. The stream, process and equipment specifications are summarized in Table 2.2.

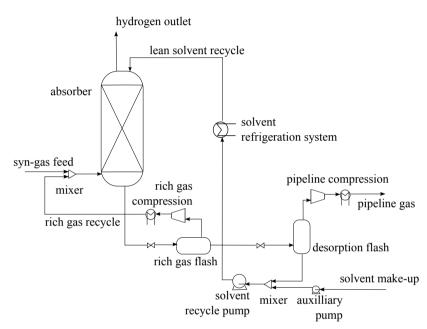


Figure 2.3: Flowsheet for  $CO_2$  capture with physical absorption, including absorption, desorption in two flash vessels and gas compression steps.

A more detailed description of the process model is given in Appendix B.1 of this thesis.

#### **2.3.2.** Description of the optimization problem

For our optimization problem (Eq.(2.2)) we define an economic objective function as the sum of several contributions of the operating costs,

$$f_{\text{tot}} = \sum_{i} f_{i} = f_{\text{electr.demand}} + f_{\text{H2 loss}} + f_{\text{solvent loss}} + f_{\text{utilities}}$$
(2.9)

The term  $f_{\text{electr.demand}}$  summarizes the costs of electricity for the solvent recycle pump and for the compressors (CO<sub>2</sub>-compression to pipeline-pressure and rich gas compression). We consider an electricity production price equal to  $55 \notin Mwh$  [56].

Table 2.1: Stream, process and equipment specifications adopted from the Buggenum pilot plant [53]. The pipeline pressure is taken from ref. [55]; efficiencies from ref. [50].

Stream specifications		
	x <sup>sg</sup> <sub>H2</sub> / <sup>mol</sup> /mol	0.5480
Syngas feed composition	x <sup>sg</sup> <sub>CO2</sub> / mol/mol	0.4485
	x <sup>sg</sup> /mol/mol	0.0035
Syngas feed temperature	T <sup>sg̃</sup> / K	313.00
Rich gas recycle temperature	T <sub>rg</sub> / K	313.00
Pipeline gas temperature	T <sup>ppl</sup> / K	313.00
Pipeline gas pressure	P <sup>ppl</sup> / MPa	11.00
Solvent make-up temperature	Т <sup>МU</sup> / К	298.15
Solvent make-up pressure	Р <sup>MU</sup> / MPa	0.1013
Process specifications		
CO <sub>2</sub> capture rate in absorber	$\alpha_{\rm CO_2}$ / –	0.90
Absorption pressure	P <sub>abs</sub> / MPa	2.00
Equipment specifications		
Absorber - number of stages	N <sub>abs</sub> / -	7
Rich gas compressor - number of stages	N <sub>comp-rg</sub> / -	1
Pipeline compressor - number of stages	N <sub>comp-des</sub> / -	1
Compressors - efficiency	η <sub>comp</sub> / –	0.82
Solvent recirculating pump - efficiency	η <sub>pump</sub> / –	1.00
Auxiliary pumps - efficiency	η <sub>aux.pump</sub> / -	0.75

 $f_{\text{utilities}}$  takes the operating cost of the cooling systems into account, given that this is measured through the electric energy demand for their operation [54]: The two heat exchangers (after the rich-gas compression and after the pipeline compression, (Figure 2.3)) are operated with cooling water. Thus, the cost contribution is due to the electrical duty of the cooling-water pumps. For cooling of the lean solvent recycle stream we consider a vapor compression refrigeration system with an exergetic efficiency  $\eta_{ex}$  of 25% [54, 57]. The term  $f_{\text{H2 loss}}$  is the lost profit due to hydrogen loss and evaluates the lost opportunity to produce electricity from the hydrogen that is captured in the CO<sub>2</sub>-rich stream. Finally, the term  $f_{\text{solvent loss}}$ expresses the costs for the fresh solvent. This term accounts for the solvent loss both in the absorption and desorption stage. We consider an average price of high molecular mass chemicals of 4,000 e/T. All cost-contributions are expressed per ton of captured CO<sub>2</sub> in the absorber. A more detailed description of the objective function is given in Appendix B.2.

The process model is given as a set of non-linear equality constraints  $h(\overline{x}, \overline{y}, \overline{p}) = 0$ . The absorber and the flash units are described by the so called MESH equations [58]. The process optimization variables  $\overline{x} = \{P^{\text{rg}}, P^{\text{des}}, T^{\text{lean}}\}$  include the desorption pressure of both desorption stages  $P^{\text{rg}}, P^{\text{des}}$  and the temperature of the lean solvent  $T^{\text{lean}}$ . The solvent optimization variables are the PC-SAFT molecular parameters of the solvent  $\overline{p} = \{m, \sigma, \varepsilon/k, \mu\}$ . Thus, we limit the presentation to non-associating solvents. As non-linear inequality process constraint  $g(\overline{x}, \overline{y}, \overline{p})$ , we limit the solvent emission  $m_s$  in the hydrogen outlet of the absorber to a maximum of  $20 \text{ mg/Nm}^3$  [59].The convex hull of the molecular parameter search space is given by the set of linear inequality constraints (Eq.(2.2)). [40]

For the solution of the optimization problem, we use a commercial NLP solver [60] with an interior Conjugate Gradient (CG) algorithm [61]. The solver delivers only the approximate Hessian of the Lagrangian at the optimum. For the mapping step, however, we need the Hessian and the Jacobian of the objective function and of the constraints at optimum (Eq.(2.3) and (2.4)). We currently calculate these derivatives with finite differences around the optimum with respect to the optimal solvent parameters  $\overline{p}^{opt}$ . The computation of each Hessian element  $\left(\frac{\partial^2 f}{\partial p_i \partial p_j}\right)_{p_{k\neq i,j}}$  with

forward finite differences demands four discretization points and one function evaluation for each discretization point. We evaluate the objective function  $f^*$  at each discretization point with  $p_i^+ = p_i^{opt} + \Delta p_i$ ,  $p_j^+ = p_j^{opt} + \Delta p_j$  and  $p_{k\neq i,j}^+ = p_{k\neq i,j}^{opt}$  solving the following optimization problem:

$$f^{+}(\overline{x}, \overline{y}, \overline{p} = \overline{p}^{+}) = \min_{\overline{x}} f^{+}(\overline{x}, \overline{y}, \overline{p} = \overline{p}^{+})$$
s.t.  

$$h(\overline{x}, \overline{y}, \overline{p} = \overline{p}^{+}) = 0 \quad (\text{process model})$$

$$g(\overline{x}, \overline{y}, \overline{p} = \overline{p}^{+}) = 0 \quad (\text{process ineq. constraint})$$

$$\overline{x}_{lb} \le \overline{x} \le \overline{x}_{ub}, \quad \overline{y}_{lb} \le \overline{y} \le \overline{y}_{ub} \quad (2.10)$$

The resulting Jacobian and Hessian (to be used in Eq.(2.3)) are thus defined for a surface of optimal process settings  $\overline{x} = \{P^{rg}, P^{des}, T^{lean}\}$ . We verified that for

the derivative calculations the use of central finite differences is not decisive for the accuracy of the Taylor approximation in the mapping step. The size of the differentiation step however should be selected carefully. The implementation of automatic analytic differentiation techniques can therefore be beneficial. Lampe et al. [29] successfully used an automatic differentiation tool in the CoMT-CAMD application for the Organic Rankine Cycle (ORC) process model.

#### 2.3.3. Predicting phase equilibria with PC-SAFT

The PC-SAFT pure component parameters of carbon dioxide, hydrogen and water are taken from the literature. Carbon dioxide is considered as a quadrupolar molecule. [37] The vapor-liquid equilibrium of pure hydrogen covers low temperatures, where quantum corrections are needed. We therefore considered hydrogen as a simple Lennard-Jones fluid and adopted parameters from Hirschfelder et al. [62], based on data of second Virial coefficients. The pure component parameters for water are taken from ref. [36] <sup>1</sup>. The heat capacity of ideal gas states,  $c_p^{ig}(T)$ , for  $CO_2$ ,  $H_2$  and  $H_2O$  is taken from the literature ref. [65].

For the vapor-liquid equilibrium calculations of the binary mixtures of  $CO_2/H_2O$ ,  $CO_2/H_2$  and  $H_2/H_2O$  we use non-zero binary interaction parameters  $k_{ij}$ . According to our correlation results, the maximum Absolute Average Deviation in both the liquid and the vapor phase occurs for the binary system  $CO_2/H_2$  with  $AAD(x_{CO_2/H_2}^L) = 1.6521\%$  and  $AAD(x_{CO_2/H_2}^V) = 1.3677\%^2$ . We note that for the three binary mixtures, the binary interaction parameter  $k_{ij}$  is treated as temperature independent. This is a simplification for the binary systems containing  $H_2O$ , which however avoids additional non-linearities in the NLP optimization problem. For the binary mixtures of the solvent with  $CO_2, H_2$  and  $H_2O$  respectively, we have set  $k_{ij}$  values equal to zero. Methods to predict  $k_{ij}$  values as a function of the PC-SAFT parameters are an objective of our current and future work. In order to provide some confidence in the phase equilibrium calculations of a relevant process solvent, Figure 2.4 shows the phase equilibrium of the ternary system  $CO_2 - H_2 -$  methanol at 2 MPa and 288 K<sup>3</sup>. The calculation results of PC-SAFT, with  $k_{ij} = 0$  for all pairs of substances involving methanol, can be considered in good agreement to the experimental data.

For the phase equilibrium calculations, we solve the adiabatic-isobaric flash problem. The sub-problem of the isothermal-isobaric two-phase flash is solved with the successive substitution Rachford-Rice algorithm (Michelsen and Mollerup) [66].

 $<sup>^1</sup>$  A summary of the parameters is published in ref. [63], available online as Supporting Information to the work of Stavrou et al. [64]

<sup>&</sup>lt;sup>2</sup>The calculated values of the binary interaction parameters  $k_{ij}$  and the correlation results are published in ref. [63], available online as Supporting Information to the work of Stavrou et al. [64]

<sup>&</sup>lt;sup>3</sup>Results for the same ternary mixture at other temperatures are published in ref. [63], available online as Supporting Information to the work of Stavrou et al. [64]

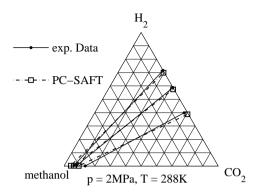


Figure 2.4: Ternary phase diagram for  $CO_2 - H_2 - MeOH$  at P = 2 MPa and T = 288 K. Comparison of predictions ( $k_{ij} = 0$  for the methanol pairs methanol- $CO_2$ , methanol- $H_2$ ) obtained from PC-SAFT (squares) to experimental data (circular points). Experimental data are taken from ref. [67].

## **2.3.4.** Mapping database of the PC-SAFT pure component parameters

Our study is based on a PC-SAFT pure component parameter database covering 657 real, non-associating components. The pure component parameters were adjusted to (quasi)experimental data taken from the DIPPR database [68]. The value of the dipole moment  $\mu_i$  for the polar components was taken directly from the DIPPR database. The n-polyethylene glycol dimethylethers included in our database (denoted hereafter as 'DEPG-n') are considered to be non-polar components and their molecular parameters have been adopted from the work of Nannan et al. [48].

For the design of the mapping database, we limit the database to components fulfilling the physical bounds of given process conditions: Substances are considered too volatile to be solvents if they have a normal boiling point temperature lower than 300 K. Further, we require a melting point temperature lower than 298.15 K and we exclude amines, nitriles and nitrates known to react with CO<sub>2</sub>.

As a result, the mapping database includes 612 polar and non-polar, non-associating components. We further divide the mapping database in two subordinate databases: The first includes 168 non-polar, non-associating components (denoted hereafter as the 'database of non-polar components'). The second includes 444 polar, non-associating components (denoted hereafter as the 'database of polar components'). It is sensible to introduce these subordinate databases since the components are described by different (sub)sets of PC-SAFT parameters (cf. Section 2.2.3). The definition of the mapping database was made prior to the CoMT step, so that the same database is used both, for the calculation of the convex hull during the optimization, and for the mapping afterward. A list of the 612 components comprising the mapping database is given in Appendix C.

It is straightforward to extend the approach formally to associating mixtures by including the corresponding pure component parameters as variables. Still, asso-

ciating components are currently not included in either of our databases because associating compounds in mixture with  $CO_2$ ,  $H_2$  and  $H_2O$  are expected to require non-zero binary interaction parameters. Vapor-liquid equilibrium calculations for these mixtures with zero binary interaction parameters  $k_{ij}$  would therefore not allow the desired level of accuracy of CoMT-CAMD. A sound implementation of associating solvents for the present mixture would thus require predictive methods for the binary interaction parameters  $k_{ij}$  which is an active topic of current research (see e.g., Haslam et al. [69])

#### 2.4. Results

## **2.4.1.** Prediction of pure component ideal gas heat capacity and molar mass using PC-SAFT parameters

For the prediction of the ideal gas heat capacity  $c_p^{ig}$  and of the molar mass M with the QSPR method as described in section 2.2.3, we use Eq.(2.8) and Eq.(2.7) respectively. For the prediction of  $c_p^{ig}$ , we have used constant temperature data for 300 K. For both  $c_p^{ig}$  and M, the QSPR coefficients in Eq.(2.8) and Eq.(2.7) have been estimated using ordinary multivariate normal maximum likelihood estimation, assuming normally distributed errors. We have used the multivariate linear regression algorithm *mvregress* provided in the Matlab Statistics Toolbox [70]. The squared correlation coefficient  $R^2$  used to evaluate the quality of the fitting is given by

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (w_{i}^{exp} - w_{i})}{\sum_{i=1}^{n} (w_{i}^{exp} - \overline{w}^{exp})}$$
(2.11)

We adjusted the QSPR coefficients separately for the two major component classes defined in section 1.3.4. For the ideal gas heat capacity  $c_p^{ig}$  we find values of  $R^2 = 0.991$  for non-polar and  $R^2 = 0.970$  for polar components. The QSPR multivariable regression for the molar mass M results to  $R^2 = 0.966$  for non-polar and  $R^2 = 0.932$  for polar components.<sup>4</sup> From all training sets, we excluded the inorganic components. Halogenated components are not taken into account for the QSPR model of the molar mass M, since they have very different QSPR-characteristics compared to other organic components. For the training set of  $c_p^{ig}$  values, we consider components for which data at 300 K were available in the DIPPR database. Figure 2.5 illustrates the QSPR results for  $c_p^{ig}$  and molar mass M for non-polar components. In particular, we do not expect the prediction of  $c_p^{ig}$  and of the molar mass M to cause significant error propagation in the process calculations of the CoMT step.

<sup>&</sup>lt;sup>4</sup>The size of the training sets, the squared correlation coefficients  $R^2$  and the resulting coefficients of the QSPR models are published in ref. [63], available online as Supporting Information to the work of Stavrou et al. [64]

<sup>&</sup>lt;sup>5</sup>The corresponding results for polar components are published in ref. [63], available online as Supporting Information to the work of Stavrou et al. [64]

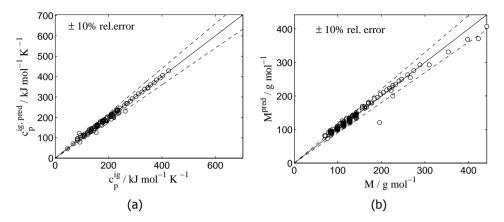


Figure 2.5: Literature values vs. QSPR results for (a) the ideal gas specific heat capacity at T = 300 K and (b) the molar mass of non-polar components. The dashed lines indicate  $\pm 10$  % relative error.

## **2.4.2.** Simultaneous solvent and process optimization: CoMT-CAMD for polar and non-polar solvents

Here, we present the results of CoMT-CAMD for the simultaneous process and solvent optimization for a CO<sub>2</sub> pre-combustion capture process. Non-polar components are fully described by three PC-SAFT parameters  $(m, \sigma, \varepsilon/k)$ . Polar components also require the dipole moment  $\mu$ . Due to this difference in parameter sets, we choose to solve the CoMT-CAMD problem for polar and non-polar components separately.

The pure component parameters of PC-SAFT are known to be correlated. We have made an attempt of defining less correlated coordinates by combining pure component parameters: the molecular 'volume'  $(m \cdot \sigma^3)$ , the molecular 'energy'  $(m \cdot \varepsilon/k)$  and  $(m \cdot \sigma^3 \cdot \varepsilon/k)$  as an expression that approximately scales the dimensionless Helmholtz energy [71]. The molecular optimization variables  $\overline{p}$  for polar components are the dispersive PC-SAFT parameters  $(m, \sigma, \varepsilon/k)$  and the reduced (dimensionless) dipole moment  $\mu^* = \mu/m \cdot \sigma^3 \cdot \varepsilon/k^{-1/2}$ .

In both cases, the process optimization variables  $\overline{x} = \{P^{\text{rg}}, P^{\text{des}}, T^{\text{lean}}\}\$  are the pressure of the rich gas flash, the pressure of the desorption flash and the temperature of the lean solvent, respectively. The process inequality constraint limits the solvent emission in absorber  $m_s$  to a maximum value of  $20 \text{ mg/Nm}^3$ .

The CoMT optimization for the non-polar solvents is initialized with the molecular parameters of Pentaethylene Glycol Dimethylether (DEPG-5). DEPG-5 is a common component in mixtures of physical solvents for  $CO_2$  absorption and therefore represents a suitable starting point. The result of the CoMT step and of the CoMT-CAMD method for non-polar solvents is summarized in Table 2.2. In Table 2.2, we compare the molecular parameters, the optimal operating conditions, and the value of the objective function for the initial substance DEPG-5, for the optimal (hypothetical) fluid and for the best real molecule (in the non-polar database). The CoMT optimization for polar solvents uses the parameters of N-methyl-2-pyrrolidone as

Table 2.2: Comparison of starting point, the result of the CoMT-step and the result of the CoMT-CAMD method for non-polar solvents. The CoMT-step defines the optimal (hypothetical) non-polar molecule. The 'mapping step' (which completes CoMT-CAMD) identifies the real molecule with best overall performance

	starting	optimal nonpolar	best nonpolar		
	molecule	molecule	real molecule		
	DEPG-5	hypothetical	1,5,9-		
			cyclododecatriene		
M/g/mol	266.33	174.22	162.27		
<i>m/-</i>	7.8895	3.1544	2.7575		
σ/Å	3.5853	4.5177	4.5709		
$\varepsilon/k/K$	253.93	360.37	377.14		
		optimal process conditions			
P <sup>des</sup> /MPa	0.197	0.239	0.234		
P <sup>rg</sup> /MPa	0.711	0.689	0.705		
T <sup>lean</sup> /K	265.3	273.4	274.2		
m <sub>S</sub> /mg/Nm <sup>3</sup>	0.0008	4.208	13.61		
f <sub>electr.demand</sub> /€/ <sub>T<sub>CO2</sub> capt.</sub>	7.894	7.228	7.197		
f <sub>H2 loss</sub> /€/ <sub>TCO2</sub> capt.	0.158	0.188	0.219		
f solvent loss /€/T <sub>CO2</sub> capt.	0.000016	0.089	0.316		
futilities/€/T <sub>CO2</sub> capt.	2.478	1.199	1.563		
f/€/T <sub>CO2</sub> capt.	10.53	8.704	9.295		

starting values. Table 2.3 compares results of the starting condition (with optimized process conditions  $\overline{x}$ ) to the results of the the CoMT-step and to results of the CoMT-CAMD method. Table 2.3 shows the pure component parameters, the optimal process conditions, and the value of the objective function for N-methyl-2-pyrrolidone (starting molecule), for the optimal (hypothetical) molecule and for the best real polar molecule (propylene carbonate). We note that the optimization converges to the same optimum from many starting points (real or hypothetical) in both cases. The computations have been performed on a standard desktop PC. For non-polar solvents the problem has 77 model variables in total, including the 3 molecular optimization variables and the 3 process optimization variables. In our implementation the NLP solver converges to the optimal solution in 44 iterations. For polar solvents the problem has 78 model variables in total, including the additional molecular optimization variable of dipole moment. For this problem the NLP solver converges to the optimal solution in 51 iterations.

In both cases, polar and non-polar components, the simultaneous process and solvent optimization leads to a successful minimization of the objective function. The optimal molecular parameters (hypothetical fluid) and the optimal operating process conditions obtained in the CoMT step define the best overall performance. The result is a lower bound to the minimization problem, as the best solution of the Table 2.3: Comparison of starting point, the result of the CoMT-step and the result of the CoMT-CAMD method for polar solvents. The CoMT-step defines the optimal (hypothetical) polar molecule. The "mapping"-step (which completes CoMT-CAMD) identifies the real molecule with best overall performance.

	starting optimal polar		best polar		
	molecule	molecule	real molecule		
	N-methyl- hypothetical		propylene		
	2-pyrrolidone		carbonate		
M/g/mol	99.131	100.47	102.09		
<i>m/-</i>	3.2008	3.2860	3.3130		
σ/Å	3.5095	3.3814	3.3598		
$\varepsilon/k/K$	314.59	308.57	313.92		
$\mu$ /D	4.0771	4.0771 4.9655			
	optir	nal process cond	itions		
P <sup>des</sup> /MPa	0.228	0.228 0.235			
P <sup>rg</sup> /MPa	0.650	0.631	0.633		
T <sup>lean</sup> /K	276.0	275.7	276.4		
m <sub>S</sub> /mg/Nm <sup>3</sup>	19.28	4.143	2.697		
felectr.demand/€/T <sub>CO2</sub> capt.	7.143	7.067	7.107		
f <sub>H2 loss</sub> /€/ <sub>TCO2 capt.</sub>	0.016	0.005	0.004		
f solvent loss /€/T <sub>CO2</sub> capt.	0.375	0.071	0.044		
f <sub>utilities</sub> /€/ <sub>TCO2</sub> capt.	0.569	0.518	0.518		
f/€/T <sub>CO2</sub> capt.	8.104	7.662	7.674		

minimization problem that is mathematically achievable with the selected thermodynamic model (PC-SAFT). The cost break-down on the various specific cost terms illustrates the benefit of using a single objective function: although some terms of the objective function are clearly dominant, the process trade-offs are balanced to enable an overall performance optimization. The best real component determined in the mapping-step is similar to the optimal hypothetical fluid, both, in terms of the pure component parameters and in terms of the corresponding process conditions. The performance of the best real component lies in the immediate vicinity of the optimum.

Tables 2.2 and 2.3 additionally show that state-of-the-art separation processes can be substantially improved, when solvent parameters and process conditions are optimized simultaneously. We compare the optimal performance of DEPG-5 (a typical component of the Selexol mixture) to the optimal performance of the best real molecules (1,5,9-cyclododecatriene and propylene carbonate) as measured by our objective function. There is a significant reduction of the specific cost: by 12 % for the best non-polar component and by 27 % for the best polar component. This improvement is even more significant if one takes into account that some cost contributions are fixed and cannot be improved by the solvent. Namely, the

compression of the CO<sub>2</sub> captured in the absorber (which is the same for all cases) from a pressure of 2 MPa (syngas feed) to the pipeline pressure of 11 MPa leads to a cost of  $2 \notin_{T_{CO_2capt}}$ .

The CoMT-CAMD method approximates the solution of the full MINLP problem in Eq.(2.1). More specifically it is the mapping step, i.e. the Taylor expansion Eq.(2.3) used to identify best performing real substances and the corresponding best process settings  $\bar{x}$ , where the procedure is approximate. In order to assess the quality of the mapping step, we have conducted individual process optimizations for all components included in both databases. The mapping list with the 10 best non-polar components is given in Table 2.4 and for the polar components in Table 2.5. The ranking predicted in the mapping-step ('mapping ranking') is compared to the ranking after the individual process optimizations ('real ranking'). The process optimization variables  $\bar{x}^{opt} = \{P^{des}, P^{rg}, T^{lean}\}^{opt}$  of the CoMT step were used as degrees of freedom for the individual process optimizations. These optimal process conditions along with the value of the process inequality constraint at optimum  $m_s^{opt}$  for each substance are also listed in Tables 2.4 and 2.5. The melting point temperature  $T_{mp}$  is the lowest temperature we allowed during each individual process optimization to avoid solvent solidification.

The results presented by Tables 2.4 and 2.5 are the core results of this study. Since the approximation made in the mapping step (Eq.(2.3) and (2.4)) is the only approximation towards the real solution of the full MINLP problem (Eq.(2.1)), it is important to find the rank list from the CoMT-CAMD procedure ('mapping ranking') in good agreement to the rank list of the individually optimized components. Tables 2.4 and 2.5 confirm that the 'mapping ranking' is very similar to the 'real ranking' and that all best components are feasible with respect to the process constraint ( $m_S^{opt} \le 20 \text{ mg/Nm}^3$ ).

A comparison between the optimal process conditions for the optimal molecule (Tables 2.2 and 2.3) and the optimal process conditions for the best real components (Tables 2.4 and 2.5, respectively) show that the identified molecules have strong similarities to the optimal molecule. The PC-SAFT parameters of the hypothetical molecule take on reasonable values, in a range, where real molecules occur. This is a significant observation, since no a priori constraints on parameter combinations are applied, beyond the convex hull.

We note that the specific cost values reported in this study serve as meaningful performance indicators. They should not, however, be interpreted as full cost estimates for a Carbon Capture and Sequestration (CCS) system, as usually presented in a techno-economic analysis of CCS systems (see e.g., ref. [72] and [73]). In particular, investment cost was neglected in our work. However, the cost objective function implemented here carries essential attributes of the full cost estimation and should allow discriminating between different solvents and process conditions.

#### **2.4.3.** Assessing the proposed solvents

Since the problem of solvent selection for  $CO_2$  capture with physical absorption is well established both in the literature and in the industrial practice, it is possible to validate (or at least evaluate) the proposed solvents. An important sign for Table 2.4: Best non-polar candidate solvents identified by CoMT-CAMD. The ranking predicted in the mapping step ('mapping ranking') is compared to the ranking after individual process optimization ('real ranking'). The optimal process conditions { $P^{\text{des}}$ ,  $P^{\text{rg}}$ ,  $T^{\text{lean}}$ }<sup>opt</sup> are given. The value of  $m_{\text{S}}$  indicates a components' feasibility against the inequality process constraint  $m_{\text{S}}^{opt} < 20 \, \text{mg/Nm}^3$ . The melting point temperature  $T_{\text{mp}}$  is the lower temperature bound to avoid solidification of the solvent.

IUPAC Name	ranking		f	m <sub>s</sub> <sup>opt</sup>	$P_{\rm des}^{opt}$	$P_{\rm rg}^{opt}$	T <sup>opt</sup> <sub>lean</sub>	T <sub>mp</sub>
	mapping	real	€/T <sub>CO2</sub> capt.	mg/Nm <sup>3</sup>	МРа	МРа	К	К
1,5,9-	1	1	9.295	13.61	0.234	0.705	274.2	256.4
cyclododecatriene								
bis(alpha-methyl-	2	4	9.399	0.750	0.233	0.705	278.0	243.2
benzyl)-ether								
bicyclohexyl	3	3	9.351	17.51	0.253	0.676	281.8	276.8
2-ethylnapthalene	4	5	9.419	2.120	0.219	0.698	274.2	265.8
n-heptylbenzene	5	2	9.342	1.650	0.226	0.699	267.6	225.2
1,2,4-triethylbenzene	6	7	9.489	7.450	0.222	0.702	267.9	195.2
n-hexylbenzene	7	6	9.457	4.710	0.223	0.701	267.9	212.0
n-pentylbenzene	8	14	9.661	15.66	0.217	0.707	268.3	198.2
1-n-propylnapthalene	9	8	9.510	0.710	0.218	0.699	272.5	264.6
n-undecane	10	16	9.750	12.26	0.219	0.711	263.1	247.6

Table 2.5: Best polar candidate solvents identified by CoMT-CAMD. The ranking predicted in the mapping step ('mapping ranking') is compared to the ranking after individual process optimization ('real ranking'). The optimal process conditions { $P^{des}$ ,  $P^{rg}$ ,  $T^{lean}$ }<sup>opt</sup> are given. The value of  $m_S$  indicates a components' feasibility against the inequality process constraint  $m_S^{opt} < 20 \text{ mg/Nm}^3$ . The melting point temperature  $T_{mp}$  is the lower temperature bound to avoid solidification of the solvent.

IUPAC Name	rankin	g	f	${\rm m_S}^{opt}$	$P_{des}^{opt}$	$P_{\mathrm{rg}}^{opt}$	$T_{\rm lean}^{opt}$	T <sub>mp</sub>
	mapping	real	€/ <sub>TCO2</sub> capt.	mg/Nm <sup>3</sup>	МРа	МРа	К	К
propylene carbonate	1	1	7.674	2.697	0.236	0.633	276.4	224.9
gamma-valerolactone	2	2	7.795	20.00	0.195	0.674	274.5	242.2
methyl maleic	3	5	8.384	19.94	0.245	0.642	281.2	281.2
anhydride								
n-methyl-	4	3	8.104	19.28	0.228	0.650	276.0	249.2
2-pyrrolidone								
diethyl sulfate	5	6	8.407	9.190	0.229	0.668	271.1	248.2
butyric anhydride	6	7	8.524	9.940	0.230	0.677	266.1	199.9
isobutyric anhydride	7	4	8.247	20.00	0.185	0.729	262.7	219.7
diphenyldichlorosilane	8	12	8.869	0.050	0.225	0.684	269.8	251.2
4-formylmorpholine	9	27	10.18	10.47	0.213	0.684	293.7	293.7
2-ethylhexyl acrylate	10	14	9.022	4.882	0.229	0.695	265.2	183.2

the validity of the proposed method is the fact that the mapping list of the polar candidates (Table 2.5) includes three state-of-the-art solvents: Propylene Carbonate (Fluor solvent process) [3], n-Methyl-2-Pyrrolidone (Purisol process) [3] and 4-Formylmorpholine (Morphysorb process) [74]. We note that the solvents identified in this study are different from the solvents identified with CoMT-CAMD for the pre-combustion  $CO_2$  capture in the previous work of Bardow et al. [33]. This is the result of implementing a different process topology and an economic objective function. In addition, an extended mapping database is used in this work compared with our earlier study. Generally, the identified solvents are a result of how the objective function is defined together with the process specifications we have laid out in Table 2.1. A strength of the CoMT-CAMD approach is that any change in the process specifications or the objective function very swiftly leads to a new list of promising solvents. Comparing the mapping lists of polar and non-polar components with each other (Tables 2.4 and 2.5) we observe, that the additional degree of freedom of polar substances is used in the optimization, leading to a lower value of the objective function. We also see that the best performing molecules possess certain functional groups. Almost all of the best performing polar molecules contain carbonylic groups, while phenyl rings are present in almost all identified polar and non-polar components. The phenyl rings and the carbonylic oxygen provide favorable interactions with CO<sub>2</sub>. These findings are reasonable and confirm earlier studies: Karazian et al. [75] demonstrated the specific interactions between CO<sub>2</sub> and the carbonylic oxygen using IR spectroscopy. Nelson et al. [76] showed, using ab initio calculations, that CO<sub>2</sub> will primarily interact with the carbonylic oxygen and that interactions with the phenyl ring can also be present but are weaker. Similar observations about the presence of certain functional groups in solvents for the physical absorption of  $CO_2$  are also discussed in the work of Miller et al. [11].

Enick et al. [10] mentioned siloxanes as potential solvents for the physical absorption of  $CO_2$  due to good  $CO_2$  solubilities. In our work, siloxanes are considered during the mapping of polar components. They are feasible components regarding the process constraint but they didn't appear in the 10 best polar components.

DEPGs are state-of-the-art solvents and they are feasible components according to our model but they are not included in the top-list of non-polar solvents (Table 2.4). The ether-oxygen in the DEPG molecule provides also a favorable interaction site for  $CO_2$ , leading to relatively high  $CO_2$  solubility. In CoMT-CAMD though components are evaluated for their overall performance. DEPGs, mainly due to their high molecular volume and the low absorption temperature required, lead to higher electricity demand and utilities' cost. The result is that according to our objective function they demonstrate a lower overall performance than small molecules with phenyl rings. If solvent loss gets a higher economic weight than in our objective function (e.g. by introducing an additional economic penalty for air pollution), the findings can be very different. DEPG components have a low vapor pressure leading to very low solvent loss (cf. Table 2.2).

The objective function evaluates the solvent performance beyond individual solvent properties and leads to molecules that: have sufficiently small molecular volume (to keep the specific cost of electricity demand in the pump low), are selec-

tive towards  $CO_2$  and not towards  $H_2$  (to achieve the same  $CO_2$  absorption rate for smaller solvent volumetric flows and lower hydrogen loss), are hydrophobic (to avoid water accumulation in the system), are less volatile and achieve the necessary cooling on a low cost.

Out of 612 non-associating components with diverse structural properties, CoMT-CAMD identifies those substances that optimize the overall process performance, without any prior judgment on favored functional groups and without using heuristics. The CoMT-CAMD results allow for conclusions about the proper molecular structure of the solvent and the optimal process conditions for a defined objective function through a continuous, deterministic mathematical procedure. In the mapping step, the database search could also be replaced by a molecular design algorithm to generate new molecular structures. Instead of mapping the optimal molecular parameters onto an existing database of pure component PC-SAFT parameters, one can map the optimal molecular parameters onto PC-SAFT parameters derived from a group-contribution approach. This would allow identifying substances beyond an existing database. This combinatorial approach requires a group contribution approach [77] and has already been implemented for the design of ORC fluids [78].

CoMT-CAMD also identifies new components which were previously not regarded for  $CO_2$  capture. An interesting example is the component gamma-Valerolactone, which is the second best polar solvent in the mapping list (Table 2.5). Gamma-Valerolactone has already been described by other authors as a promising green solvent for bio-refineries. [79, 80]

Further refinements of the flowsheet are possible, for example by considering additional flashes for the desorption or a heat integration scheme [81]. Any modification of the process specifications or of the objective function will result in a new rank list of solvents together with corresponding optimal process settings.

#### **2.5.** Conclusions

We analyze and further develop CoMT-CAMD for the simultaneous process and solvent optimization by considering a physical absorption process, namely a precombustion capture process of  $CO_2$ , where the absorption solvent is a degree of freedom. We developed QSPR models for the ideal gas heat capacity and the molar mass of the optimized solvent based on pure component parameters of the PC-SAFT equation of state and found very satisfying accuracy of these approaches for organic solvents. With these extensions, PC-SAFT provides a unified thermodynamic framework for predicting solvent properties throughout all steps of a systematic solvent and process optimization using CoMT-CAMD.

We observed that the rank list from the CoMT-CAMD method is a good approximation to the real rank list of the full MINLP problem of solvent and process design. We came to this conclusion by individually optimizing the process conditions of 612 substances (representing our database) in order to assess the results obtained by CoMT-CAMD. The agreement between the predicted rank list of best solvents is in very satisfying agreement to the actual rank list of individually optimized solvents. Moreover the predicted optimal process setting to each member of the most promising solvents is in very good agreement to the individually optimized process setting. Further, the predicted rank list of best solvents includes only feasible components without a priori pre-selecting fluids.

The process topology examined here represents the  $CO_2$ -capture process of an existing IGCC power plant [53], including all three major steps of absorption, desorption and  $CO_2$  compression and an emission limit for the solvent as a process constraint. CoMT-CAMD allows to measure the performance of the system with a single objective function that can be formulated freely according to the problem at hand. Our cost function summarizes several contributions to simultaneously evaluate all process trade-offs on a common basis. Since pre-combustion capture of  $CO_2$  is a well-studied process, it was reassuring to find that the rank-list of CoMT-CAMD comprises several state-of-the-art solvents. But, also new promising solvent candidates were identified.

CoMT-CAMD is a deterministic approach that does not involve any pre-selection or heuristic decisions. It is a versatile and generic method. CoMT-CAMD can be implemented with any physically based thermodynamic model. It is a suitable method for the integrated process and molecular design for a wide spectrum of existing applications as well as for new process designs, when limited process know-how is available.

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# 3

Estimation of the Binary Interaction Parameter  $k_{ij}$  of the PC-SAFT Equation of State Based on Pure Component Parameters Using a QSPR Method

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Statistical Associating Fluid Theory (SAFT) equations of state (EoS) for mixtures require cross-interaction parameters. For real systems, combining rules, such as the Lorenz-Berthelot combining rules, have to be corrected using at least one binary interaction parameter,  $k_{ii}$ . Values of  $k_{ii}$  are usually adjusted to experimental data of phase equilibria. Here, we correlate  $k_{ii}$  to the pure component parameters of the Perturbed Chain - Statistical Associating Fluid Theory (PC-SAFT) EoS, using a Quantitative Structure Property Relationship (QSPR) model. The coefficients of the proposed QSPR model are regressed separately for mixtures with non-associating components and for mixtures with associating components. The QSPR model is validated using the statistical measures of the QSPR method. We compare the values of  $k_{ii}$  that are estimated from the QSPR model to values of  $k_{ii}$  estimated from London's dispersive theory. Phase equilibrium calculations carried out with these two approaches of estimating  $k_{ij}$  values are compared to experimental data. The estimation of  $k_{ij}$  values as function of the pure component PC-SAFT parameters can be applied to problems of process design and in Computer Aided Molecular Design (CAMD), to allow for calculations that are reasonably accurate and independent from the availability of experimental mixture data.

## **3.1.** Introduction

Statistical Associating Fluid Theory (SAFT) equations of state (EoS) are expressions of the residual Helmholtz energy that represent approximate algebraic solutions of equations from statistical mechanics [1-4]. For mixtures, a SAFT EoS requires the intermolecular potential  $\phi_{ii}$  between the unlike molecules *i* and *j*. Usually, a conformal solution theory is applied, requiring cross-interaction parameters, such as a size-parameter  $\sigma_{ii}$  and an energy parameter  $\varepsilon_{ii}$ . Strictly speaking the i - jcross-interaction potential, just as the potential between like i - i species, has to be determined by quantum mechanical calculations. For van der Waals (dispersive) interactions, however, combining rules are often successful for estimating of cross-interaction parameters. Most variants of the SAFT-type EoS use the Lorenz-Berthelot combining rules:  $\sigma_{ij} = 1/2(\sigma_i + \sigma_j)$  and  $\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j}$ . For an accurate correlation of real systems, the combining rules have to be corrected using at least one interaction parameter,  $k_{ij}$  for every binary pair. As a modification of the Lorenz-Berthelot combining rules, the binary interaction parameter  $k_{ii}$  is introduced as a correction to the dispersive energy parameter for the binary pair:  $\varepsilon_{ii} = (1 - k_{ii}) \sqrt{\varepsilon_i \varepsilon_i}$ . Binary interaction parameters are often adjusted to experimental phase equilibrium data of the binary mixtures.

SAFT-type EoS were successfully applied to a wide range of complex systems, that include polar and associating components, polymers, ionic liquids, pharmaceuticals and bio-molecules (see for example ref. [1-3, 5-8]). SAFT-type EoS are often more accurate and more predictive than cubic EoS and extrapolate more reliably than g<sup>E</sup>-models [1]. For mixtures of substances where the intermolecular potentials are dominated by van der Waals interactions, SAFT-type EoS often give accurate results, even without binary correction ( $k_{ij} \approx 0$ ). Many mixtures of industrial interest however require adjusting a binary interaction parameter  $k_{ij}$ .

Experimental data of phase equilibria are not always available for the estimation of  $k_{ij}$  values. Consider the design of novel processes or a molecular design problem. In Computer Aided Molecular Design (CAMD) for example, thermodynamic models are required to evaluate some objective function quantifying the performance of the designed molecule [9, 10]. CAMD problems are formulated as reverse property prediction problems [11]. In CAMD problems it is not possible to adjust binary interaction parameters on experimental mixture data. Early stages of process design and CAMD rely on predictions of mixture behavior, which in our context means predictions of  $k_{ij}$  values.

O'Connell et al. [10] studied several thermodynamic property models and suggested SAFT-type EoS to have a potential for accurate property predictions in CAMD. In a recent study, Ng et al. [12] gave a thorough review of the various approaches and advances in CAMD methods. Among the most recent advances are CAMD frameworks that use a SAFT-type model [13–19]. Adjiman et al. [20] presented the rapid progress made in the field of SAFT-based CAMD and discussed the role of SAFT-type EoS in tackling previously challenging problems in molecular and process design. In a SAFT-based CAMD framework, variables that characterize the structure of the optimized molecule are utilized as additional degrees of freedom inside the process optimization. The molecular optimization can thereby be integrated with the process optimization problem, based on an objective function for the entire process. The problem of integrated process and fluid design has in the past been circumvented, by defining individual or collected property targets for the optimized fluid [21–23].

Pereira et al. [13, 15] introduced the framework of Computer Aided Molecular and Process Design (CAMPD) that uses the SAFT-VR EoS [24]. In their work, the authors applied CAMPD for the solvent selection among alkane blends. The molecular search space was defined over the homologous series of n-alkanes and the number of carbon atoms of the n-alkane was treated as a continuous molecular optimization variable. The necessary SAFT-VR parameters were expressed as functions of the molecular mass and therefore as functions of the optimized number of carbon atoms. The values of  $k_{ij}$  for the SAFT-VR EoS were adjusted to experimental phase equilibrium data of binary mixtures relevant to the examined system and they were held constant throughout CAMPD. Recently, Burger et al. [25] proposed a CAMPD method that uses the SAFT- $\gamma$  Mie GC EoS [26] and a hierarchical optimization approach. The authors demonstrated the proposed method for the problem of solvent selection adopted from Pereira et al. In their work, Burger et al. [25] applied a group contribution (GC) approach for SAFT and considered additional chemical families extending the search space to linear alkyl ethers.

The framework of Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD), established by Bardow et al. [14], uses the PC-SAFT EoS [27–30]. CoMT-CAMD considers the parameters of the thermodynamic model (e.g. representing a solvent) as additional degrees of freedom in an integrated process and fluid optimization problem. In CoMT-CAMD the discrete search space of parameters representing a real substance is relaxed to a continuous parameter domain. Specifically, the molecular optimization variables (PC-SAFT pure component parameters) are treated as continuous variables. This relaxation allows formulating a non-linear optimization problem with a single objective function, whereby a detailed process model can be maintained without the need for pre-selecting candidate molecules. CoMT-CAMD has been implemented, so far, for the selection and design of working fluids for organic rankine cycles (ORCs) [16, 19] and for the selection and design of physical solvents for  $CO_2$  capture [18, 19]. In phase equilibrium calculations no binary interaction correction was introduced to the PC-SAFT EoS for binary systems involving the optimized fluid ( $k_{ii} = 0$ ).

The result of a CAMD approach is determined by the employed thermodynamic model. The accuracy of the SAFT model therefore plays a crucial role in the predictive capability of the CAMD framework.

In order to improve predictions of mixture properties (with  $k_{ij} = 0$ ), many studies have revisited the Lorentz-Berthelot combining rules [31–38]. More recently, Haslam et al. [39] derived a new combining rule using a generalization of the Hudson-McCoubrey combining rules, including additional terms for the dipole-dipole and the dipole-induced dipole interactions. The authors presented results of their theory with the SAFT-VR EoS [24] for mixtures with large non-polar and polar components and for mixtures with a single associating component. Singh et al. [40] and Leonhard et al. [41] proposed the prediction of pure component param-

eters based on quantum mechanical calculations and a new combining rule for the unlike-dispersion interaction, derived from London's dispersive theory. Leonhard et al. applied the proposed combining rule with the PC-SAFT EoS. Both of the above approaches have a theoretical background and gave good results for mixtures.

Group contribution approaches are promising for estimating binary interaction corrections  $k_{ij}$  to the Lorenz-Berthelot combining rules. Peters et al. [42] proposed a group contribution method for determining binary interaction parameters of the PC-SAFT EoS for polymer-solvent mixtures. Inspired by London's dispersive theory, Huynh et al. [43, 44] proposed the correlation of  $k_{ij}$  to pseudo-ionization energies of the constituents of the mixture. The method was developed for the GC-SAFT EoS [45] and was shown to lead to very good results. London's dispersive theory applied to the Mie potential function has been used by Coutinho et al. [46] to derive a new combining rule for the cross-energy parameter in cubic EoS and in the Cubic Plus Association EoS [47].

Due to the analogy between the combining rules of SAFT-type EoS and the combining rules in cubic EoS, we mention the work of Shacham et al. [48] and the work of Abudour et al. [49]. Both studies proposed the prediction of  $k_{ij}$  values for cubic EoS using a Quantitative Structure Property Relationship (QSPR) method with automatically generated molecular descriptors.

The CoMT-CAMD approach requires the prediction of mixture properties (i.e. estimating a suitable  $k_{ij}$ ) based on pure component parameters of PC-SAFT for the optimized fluid. On that grounds, two of the approaches for estimating  $k_{ij}$  mentioned above particularly lend themselves for the CoMT-CAMD framework: the estimation of  $k_{ij}$  based on predicted ionization potentials and the QSPR estimation method.

In this work, we relate the binary interaction parameter  $k_{ij}$  to pure component parameters of both substances, in order to allow for predicting mixture properties in CAMD applications, especially in the CoMT-CAMD framework. Two approaches are examined. Values of  $k_{ij}$  are estimated based on London's dispersive theory using experimental ionization potentials. Further, we propose a multilinear regression model for estimating  $k_{ij}$  based only on the PC-SAFT pure component parameters. For the development of the proposed model, a QSPR method is applied.

# **3.2.** Estimation of $k_{ij}$ based on London's dispersive theory

For a mixture of conformal fluids, i.e. fluids with the same functional form of van der Waals intermolecular pair potentials, theoretical expressions of the  $k_{ij}$  value can be derived from London's dispersive theory. Most common is the expression based on the work of Hudson and McCoubrey [50]. Hudson and McCoubrey wrote the equation of London's attractive potential  $\phi_{ij}^{disp}$  as function of the ionization potentials  $I_i$  and  $I_j$  and the (scalar valued) static polarizabilities  $\alpha_i$  and  $\alpha_j$  of the two constituents of the mixture

$$\phi_{ij}^{\text{disp}} = -\frac{3}{2} \frac{I_i I_j}{(I_i + I_j)} \frac{\alpha_i \alpha_j}{r_{ij}^6}$$
(3.1)

Eq.(3.1) combined with the attractive part of the Lennard-Jones potential

$$\phi_{ij}^{\text{LJ}} = 4\varepsilon_{ij} \left( \left[ \frac{\sigma_{ij}}{r_{ij}} \right]^{12} - \left[ \frac{\sigma_{ij}}{r_{ij}} \right]^{6} \right)$$
(3.2)

and using the arithmetic mean for the segment diameter parameter  $\sigma_{ij}$ 

$$\sigma_{ij} = \frac{1}{2} \left( \sigma_i + \sigma_j \right) \tag{3.3}$$

led to an expression for the depth of the attractive potential well due to dispersive interactions  $\varepsilon_{ij}$ , i.e. the Hudson-McCoubrey rules

$$\varepsilon_{ij} = \left[2 \cdot \frac{\left(I_i I_j\right)^{1/2}}{\left(I_i + I_j\right)}\right] \cdot \left[2^6 \cdot \frac{\sigma_i^3 \sigma_j^3}{\left(\sigma_i + \sigma_j\right)^6}\right] \cdot \sqrt{\varepsilon_i \varepsilon_j} \quad . \tag{3.4}$$

For a SAFT-type EoS Eq.(3.4) leads to an approximation of  $k_{ij}$  as function of the segment diameter parameters and the ionization potentials of the two Lennard-Jones fluids in the mixture

$$k_{ij} = 1 - \left[2 \cdot \frac{(I_i I_j)^{1/2}}{(I_i + I_j)}\right] \cdot \left[2^6 \cdot \frac{\sigma_i^3 \sigma_j^3}{(\sigma_i + \sigma_j)^6}\right] \quad .$$
(3.5)

For details on the derivation of Eq.(3.4) and Eq.(3.5) we refer to the original work of Hudson and McCoubrey [50] and to the study of Haslam et al. [39].

The expression in Eq.(3.5), derived from London's theory, accounts only for the asymmetry in dispersive interactions. For mixtures of polar or associating components, however,  $k_{ij}$  does not only serve as correction to the dispersive intermolecular potential, as already pointed out by Hiza and Duncan [32] and Kontogeorgis [51]. Rather,  $k_{ij}$  corrects a SAFT-type model regarding any other model deficiency, including those arising from attractive interactions, not explicitly accounted for. However, London's dispersive theory is appealing for (CoMT-) CAMD applications, and more generally for predicting mixture properties, because only pure component properties of the mixtures' constituents are required. In this work, we evaluate phase equilibria predicted using  $k_{ij}$  values from Eq.(3.5) applied with the PC-SAFT model, using experimental values for the required ionization potentials.

## **3.3.** Multivariate regression model for $k_{ij}$ prediction **3.3.1.** Contribution of asymmetric intermolecular potentials to the value of $k_{ij}$

QSPR studies focus mainly on the prediction of properties for pure substances. In most QSPR studies, QSPR software like CODESSA [52] or DRAGON [53] is employed to generate constitutional, topological, geometrical, electrostatic, quantum chemical or thermodynamic molecular descriptors (e.g. ref. [49, 54, 55]). The

significant descriptors are then selected using various stochastic or deterministic methods. Subsequently, the selected descriptors are combined to generate QSPR models. The resulting QSPR models are evaluated and compared based on multivariate statistics. In this study, we aim to develop a QSPR model for the estimation of  $k_{ij}$ , whereby  $k_{ij}$  is a mixture attribute. While a large number of descriptors are available for pure substances, the number of descriptors characterizing molecular pairs is very limited [56]. Here, we define the QSPR descriptors in an ad hoc manner, based on two principles. The descriptors for the estimation of  $k_{ij}$  should: First, be a function of the PC-SAFT pure component parameters only, and second, effectively relate dissimilarities in the molecular structure of two components to the  $k_{ij}$  value of their binary mixture.

In PC-SAFT, each pure component is identified by a unique set of molecular parameters: the segment number m, the segment size parameter  $\sigma$ , the dispersive energy parameter  $\varepsilon/k$ , the dipole moment  $\mu$ , the quadrupole moment Q, the association energy parameter  $\varepsilon^{AB}/k$  and the effective association volume  $\kappa^{AB}$ . The equation of the QSPR model for the estimation of the value of  $k_{ij}$  ( $k_{ij}^{\text{QSPR}}$ ) as function of the molecular parameters of the mixture components is therefore

$$k_{ij}^{\text{QSPR}} = \sum_{L=1}^{N_d} c_L \cdot D_L(\overline{p}_i, \overline{p}_j)$$
(3.6)

where  $N_d$  is the number of descriptors,  $D_L(\overline{p}_i, \overline{p}_j)$  are the descriptors as function of the PC-SAFT molecular parameters  $\overline{p}_i = \{m_i, \sigma_i, \varepsilon_i/k, \mu_i, Q_i, \varepsilon_i^{AB}/k\}$  and  $\overline{p}_j = \{m_j, \sigma_j, \varepsilon_j/k, \mu_j, Q_j, \varepsilon_j^{AB}/k\}$  of the two components, *i* and *j*, of the mixture, and  $c_L$  are the corresponding regression coefficients.

Let  $p_{k,i}$  be the  $k^{\text{th}}$  element of the PC-SAFT pure component parameter vector  $\overline{p}_i$ , e.g.  $p_{1,i} = m_i$ . Relations such as ratios of the pure component parameters,  $a_{ij} = p_{k,i}/p_{k,j}$  or absolute differences,  $\delta_{ij} = |p_{k,i} - p_{k,j}|$  can be used as measures of the asymmetry of intermolecular potentials in the binary mixture. Parameter ratios  $a_{ij}$  and absolute differences  $\delta_{ij}$  can also be defined over combinations of the PC-SAFT parameters:  $a_{ij} = h(\overline{p}_i)/h(\overline{p}_j)$  and  $\delta_{ij} = |h(\overline{p}_i) - h(\overline{p}_j)|$ . The departure of  $a_{ij}$  from unity and of  $\delta_{ij}$  from zero quantify the difference between the i - i and the j - j property for the two components of the mixture, respectively. In order to make the parameter ratio  $a_{ij}$  invariant for interchanging the component indices i and j for the pair of substances, we further define the ratio operator

$$\langle a_{ij} \rangle = \begin{cases} a_{ij}^{(a_{ij}-1)} & a_{ii} \neq a_{jj} \\ 1 & a_{ii} = a_{jj} \end{cases}$$
(3.7)

Measures of this type were combined to form the candidate descriptors for the QSPR model.

Unlike intermolecular potentials are caused by asymmetric dispersive, polar and associating forces. In order to quantify the contribution of the aforementioned

asymmetries to the  $k_{ij}$  value, we defined eight descriptors. The initial form of the descriptors was mainly motivated by parameter combinations as they appear in the mathematical formulation of the PC-SAFT EoS. The exponents used in the final mathematical formulation of the descriptors are defined empirically.

#### **Dispersive interactions**

We define the descriptor  $D^{LJ}$  to express the asymmetry in the dispersive intermolecular potential, as

$$D^{\text{LJ}} = 1 - \left(\frac{\sigma_i^3(\varepsilon_i/k)^2}{\sigma_j^3(\varepsilon_j/k)^2}\right)$$
(3.8)

by taking into account the segment diameter  $\sigma_i, \sigma_j$  and the Lennard-Jones energy potentials  $\varepsilon_i/k, \varepsilon_j/k$ . Our starting point for this descriptor has been the ratio  $\langle \frac{m_i^2 \sigma_i^3 (\varepsilon_i/k)^2}{m_j^2 \sigma_j^3 (\varepsilon_j/k)^2} \rangle$  as motivated from the first order term of the perturbation theory for dispersive attraction. The exponents were varied empirically, usually in the integer-range of  $\pm 2$ .  $D^{LJ}$  will approach zero for very similar components and if no other types of interactions exist (e.g. polar or associating interactions).

#### Polar interactions

For contributions to the value of  $k_{ij}$  due to polar interactions, we define four descriptors. The contribution due to asymmetry in dipole-dipole interactions is expressed through the descriptors  $D^{dd,a}$  and  $D^{dd,b}$ . Descriptor  $D^{dd,a}$  measures the absolute difference in the reduced dipole moments.

$$D^{dd,a} = \left| \frac{\mu_i}{\sqrt{m_i \sigma_i^3(\varepsilon_i/k)}} - \frac{\mu_j}{\sqrt{m_j \sigma_j^3(\varepsilon_j/k)}} \right|$$
(3.9)

The difference in the reduced dipole moments contributes in a different way to the asymmetry in mixtures with only one dipolar component than in the case when both mixture components are dipolar. In order to distinguish these two cases, we introduce the descriptor  $D^{dd,b}$ .

$$D^{dd,b} = \sqrt{\mu_i \mu_j} \cdot \left(\mu_i - \mu_j\right)^2 \tag{3.10}$$

A further contribution due to asymmetry in quadrupole-quadrupole interactions is given by the descriptor  $D^{qq}$ . Descriptor  $D^{qq}$  considers the difference of the scaled quadrupole moments over the potential energy of the chain molecule. The difference in the quadrupole moments is scaled by the ratio of segment diameters according to

$$D^{qq} = \left[\frac{Q_i}{m_i(\varepsilon_i/k)} - \frac{Q_j}{m_j(\varepsilon_j/k)}\right]^2 \cdot \left\langle \frac{\sigma_i^5}{\sigma_j^5} \right\rangle$$
(3.11)

Finally, we account for the case that dipole-dipole and quadrupole-quadrupole interactions occur simultaneously with the descriptor  $D^{dq}$ .

$$D^{dq} = \left| \frac{\mu_i}{\sqrt{m_i \sigma_i^3(\varepsilon_i/k)}} - \frac{\mu_j}{\sqrt{m_j \sigma_j^3(\varepsilon_j/k)}} \right| \cdot \left[ \frac{Q_i}{m_i(\varepsilon_i/k)} - \frac{Q_j}{m_j(\varepsilon_j/k)} \right]^2$$
(3.12)

#### Association

Naive combining rules are not suited to describe cross-association of two substances, because cross-association can not be detached from electrostatic concepts of partial charge distributions in individual molecules. In that light, it is surprising that simple combining rules have shown promising results for a collection of chemical species [28, 51, 57]. (A group contribution approach on the other hand is in our view a rather promising concept). In studies where combining rules for cross-association are applied, a binary interaction correction is often applied to the dispersive interactions, rather than to the cross-association.

Consequently, mixtures with (cross-)associating substances are demanding for our approach, where the binary mixture shall be described based on pure component parameters of both species. With some reservation, we include associating mixtures in this study. It is important to note that the  $k_{ij}$  parameters adjusted to such mixtures usually show rather high (positive or negative) values, because of the uncertainty in cross-associating interactions. We account for the contribution of self- and cross-association effects with three descriptors. Descriptor  $D^{assoc,s}$  measures the strength of self-association for component *i* against the strength of self-association for component *j*.

$$D^{assoc,s} = \sqrt{(\varepsilon_i/k)(\varepsilon_j/k)} \cdot \left[\sigma_i^3\left(\varepsilon_i^{AB}/k\right) - \sigma_j^3\left(\varepsilon_j^{AB}/k\right)\right]^2$$
(3.13)

Kontogeorgis and Folas [58] distinguish between five different types of cross-association. We turn to the effect of cross-association between two dipolar components, when at least one of them is self-associating. Kleiner and Sadowski [57] proposed an approach to account for the cross-association that is likely to occur for such mixtures; they refer to these interactions as 'induced association'. We also observed that the combining rule for induced association [28, 59]

$$\varepsilon^{A_i B_j} = \frac{1}{2} \left( \varepsilon_i^{AB} + \varepsilon_j^{AB} \right) \tag{3.14}$$

$$\kappa^{A_i B_j} = \sqrt{\kappa^{A_i B_i} \kappa^{A_j B_j}} \cdot \left(\frac{\sigma_i \sigma_j}{1/2 \left(\sigma_i + \sigma_j\right)}\right)^3 \tag{3.15}$$

noticeably improves the accuracy of phase equilibrium calculations for this type of mixtures. The descriptor for the contribution due to induced association is defined as

$$D^{assoc,c} = \sqrt{\mu_i \mu_j} \cdot \frac{\left[ (\varepsilon_i^{AB}/k) + (\varepsilon_j^{AB}/k) \right]^2}{\sqrt{\left( m_i \sigma_i^3 \cdot m_j \sigma_j^3 \right)}}$$
(3.16)

The indices s and c in Eq.(3.13) and (3.16) are for "self" and "cross" association contributions, respectively. The contribution to the value of  $k_{ii}$  due to induced association accounts for the mutual strength of the dipole moments [60]. The contribution of the association energy parameters and the dipole moments in the descriptor  $D^{assoc,c}$  is scaled by the molecular volume of the two components. This provides a better description for mixtures with small but strong associating molecules (e.g. mixtures of acetic acid) [61]. In mixtures with one associating and one non-polar, non-associating component, the effect of induced-association should not be accounted for. In this case, the descriptor  $D^{assoc,c}$  is therefore equal to zero and no discrete decisions are necessary to distinguish between cases. The contribution of induced association in the asymmetry of a mixture is different when both components are self-associating species than when the mixture contains only one self-associating component and one dipolar, non-associating component. We introduced the third descriptor Dassoc, in order to decouple the two cases when describing these types of mixtures with the same model simultaneously. The descriptor D<sup>assoc,sc</sup> is active only for mixtures with two self-associating components

$$D^{assoc,sc} = \left(\mu_i \mu_j\right) \cdot \sqrt{\left(\varepsilon_i^{AB}/k\right)\left(\varepsilon_j^{AB}/k\right)} \cdot \left| \left[\sigma_i^3\left(\varepsilon_i^{AB}/k\right)\right]^2 - \left[\sigma_j^3\left(\varepsilon_j^{AB}/k\right)\right]^2 \right| \quad . \tag{3.17}$$

#### 3.3.2. Pure component parameters

The necessary PC-SAFT pure component parameters were either adopted from ref. [27–30, 62] or, if not available, they were identified in the present work. In those cases, the pure component parameters  $(m, \sigma, \varepsilon/k, \varepsilon^{AB}/k)$  were adjusted to experimental data of vapor pressure and liquid density. We have implemented the 2*B* association scheme [63] for all associating components. The association energy parameter  $\varepsilon^{AB}/k$  and the effective association volume  $\kappa^{AB}$  are known to be strongly correlated, which is why a constant effective association volume  $\kappa^{AB} = 0.03$  was used, as previously suggested by Ruether and Sadowski [64]. Dipole moments were taken from the DIPPR database [65] and they originate either from *ab initio* calculations or from measurements. The quadrupole moments were taken from ref. [29].

# **3.3.3.** Database of $k_{ij}$ values adjusted to experimental data of phase equilibria

For isolating the effect of the different descriptors, we define four classes of substances: non-associating, non-polar (nAnP), non-associating, dipolar (nAdP), nonassociating, quadrupolar (nAqP) and associating, dipolar (AdP). From the four classes of pure components, we define 10 groups of binary mixtures. The 10 groups of binary systems considered in our study and the number of mixtures per group are listed in Table 3.1.

For every binary mixture in our database, we adjusted the binary interaction parameter  $k_{ij}$  using experimental vapor-liquid equilibrium (VLE) data. The selected experimental data comprised sets of isothermal (P,x) and (P,x,y) data obtained from the Dortmund Database (DDB) [66], which passed the standard thermody-

namic consistency tests, namely the point-to-point test and the area-test. [67] For mixtures with several experimental isotherms, we adjusted a single temperature-independent value of  $k_{ij}$ . The objective function for adjusting the  $k_{ij}$  values is

Table 3.1: The database of binary mixtures is divided in 10 groups (here denoted as G1 to G10). The binary mixtures are categorized according to the type of components they consist of: (a) non-associating, non-polar (nAnP), (b) non-associating, dipolar (nAdP), (c) non-associating, quadrupolar (nAqP) and (d) associating, dipolar (AdP). The number of mixtures for each subgroup in the database is listed.

	comp. j				
		nAnP	nAdP	nAqP	AdP
	nAnP	<sup>(G1)</sup> 48			
comp. i	nAdP	<sup>(G2)</sup> 47	<sup>(G6)</sup> 23		
	nAqP	<sup>(G3)</sup> 44	<sup>(G4)</sup> 32	<sup>(G5)</sup> 5	
	AdP	<sup>(G7)</sup> 67	<sup>(68)</sup> 90	<sup>(G9)</sup> 43	<sup>(G10)</sup> 53

formulated on the combined residuals of the mole fraction of the liquid phase and the residuals of the pressure for every experimental point [68]:

$$F = \left[\sum_{l=1}^{n_{\text{exp}}} \frac{(\Delta x_l)^2 \cdot (\Delta P_l^{rel})^2}{(\Delta x_l)^2 + (\Delta P_l^{rel})^2}\right]^{1/2}$$
(3.18)

with  $n_{exp}$  as the number of experimental data points,  $\Delta x_l = |x_l^{calc} - x_l^{exp}|$  the absolute residuals in the mole fraction of the liquid phase resulting from isobaricisothermal flash calculations and  $\Delta P_l^{rel} = \left| \frac{P_l^{calc}}{P_l^{exp}} - 1 \right|$  the relative residuals in pressure resulting from bubble point calculations.

# **3.3.4.** Quantitative Structure Property Relationship (QSPR) for predicting $k_{ij}$

#### Multivariate regression

The QSPR model for predicting  $k_{ij}$  was built in steps: Initially, the QSPR model was developed for the simplest case; for predicting  $k_{ij}$  in mixtures of two non-associating, non-polar components (group 1), using only the descriptor for the asymmetry in the dispersive intermolecular potential  $D^{LJ}$ . Additional groups of binary mixtures were considered progressively and the model was supplemented with the necessary descriptors. In this way, the model was extended to all groups of mixtures with non-associating components (groups 1 to 6). Subsequently, the mixtures of associating components (groups 7 to 10) were considered. The QSPR

model for all groups of binary mixtures reads

$$k_{ij}^{\text{QSPR}} = \sum_{L=1}^{N_d} c_L \cdot D_L \tag{3.19}$$

with model coefficients

$$c_L \in \{c^{\text{LJ}}, c^{\text{dd,a}}, c^{\text{dd,b}}, c^{\text{qq}}, c^{\text{dq}}, c^{\text{assoc,s}}, c^{\text{assoc,c}}, c^{\text{assoc,sc}}\}$$

and with corresponding descriptors  $D_L$ 

$$D_{I} \in \{D^{LJ}, D^{dd,a}, D^{dd,b}, D^{qq}, D^{dq}, D^{assoc,s}, D^{assoc,c}, D^{assoc,sc}\}$$

as introduced in Eq.(3.8) to (3.17). A non-weighted non-linear least squares problem is solved for the regression of the model coefficients  $c_L$ . The objective function for the model regression is defined as the total sum of the squared residuals between the values of  $k_{ij}$  individually adjusted to experimental data  $k_{ij}^{\text{fit}}$  and the values of  $k_{ij}$  calculated from the QSPR model  $k_{ij}^{\text{QSPR}}$  in Eq.(3.19) as

$$\min_{\overline{c}} Q = \sum_{m=1}^{N_{\text{tr}}} \left( k_{ij,m}^{\text{fit}} - k_{ij,m}^{\text{QSPR}} \right)^2$$
(3.20)

with  $N_{\rm tr}$  the number of mixtures used for the regression. The least squares minimization was conducted using the solver *nlinfit* provided in Matlab [69]. For the 95% confidence interval of the model coefficients  $\Delta c_{L,95}$  we use the *t*-distribution with  $N_{\rm tr} - N_d - 1$  degrees of freedom [70]

$$\Delta c_{L,95} = t_{0.95, N_{\rm tr} - N_d - 1} \cdot \sqrt{S^2} \cdot \sqrt{V_{LL}}$$
(3.21)

with  $S^2$  as the estimated model variance

$$S^{2} = \frac{\sum_{m=1}^{N_{\rm tr}} \left( k_{ij,m}^{\rm fit} - k_{ij,m}^{\rm QSPR} \right)^{2}}{N_{\rm tr} - N_{d} - 1}$$
(3.22)

and with  $V_{LL}$  as the corresponding diagonal element of the coefficient covariance matrix.

#### Training and test set

The quality and the morphology of the data sets used to derive and validate the QSPR model coefficients (QSPR database) is decisive. The set used to derive the QSPR model coefficients (training set) should span the whole region of the descriptor space, it should be diverse and it should include data points close to the data points used for the external validation of the model (test set) [71, 72]. In order to ensure these conditions, we define the training and test set respectively in a three-step procedure: In step 1, we *a priori* detect and remove from the QSPR database

the binary mixtures with unreliable  $k_{ij}$  values [70, 73]. In step 2, we divide the QSPR database in training and test set, using a uniform design method for subset selection [74]. In step 3, we iteratively remove the outliers from the training set. The steps are discussed in more detail in the following.

In step 1 we use as measure for the quality of the adjusted  $k_{ij}$  values the value of the objective function *F* in Eq. (3.18), divided by the total number of the experimental data points, according to

$$f = F/n_{\text{exp}} \quad . \tag{3.23}$$

The value of  $k_{ij}$  for a mixture m is considered as unreliable if  $f_m > 0.95 \cdot \max(\overline{f})$  and the absolute average residuals AAD-x and AAD- $P^{rel}$  are higher than 15%. Those cases either correspond to binary mixtures with experimental data of poor quality or to mixtures, where PC-SAFT leads to inaccurate results with the chosen pure component parameters.

After unreliable data were removed, the curated database ( $N_m$  binary mixtures) is divided into the training and the test set in step 2. In our case, we define the split fraction between the training and the test set  $N_{tr}/N_{ts}$  equal to 9 (with  $N_{tr}+N_{ts}=N_m$ ). For the selection of the training set, we have used an in-house implementation of the Kennard and Stone algorithm. The Kennard and Stone (KS) algorithm [75] is a well-established method for uniform design in the field of chemometrics [74]. The selection principle of the algorithm [75] ensures that the points which are excluded (test set) are close to the points of the design set (training set). Here, we implemented the KS algorithm individually for each one of the 10 binary mixture groups ('clusters') defined in Section 3.3. For all groups we used the same fraction of training to test set, as for the complete database  $(N_{tr,group}/N_{ts,group} = 9)$ . Implementing the KS algorithm individually for each group is a way to ensure that all groups are represented in the training set, even if the number of available data per group is limited [76] (e.g. binary mixtures with two non-associating, guadrupolar components). Since the KS algorithm uses the Euclidean norm of the descriptor vector, the results are sensitive to descriptor scaling [77]. For better scaling of the highly irregular multidimensional descriptor space, we used the standardized values of the descriptors [78]

$$\hat{D}_{L,m} = \frac{D_{L,m} - D_L}{S_{DL}}$$
(3.24)

with  $\hat{D}_{L,m}$  the standardized value of descriptor  $D_L$  for mixture m,  $\overline{D}_L$  denotes the average value of descriptor  $D_L$  for all mixtures, and  $S_{DL}$  is the standard deviation of descriptor  $D_L$  for all mixtures of the database. In our implementation, the KS algorithm is initialized on the boundaries of the multidimensional descriptor space. Thus, the designed training set is expected to be sensitive to outliers [76].

We exclude outliers from the training set iteratively in step 3. We fit the model coefficients  $N_m$  times, excluding one mixture  $\beta$  at a time ("Leave-One-Out" proce-

dure), and we calculate the corresponding sum of the residuals  $r_{N_m-1,\beta}$ 

$$r_{N_m - 1,\beta} = \sum_{\substack{m=1\\m \neq \beta}}^{N_m - 1} \left( k_{ij,m}^{\text{fit}} - k_{ij,m}^{\text{QSPR}} \right)^2$$
(3.25)

with  $\beta \in \{1, 2, ..., N_m\}$ . We determine the mean value

$$\bar{r}_{N_m-1} = \frac{1}{N_m} \cdot \sum_{\beta}^{N_m} r_{N_m-1,\beta}$$
(3.26)

and the standardized value of the residual for each mixture  $\beta$  around the mean value  $\overline{r}_{N_m-1}$  as

$$\hat{r}_{N_m-1,\beta} = \frac{r_{N_m-1,\beta} - \bar{r}_{N_m-1}}{S_r}$$
(3.27)

where  $S_r$  is the standard deviation of the residuals. Mixtures that led to  $\hat{r}_{N_m-1,\beta}$  values greater than three standard deviation units  $(3S_r)$  were considered as outliers and were excluded. [70, 71, 79]

#### Model validation

Model validation is an integral part of any QSPR method. On the one hand, the goodness-of-fit, the robustness of the model and its internal predictive power are measured by internal validation techniques. On the other hand, the actual predictive power of the model is evaluated by external validation. External validation is defined through data that was not used for the model regression [72].

The goodness-of-fit is measured by the coefficient of multiple determination  $R^2$ . The coefficient of multiple determination estimates the portion of the variation in the independent variable (here  $k_{ij}^{\text{fit}}$ ) that is explained by the regression [72, 73, 79].  $R^2$  is calculated over all mixtures of the training set ( $N_{\text{tr}}$ ) and is defined as

$$R^{2} = 1 - \frac{\sum_{m=1}^{N_{\text{tr}}} \left( k_{ij,m}^{\text{fit}} - k_{ij,m}^{\text{QSPR}} \right)^{2}}{\sum_{m=1}^{N_{\text{tr}}} \left( k_{ij,m}^{\text{fit}} - \overline{k}_{ij}^{\text{fit}} \right)^{2}}$$
(3.28)

where  $\overline{k}_{ij}^{\text{fit}}$  is the average value of  $k_{ij}^{\text{fit}}$  for all mixtures of the training set. A QSPR model with  $R^2$  higher than 0.6 can be considered predictive [73]. However, Tropsha [73] also points out, that the predictive power of a QSPR model needs to be further evaluated for compounds that were not included in the training set.

The Leave-One-Out (LOO) cross-validated correlation coefficient  $Q_{LOO}^2$  and the Leave-Many-Out (LMO) cross-validated correlation coefficient  $Q_{LMO}^2$  measure the robustness of the model and its internal predictive power. The cross-validated correlation coefficients should be calculated over a large number of trials. In both the

LOO and LMO procedures, a certain subset of the training set is omitted at each trial.

For the calculation of the LOO cross-validated correlation coefficient  $Q_{LOO}^2$  the number of trials is equal to the total number of mixtures in the QSPR database  $N_m$ . At each trial a mixture is individually omitted. The QSPR model coefficients are regressed using the remaining  $N_m - 1$  mixtures as training set. Using this regression, one can now predict the  $k_{ij}$  value ( $k_{ij}^{QSPR/-m}$ ) for mixture m (which was temporarily excluded from the training set). The definition of  $Q_{LOO}^2$  according to the guidlines of the Organization of Economic Co-operation and Development (OECD) [72] is

$$Q_{\text{LOO}}^{2} = 1 - \frac{\sum_{m=1}^{N_{m}} \left( k_{ij,m}^{\text{fit}} - k_{ij,m}^{QSPR/-m} \right)^{2}}{\sum_{m=1}^{N_{m}} \left( k_{ij,m}^{\text{fit}} - \overline{k}_{ij}^{\text{fit}} \right)^{2}} \quad .$$
(3.29)

At each trial of the LMO procedure, more mixtures than one are simultaneously excluded. Here, we have calculated the value of  $Q_{\rm LMO}^2$  over  $2N_m$  number of trials. At each trial, 50% of the complete database was excluded [71] ( $N_{\rm LMO} = 0.5N_m$ ). The value of the LMO cross-validated correlation coefficient for each trial  $Q_{LMO/50,trial}^2$  is calculated as

$$Q_{LMO/50,trial}^{2} = 1 - \frac{\sum_{m=1}^{N_{LMO}} \left(k_{ij,m}^{\text{fit}} - k_{ij,m}^{QSPR/-m}\right)^{2}}{\sum_{m=1}^{N_{m}} \left(k_{ij,m}^{\text{fit}} - \overline{k}_{ij}^{\text{fit}}\right)^{2}}$$
(3.30)

with  $k_{ij,m}^{QSPR/-m}$  representing the predicted  $k_{ij}$  value for each mixture m that is part of the excluded set. The standard deviation and the average value of  $Q_{LMO/50,trial}^2$ over all trials are used as indicators of the robustness in the model prediction. A robust model should remain invariant to changes of the training set and it is thus expected to exhibit small difference between the average value of  $Q_{LMO}^2$  and  $R^2$ . [80] We should note that the LMO procedure demands to generate as many different training sets as the number of trials. The Kennard and Stone algorithm described in Section 3.4.2 is initialized on a fixed point of the descriptor space and therefore provides a single design for the training set. Thus, for the calculation of  $Q_{LMO}^2$ , we used a straightforward random selection of the training set.

An important indicator of the actual predictive capability of the model is the external explained variance  $Q_{ext}^2$ . The external explained variance is a measure for the quality of prediction for data that were not included in the set used for the model development. There are several approaches in the literature for the calculation of  $Q_{ext}^2$  [71, 72, 81, 82]. In our implementation, the training set is much larger than the test set. In this case, the definition of Consonni et al. [81] is appropriate, with

$$Q_{ext}^{2} = 1 - \frac{\left[\sum_{m=1}^{N_{ts}} \left(k_{ij,m}^{\text{fit}} - k_{ij,m}^{\text{QSPR}}\right)^{2}\right] / N_{ts}}{\left[\sum_{m=1}^{N_{tr}} \left(k_{ij,m}^{\text{fit}} - \overline{k}_{ij}^{\text{fit}}\right)^{2}\right] / N_{tr}} \quad .$$
(3.31)

The numerator in Eq.(3.31) sums over data of the test set, whereas the denominator sums over the training set.

#### 3.4. Results

## **3.4.1.** Estimation of $k_{ij}$ based on London's dispersive theory for mixtures

Calculating  $k_{ij}$  values from London's dispersive theory, according to Eq.(3.5), requires segment diameters  $\sigma_i$  and  $\sigma_j$  and the ionization potentials  $I_i$  and  $I_j$ . Experimental values of the ionization potentials were taken from the literature [83]. We limit consideration to mixtures of two non-polar, non-associating components (group 1). Figure 3.1 compares the values of  $k_{ij}$  calculated with Eq.(3.5) to the values of  $k_{ij}$  individually adjusted on experimental data. A detailed list of the examined binary mixtures with the corresponding values of  $k_{ij}(\sigma, I)$  and  $k_{ij}^{fit}$  is given in Table E.1 in Appendix E.

 $k_{ij}$  calculated with Eq.(3.5) cannot take on negative values. For mixtures of non-polar, non-associating components this limitation is not strongly restricting the results, because the negative  $k_{ij}^{\text{fit}}$  values are all fairly close to zero. Figure 3.2 shows that for the mixtures of group 1 with negative values of  $k_{ij}^{\text{fit}}$  (mixtures # 1,9,15,19,26,30,34,44,45) the results of phase equilibrium calculations remain good for calculations with the slightly positive  $k_{ij}$  values from Eq.(3.5). Mixtures with polar and associating components, though, often demand more negative  $k_{ij}$  values. In this case, the predictions of  $k_{ij}$  with Eq.(3.5) are expected to lead to more significant errors.

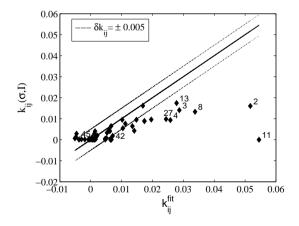


Figure 3.1: Comparison of  $k_{ij}(\sigma, I)$  values estimated from the London's dispersive theory (Eq. (3.5)) to  $k_{ij}^{\text{fit}}$  values individually adjusted to experimental data for mixtures of two non-polar, non-associating components (group 1). The dashed lines illustrate the absolute deviations of  $\pm 0.005$  for the value of  $k_{ij}^{\text{fit}}$ .

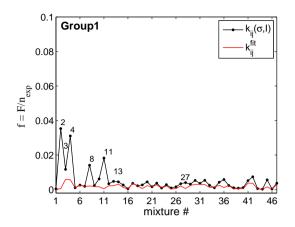


Figure 3.2: Deviations of PC-SAFT EoS from experimental binary phase equilibrium data of two nonassociating, non-polar components (group 1). The deviations are defined as  $f = F/n_{exp}$  according to Eq.(3.23). The red line serves as a reference and is obtained for individually optimized  $k_{ij}^{fit}$  values. The symbols (connected by black line) are obtained using estimated values  $k_{ij}(\sigma, I)$ . For hexadecane no ionization potential  $\sigma$  was available, which is why  $k_{ij}(\sigma, I)$  was set to zero for mixtures #12 and #43.

Higher deviations in the prediction of  $k_{ij}$  are observed for binary mixtures including carbon monoxide (mixtures 2, 3 and 4 in Figures 3.1 and 3.2) and for binary mixtures including methane (mixtures 8, 13 and 27). These mixtures demand higher values of  $k_{ij}$  for an adequate description. We conjecture that in those cases,  $k_{ij}$  does not only correct the dispersive intermolecular potential of the mixture but compensates other model deficiencies. Below we show that a QSPR model based on semi-empirical descriptors takes the necessary contributions into account to model the value of  $k_{ij}$  for these mixtures.

# **3.4.2.** QSPR estimation of $k_{ij}$ - Model regression and assessment of the results

The descriptors of the QSPR model for the estimation of  $k_{ij}$  values were constructed using the PC-SAFT molecular parameters. The initial structure of the descriptors was defined in an ad hoc manner and their exact structure was adjusted empirically, by varying exponents, as described in Section 3.1. In the course of this process, different sets of descriptors were generated. For each set of descriptors, the coefficients of the QSPR model were regressed as described in Section 3.4.1. The performance of each QSPR model was evaluated using the internal and external validation techniques described in Section 3.4.3. The training and the test set remained unchanged. The QSPR model that achieved the best overall description for all groups of mixtures based on the value of  $R^2$  has been obtained with the descriptors defined in Eq.(3.8) to (3.17). Here, we limit our discussion to the results of this model.

Mixtures with associating components are the most difficult to describe. For the

regression of the model coefficients, we therefore distinguish two cases: In the first case, we estimate the model coefficients only for mixtures of non-associating components ("1<sup>st</sup> regression case": groups 1 to 6). In the second case, we adjust the model only to mixtures containing associating components ("2<sup>nd</sup> regression case": groups 7 to 10).

In the first case, the database of mixtures with only non-associating components includes 199 binary mixtures. Unreliable data and outliers have been removed according to the rationale described in Section 3.4.2. Then, the training set consists of 151 and the test set of 22 binary mixtures. The adjusted model coefficients  $c_L$  along with the values of their 95% confidence intervals  $\Delta c_{L,95}$  are given in Table 3.2. For all regressed model coefficients we observed  $|\Delta c_{L,95}| << |c_L|$ , which qualifies a stable regression model [84]. For mixtures of groups 1 to 6 the values of  $k_{ij}$  predicted with the QSPR model are given in Appendix E (Tables E.3 to E.8). In

Table 3.2: Results of the regressed model coefficients for mixtures of non-associating components (groups 1 to 6). The values of the coefficients  $c_L$  and their 95% confidence interval  $\Delta c_{L,95}$  for the QSPR model defined in Eq.(3.19) and (3.21), with  $c^{\text{assoc,s}} = 0$ ,  $c^{\text{assoc,c}} = 0$  and  $c^{\text{assoc,sc}} = 0$ .

	mixtures with					
non	non-associating components					
	$c_L \cdot 10^4 \qquad \Delta c_{L,95} \cdot 10^4$					
$c^{LJ}$	-103.285	$\pm 0.065$				
$c^{\mathrm{dd,a}}$	57.533	$\pm 0.235$				
$c^{dd,b}$	-25.064	$\pm 0.095$				
cqq	0.114	$\pm 0.001$				
$c^{dq}$	-0.645	$\pm 0.002$				

the second case, for associating mixtures the database includes 253 mixtures with at least one associating component. After unreliable data and outliers have been removed, the training set consists of 167 and the test set of 23 binary mixtures. The adjusted model coefficients  $c_L$  for mixtures with at least one associating component and their 95% confidence intervals  $\Delta c_{L,95}$  are given in Table 3.3. For this "2<sup>nd</sup> regression case" we also find  $|\Delta c_{L95}| \ll |c_L|$ . The regression model for mixtures of the groups 7 to 10 can therefore be characterized stable as well. For mixtures of groups 7 to 10 the predicted values of  $k_{ii}$  are given in Appendix E (Tables E.9 to E.12). The multiple correlation coefficient  $R^2$  for the QSPR model adjusted to mixtures of non-associating components is 88.4%. For the OSPR model adjusted to mixtures of associating components  $R^2$  is 70.1%. In both cases, the model can, in the jargon of QSPR methods, be considered to be predictive. Figure 3.3 shows the values of the multiple correlation coefficient  $(R_{aroup}^2)$  calculated individually for each group of binary mixtures. Values of  $R_{group}^2$  have been calculated using Eq.(3.20), with the summation running over all mixtures of the training set for each particular group. The results of the internal and external validation of the QSPR model for both regression cases are summarized in Table 3.4.

Table 3.3: Results of the regressed model coefficients for mixtures with at least one associating component (groups 7 to 10). The values of the coefficients  $c_L$  and their 95% confidence interval  $\Delta c_{L,95}$  for the QSPR model defined in Eq.(3.19) and (3.21).

mixtures with					
associating components					
$c_L \cdot 10^4  \Delta c_{L,95} \cdot 10^4$					
c <sup>LJ</sup>	-149.236	$\pm 0.591$			
$c^{dd,a}$	20.178	$\pm 0.841$			
$c^{dd,b}$	-23.180	$\pm 0.210$			
cqq	-0.428	$\pm 0.006$			
$c^{dq}$	0.089	$\pm 0.006$			
$c^{assoc,s}$	-12.432	$\pm 0.062$			
$c^{\text{assoc,c}}$	-4.797	$\pm 0.018$			
$c^{\text{assoc,sc}}$	0.592	$\pm 0.006$			

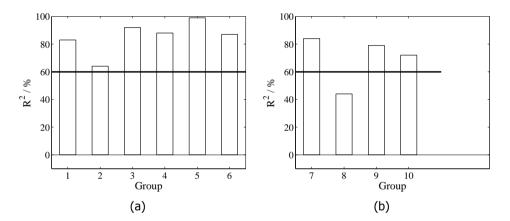


Figure 3.3: Coefficient of multiple determination  $R^2$  for: (a) mixtures of two non-associating components (groups 1 to 6) and (b) mixtures including at least one associating component (groups 7 to 10).

The QSPR model adjusted to mixtures of non-associating components describes all types of non-associating mixtures reasonably well. The results are satisfactory, especially considering the diversity of mixtures in our database. The value of the LOO cross-validated coefficient  $Q_{LOO}^2$  and the average value of the LMO cross-validated coefficient  $\hat{Q}_{LMO/50}^2$  (Table 3.4) are close to the value of  $R^2$ . The proposed model for mixtures with non-associating, polar or non-polar components can be thus characterized as sufficiently robust [80]. Further, the low standard-deviation of  $Q_{LMO/50}^2$  (5.4%) over 346 trials indicates that the model is robust against strong variations of the training set.

For the model adjusted to mixtures of associating components ("2<sup>nd</sup> regression

mixtures with					
	non-associating components				
$R^{2}(\%)$	$R^{2}(\%) = Q^{2}_{LOO}(\%) = \hat{Q}^{2}_{LMO/50}(\%) = Q^{2}_{ext}(\%)$				
88.4	86.5	84.5	92.4		
	mixtures with				
	associating components				
$R^{2}(\%)$	$Q_{LOO}^{2}(\%)$	$\hat{Q}^2_{LMO/50}(\%)$	$Q_{ext}^{2}(\%)$		
70.1	64.3	57.9	82.3		

Table 3.4: Results of internal and external validation of the QSPR model (Eq.(3.19)) developed for mixtures of non-associating and mixtures of associating components.

case") the coefficients of multiple determination  $R_{\text{group}}^2$  (explained variance) for the individual groups are also high, particularly for the groups 7, 9 and 10. Group 8 contains mixtures of species with widely differing pure component parameters which we call asymmetry. To properly and transferably account for this asymmetry in the resulting  $k_{ij}$  values was only partially successful in our QSPR approach. We note that mixtures of group 8 represent 34% of the training set used for the adjustment of the QSPR model coefficients in the "2<sup>nd</sup> regression case". When mixtures of group 8 are omitted during the Leave-One-Out (LOO) or Leave-Many-Out (LMO) validation tests, the QSPR model demonstrates a much better overall performance in terms of the  $Q_{\text{LOO}}^2$  and  $\hat{Q}_{\text{LMO}/50}^2$  QSPR validation measures. The model adjusted to mixtures of associating components is more uncertain than the QSPR model for mixtures of non-associating components. The choice of the training set acts on the result. This is reflected directly in a) the high standard deviation of the  $Q_{\text{LMO}/50}^2$ coefficient over 380 trials (22.6%) and b) the higher difference between the value of  $R^2$  and the values of the cross validated coefficients  $\hat{Q}_{\text{LMO}/50}^2$  and  $Q_{\text{LOO}}^2$  (Table 3.4).

The external explained variance  $Q_{\text{ext}}^2$  by the QSPR model adjusted to mixtures of non-associating components is 92%. For the QSPR model adjusted to mixtures of associating components  $Q_{\text{ext}}^2$  is 82%. The high values of  $Q_{\text{ext}}^2$  indicate the high predictive power of the QSPR model in both cases. Nevertheless, the results of  $Q_{\text{ext}}^2$ should be interpreted cautiously. One should bear in mind that the size of the test set is much smaller and less diverse than the size of the training set ( $N_{\text{tr}}/N_{\text{ts}} = 9$ ).

Generally, the proposed QSPR model is stable and robust and has (in the sense of a QSPR method) a good predictive capacity. The statistical measures (Table 3.4) indicate that the QSPR model predicts  $k_{ij}$  values in binary mixtures of non-associating components with sufficient accuracy. For mixtures of associating components, the model is also reliable (in the jargon of QSPR). However, the estimations of  $k_{ij}$  for mixtures containing one dipolar, non-associating component and one associating component are more uncertain and should be used with reservation.

#### **3.4.3.** Evaluating phase equilibria with predicted $k_{ij}$ values

The  $k_{ij}$  values used for the regression of the QSPR model ( $k_{ij}^{\text{fit}}$ ) are not experimental data, but parameters fitted to experimental data. We therefore find it important to evaluate the QSPR model beyond just the statistical measures of the QSPR method. We have examined the results of phase equilibrium calculations with the predicted  $k_{ij}$  values for each group of mixtures. The parity plots and the diagrams that show the results in phase equilibrium calculations for all groups of mixtures are given in Appendix E (Figures E.1 to E.4).

Here, we discuss in more detail the results for mixtures of group 4 (mixtures of one non-associating, quadrupolar and one non-associating, dipolar component). We find the performance for mixtures of group 4 representative of the overall performance of the QSPR predictions of  $k_{ij}$  for non-associating mixtures ( $R_{group 4}^2 = 88.1\% \simeq R^2$ ). Moreover, the prediction for mixtures of group 4 is of practical interest, for example by the application of CAMD for polar solvents, for the CO<sub>2</sub> capture with physical absorption [18].

Figure 3.4 compares the estimated values,  $k_{ij}^{\text{QSPR}}$ , to the reference values,  $k_{ij}^{\text{fit}}$ , for group 4. Further, Figure 3.5 illustrates the accuracy in phase equilibrium calculations with PC-SAFT for the mixtures of group 4 with  $k_{ij}$  values estimated with the QSPR model adjusted to non-associating mixtures (Table 3.2). The results in phase equilibrium calculations are compared to experimental VLE data. We consider the same experimental data that were used for the individual fitting of  $k_{ij}$  values. We assess the results using the average value f of the combined residuals in the liquid mole fraction and the pressure, over the number of experimental data points for each mixture as defined in Eq.(3.23). In Figure 3.5, we also present the results in phase equilibrium calculations, when no correction is used for the PC-SAFT EoS ( $k_{ij} = 0$ ), as well as the results achieved when  $k_{ij}$  is individually adjusted to the experimental data, namely  $f(k_{ij}^{\text{fit}})$ . We observe that for the majority of the mixtures in group 4 (in both the training and the test set) phase equilibrium calculations with the QSPR estimations of  $k_{ij}$  give lower residuals than if no correction is used ( $k_{ij} = 0$ ).

It is however difficult to quantify the relationship between the error in  $k_{ij}$  prediction  $\Delta k_{ij} = |k_{ij}^{\text{fit}} - k_{ij}^{\text{QSPR}}|$  and the subsequent error in phase equilibrium calculations  $\Delta f = |f(k_{ij}^{\text{fit}}) - f(k_{ij}^{\text{QSPR}})|$ . For different mixtures, the sensitivity of the objective function *F* (and thereby *f*) to the value of  $k_{ij}$  is different, depending on different factors, like azeotropy or supercritical regions. Let us, for example, examine the performance of the  $k_{ij}$  prediction and phase equilibrium calculations for mixture #4 (carbon dioxide - 1-bromobenzene) compared to mixture #20 (1-hexene - ethylene). For mixture #4, the error in the estimation of  $k_{ij}$  is much higher than the error in the estimation of  $k_{ij}$  for mixture #20 (Figure 3.4, Table S5). Still, the error in phase equilibrium calculations is almost identical for both mixtures (Figure 3.5).

Finally, the  $k_{ij}$  values estimated from London's dispersive theory  $k_{ij}(\sigma, I)$  (Eq.(3.5)) were used in phase equilibrium calculations for the mixtures of group 4. A list of the estimated values  $k_{ij}(\sigma, I)$  is given in Table E.2 in Appendix E. In Figure 3.6, phase equilibrium calculations carried out with the estimated values  $k_{ij}^{\text{QSPR}}$  are com-

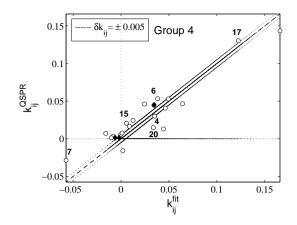


Figure 3.4: Comparison of the estimated  $k_{ij}^{\text{QSPR}}$  values with  $k_{ij}^{\text{fit}}$  values individually adjusted to experimental data for mixtures of one non-associating, dipolar and one non-associating, quadrupolar component (group 4). Open symbols indicate mixtures of the training set, whereas solid symbols correspond to the mixtures of the test set. The dashed lines illustrate the absolute deviations of  $\pm 0.005$  for the value of  $(k_{ij}^{\text{fit}})$ .

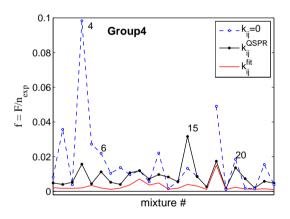


Figure 3.5: Deviations of PC-SAFT from experimental binary phase equilibrium data of one nonassociating, dipolar and one non-associating, quadrupolar component (group 4). The deviations are defined as  $f = F/n_{exp}$  according to Eq.(3.23). The red line serves as a reference and is obtained for individually optimized  $k_{ij}^{fit}$  values. The symbols (connected by black line) are obtained using estimated values  $k_{ij}^{QSPR}$ . The blue dashed line represent phase equilibrium calculations, when the PC-SAFT EoS is not corrected ( $k_{ij} = 0$ ).

pared to phase equilibrium calculations with the estimated values from London's dispersive theory  $k_{ij}(\sigma, I)$ . The results obtained with the estimated value  $k_{ij}^{\text{QSPR}}$  are

in most cases better than the results obtained with  $k_{ij}(\sigma, I)$ . For example, mixture #7 (dimethyl ether-carbon dioxide) requires a negative  $k_{ij}$  value. Negative  $k_{ij}$  values cannot be calculated using Eq.(3.5). As discussed in Section 4.1, this limitation has a higher impact on mixtures containing polar components. For mixture #7, the estimated  $k_{ij}^{\text{QSPR}}$  is negative. With  $k_{ij}^{\text{QSPR}}$ , the PC-SAFT EoS is corrected and phase equilibrium calculations are considerably better. Moreover, for mixtures that require high positive  $k_{ij}$  values, the predicted value  $k_{ij}^{\text{QSPR}}$  leads to significantly lower residuals in the phase equilibrium calculations. Representative examples are mixture #2 (nitrogen-propylbenzene) and mixture #17 (nitrogen-toluene). The

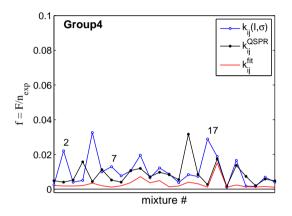


Figure 3.6: Deviations of PC-SAFT from experimental binary phase equilibrium data of one nonassociating, dipolar and one non-associating, quadrupolar component (group 4). The deviations are defined as  $f = F/n_{exp}$  according to Eq.(3.23). The red line serves as a reference and is obtained for individually optimized  $k_{ij}^{fit}$  values. The black line represents phase equilibrium calculations, when the PC-SAFT EoS is corrected with  $k_{ij}^{QSPR}$ . The blue solid line is for results using  $k_{ij}(\sigma, I)$  from London's dispersive theory.

 $k_{ij}$  values predicted by the proposed QSPR model (with the descriptors defined in Eq.(3.8) to (3.17) and the regressed coefficients given in Tables 3.2 and 3.3) are used in phase equilibrium calculations for all mixtures considered in our QSPR database. In Figure 3.7, a general overview is given of the improvement potential in phase equilibrium calculations, using the  $k_{ij}$  values estimated with the proposed QSPR model. For each group of mixtures, Figure 3.7 displays the percentage of cases in which phase equilibrium calculations are more accurate with the estimated value  $k_{ij}^{\text{QSPR}}$ . The percentage of cases when phase equilibrium calculations with  $k_{ij} = 0$  are more accurate and the percentage of cases when phase equilibrium calculations are equally good for  $k_{ij}^{\text{QSPR}}$  and  $k_{ij} = 0$  are given as well. For all groups of mixtures (associating and non-associating) the proposed QSPR model provides  $k_{ij}$  estimates that generally improve the accuracy of PC-SAFT in phase equilibrium calculations. According to Figure 3.7, the most significant improvement is achieved for mixtures of group 5. However, the small size of group 5 (Table 3.1) and its'

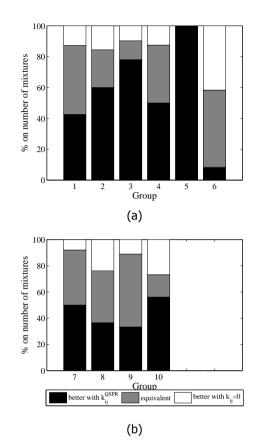


Figure 3.7: Assessing phase equilibrium calculations: Black surface represents the percentage of cases for which calculations with estimated  $k_{ij}^{\text{QSPR}}$  values are more accurate than with  $k_{ij} = 0$ . The gray shaded area represents the percentage of cases when both cases are equivalent.

limited diversity (Table E.7) do not allow us to draw a generalized conclusion about the performance of the method for mixtures of two non-associating, quadrupolar components. Further, in the group with the least improvement, for mixtures of two dipolar, non-associating components (group 6), the individually adjusted  $k_{ij}$  values are close to zero (see Appendix E). Calculation results for  $k_{ij} = 0$  are thus close to optimal, so that the use of estimated  $k_{ij}^{QSPR}$  cannot lead to significant improvements for group 6.

## 3.5. Conclusions

We developed and analyzed a multivariate regression model for the estimation of the binary interaction parameter  $k_{ij}$  of the PC-SAFT EoS using a QSPR method. The descriptors of the regression model are based on the pure component parameters of

the PC-SAFT model. The regression models were developed separately for mixtures with non-associating components and for mixtures with at least one associating component.

For mixtures with non-associating components, values of  $k_{ij}$  were also estimated from London's dispersive theory, using the expression of Hudson and Mc-Coubrey [50]. Values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{\text{QSPR}}$ ) and values of  $k_{ij}$  estimated from London's dispersive theory ( $k_{ij}(\sigma, I)$ ) were compared to values of  $k_{ij}$  individually fitted on experimental data. For mixtures containing non-associating, polar components the QSPR regression model allows for negative values of  $k_{ij}$  and leads to more accurate predictions than the expression of Hudson and McCoubrey. The QSPR regression model considers additional contributions to the value of  $k_{ij}$  than just the asymmetry in the dispersive intermolecular forces.

The coefficient of multiple determination  $R^2$  of the QSPR regression model for mixtures with non-associating components is 88.4%. For mixtures with at least one associating component  $R^2$  is 70.1%. Thus, for both regression cases the QSPR model can, in the jargon of QSPR methods, be characterized as stable and robust and with good predictive capacity.

The  $k_{ij}$  values estimated as function of the pure component PC-SAFT parameters, with the proposed QSPR regression model, can be used to enhance the accuracy of phase equilibrium calculations with PC-SAFT. With the proposed QSPR model for the estimation of  $k_{ij}$ , no prior knowledge of the real behavior of the examined binary mixture is demanded. The QSPR approach can be implemented in a CAMD framework that uses the pure component parameters of the optimized fluid directly as optimization variables. In that case, we expect that phase equilibrium calculations and thus the accuracy of CAMD results can be enhanced.

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# 4

CoMT-CAMD for CO<sub>2</sub>-Absorption: The Impact of Binary Interaction Parameters Predictions

The CoMT-CAMD approach relies on the predictive capabilities of the chosen thermodynamic model. Separation processes, in particular, require the estimation of mixture properties. Predictions of mixture phase equilibria or other properties that require a sufficiently accurate representation of excess properties are particularly demanding for thermodynamic models. This Chapter investigates how two modeling approaches for the PC-SAFT equation of state impact the resulting list of the proposed solvents for the  $CO_2$ -capture process. The two models are:

- 1. PC-SAFT, applied with  $k_{ij}$ =0 for all pairs of substances involving the target solvent
- 2. PC-SAFT, applied with the QSPR-relation for  $k_{ij}$  developed in Chapter 3 for pairs of substances involving the hypothetical target solvent

Both modeling approaches are assessed by comparison to results obtained with individually optimized  $k_{ij}$ -parameters and with fully optimized process settings.

## 4.1. Case study: Process and problem description

The examined case study preserves the topology of the pre-combustion  $CO_2$  capture process described in Chapter 2 (Figure 2.3, Appendix B.1). The process specifications are given in Table 4.1 and differ slightly from Chapter 2. The efficiency of the pump for lean solvent recirculation has been changed according to ref. [1]. Besides, the compressor is now modeled with 3 compression stages for the ( $CO_2$ -rich) vapor stream exiting the desorption flash to the pipeline pressure ( $N_{comp-des} = 3$ ). A 3-staged compression is a more realistic design option, leading to adequate compression ratios r [1], in the range between 2.9 and 4.8<sup>1</sup>.

The simultaneous process and solvent optimization problem is formulated as in problem (2.2), for the cost objective function described in Chapter 2 and Appendix B.2. In the current chapter, only the case of polar solvents was examined. The implementation of CoMT-CAMD to polar solvents is a more demanding problem than the implementation to non-polar solvents due to the additional degree of freedom of dipole moment. In order to examine the limits of the proposed implementation of  $k_{ij}$ -predictions, the problem of simultaneous process and polar solvent optimization is therefore seen as a more suitable case-study.

The degrees of freedom are the process variables  $\overline{x} = \{P^{\text{des}}, P^{\text{rg}}, T^{\text{lean}}\}$  and the molecular parameters of the solvent  $\overline{p} = \{m, \sigma, \varepsilon/k, \mu/(m\sigma^3(\varepsilon/k))^{0.5}\}$ . The lower and upper bounds of the variables during optimization remain also unchanged. The database of candidate solvents used in the mapping step is the database of polar, non-associating organic components (Appendix C), same as for the problem described in Chapter 2.

Residual caloric properties and phase equilibria are calculated with the PC-SAFT EoS. The ideal gas heat capacity  $c_p^{ig}$  and the molar mass M of the solvent are estimated with QSPR models, as functions of the PC-SAFT pure component parameters. Binary interaction parameters  $k_{ij}$  for mixtures of the optimized solvent with CO<sub>2</sub> and H<sub>2</sub> either are predicted using QSPR models (Chapter 3), or  $k_{ij}$  is set to zero for these binary pairs. The CoMT-CAMD results are compared. The  $k_{ij}$  values for the binary mixtures CO<sub>2</sub> - H<sub>2</sub>O, CO<sub>2</sub> - H<sub>2</sub> and H<sub>2</sub> - H<sub>2</sub>O were adjusted to experimental mixture data. The PC-SAFT pure component parameters for CO<sub>2</sub>, H<sub>2</sub> and H<sub>2</sub>O and the  $k_{ij}$  values of their binary mixtures used in this case study<sup>2</sup> are given in Tables 4.2 and 4.3.

$${}^{1}r_{lb} = \left(\frac{P^{\text{ppl}}}{P_{lb}^{\text{des}}}\right)^{\left(1/N_{\text{comp-des}}\right)} \text{ and } r_{ub} = \left(\frac{P^{\text{ppl}}}{P_{ub}^{\text{des}}}\right)^{\left(1/N_{\text{comp-des}}\right)} \text{ with } P_{lb}^{\text{des}} = 0.1013 \text{ MPa and } P_{ub}^{\text{des}} = 0.4500 \text{ MPa.}$$

<sup>&</sup>lt;sup>2</sup> The PC-SAFT pure component parameters for  $CO_2$  and  $H_2$  are the same with those used in Chapter 2. The PC-SAFT pure component parameters for  $H_2O$  are slightly different, since the dipole moment of  $H_2O$  is additionally considered. The  $k_{ij}$  values for the binary mixtures of  $CO_2$ ,  $H_2$  and  $H_2O$  were adjusted to a higher number of experimental data and using the PC-SAFT pure component parameters given in Table 4.2.

Table 4.1: Stream, process and equipment specifications adopted from the Buggenum pilot plant [2]. The pipeline pressure is taken from ref. [3]; efficiencies from ref. ([4]); the efficiency of the lean solvent pump and the number of compression stages for the pipeline compressor estimated according to ref. [1].

Stream specifications		
	x <sup>sg</sup> <sub>H2</sub> / <sup>mol</sup> /mol	0.5480
Syngas feed composition	x <sup>sg</sup> <sub>CO2</sub> / <sup>mol</sup> /mol	0.4485
	x <sup>sg</sup> <sub>H2O</sub> / <sup>mol</sup> /mol	0.0035
Syngas feed temperature	T <sup>sg</sup> / K	313.00
Rich gas recycle temperature	T <sub>rg</sub> / K	313.00
Pipeline gas temperature	T <sup>ppl</sup> / K	313.00
Pipeline gas pressure	P <sup>ppl</sup> / MPa	11.00
Solvent make-up temperature	Т <sup>МU</sup> / К	298.15
Solvent make-up pressure	P <sup>MU</sup> / MPa	0.1013
Process specifications		
CO <sub>2</sub> capture rate in absorber	α <sub>CO2</sub> / –	0.90
Absorption pressure	P <sub>abs</sub> / MPa	2.00
Equipment specifications		
Absorber - number of stages	N <sub>abs</sub> / -	7
Rich gas compressor - number of stages	N <sub>comp-rg</sub> / -	1
Pipeline compressor - number of stages	N <sub>comp-des</sub> / -	3
Compressors - efficiency	η <sub>comp</sub> / –	0.82
Solvent recirculating pump - efficiency	η <sub>pump</sub> / –	0.90
Auxiliary pumps - efficiency	η <sub>aux.pump</sub> / –	0.75

Substance	М	т	σ	ε/k	μ	Q	$\kappa^{AB}$	$\varepsilon^{AB}/k$	Ref.
	$g \cdot mol^{-1}$	-	Å	К	D	DÅ	-	К	
C0 <sub>2</sub>	44.01	1.5131	3.1869	163.33	-	4.4	-	-	[5]
H <sub>2</sub>	2.016	1.0000	2.9280	37.00	-	-	-	-	[6]
H <sub>2</sub> O	18.02	1.3886	2.7139	339.14	1.85	-	0.03	1687.1	this work

Table 4.2: PC-SAFT pure component parameters for CO<sub>2</sub>, H<sub>2</sub> and H<sub>2</sub>O used in the current study.

Table 4.3: Binary interaction parameters  $k_{ij}$  for the mixtures CO<sub>2</sub>-H<sub>2</sub>O, CO<sub>2</sub>-H<sub>2</sub> and H<sub>2</sub>-H<sub>2</sub>O adjusted to experimental VLE data.

Binary mixture	k <sub>ij</sub>	$%AAD(x^L)$	$\%AAD(x^V)$	Temp. range	Number of experimental data points	Ref.
CO <sub>2</sub> -H <sub>2</sub> O	-0.0766	0.16	0.70	323 K – 473 K	56	[7-10]
CO <sub>2</sub> -H <sub>2</sub>	-0.0623	1.45	2.23	225 K – 280 K	92	[11-13]
H <sub>2</sub> -H <sub>2</sub> O	-0.3945	0.09	-	273 K – 373 K	40	[14, 15]

# **4.2.** Prediction of $k_{ij}$ values for the solvent binary mixtures

Values of the binary interaction parameter  $k_{ij}$  for mixtures of the optimized solvent with CO<sub>2</sub> and H<sub>2</sub> are estimated using the descriptors of the QSPR model presented in Eq.(3.6) to (3.17) (Chapter 3). The limited accuracy of the QSPR model in the prediction of  $k_{ij}$  values for binary mixtures of one non-associating, dipolar and one associating component has been taken into consideration. Therefore, the values of  $k_{ij}$  for the binary mixtures of polar solvents with H<sub>2</sub>O have been set equal to zero (no correction is implemented).

The QSPR model presented in Chapter 3 leads, generally, to satisfactory correlations of  $k_{ij}$  and better predictions of phase equilibria with PC-SAFT. Nevertheless, the training set of the QSPR method presented in Chapter 3 does not include mixtures with H<sub>2</sub>. Binary mixtures with H<sub>2</sub> require unusual  $k_{ij}$ -values and mixtures with H<sub>2</sub> were deliberately excluded from the training set in Chapter 3. Here, values of  $k_{ij}$  for mixtures of the solvent with H<sub>2</sub> are estimated using the descriptors of the QSPR model presented in Chapter 3 (Eq.(3.6) to (3.17)), with coefficients adjusted only for binary mixtures containing H<sub>2</sub>. The training set and the corresponding coefficients of the QSPR model for the estimation of  $k_{ij}$  values for binary mixtures with H<sub>2</sub> are given in Appendix E.4. Additionally, the training set for binary mixtures with one non-associating, dipolar and one non-associating, quadrupolar component was extended here to include additional mixtures with  $CO_2$ . In order to provide more accurate predictions of  $k_{ij}$  for mixtures including  $CO_2$ , the QSPR model coefficients were adjusted individually for this group. The new model coefficients and the extended training set are given in Appendix E.5. The performance of both QSPR models, evaluated using the internal and external validation techniques of the QSPR method, is given in Table 4.4.

With multiple correlation coefficients  $R^2 \ge 80\%$ , both models can be considered to be predictive. The high values of  $Q_{\text{ext}}^2$  indicate high predictive power of the QSPR models. (For a more detailed discussion on the meaning of the QSPR-measures for internal and external model validation see Chapter 3).

Table 4.4: Results of internal and external validation of the QSPR models (Eq.(3.19)) with coefficients adjusted for binary mixtures with  $H_2$  and  $CO_2$  (Appendix E.4 and E.5).

k <sub>ij</sub> QSPR model	$R^{2}(\%)$	$Q_{\rm ext}^2(\%)$
mixtures with $H_2$	83.9	88.3
mixtures with $\rm CO_2$	79.5	99.2

## **4.3.** CoMT-CAMD results

The PC-SAFT parameters of the optimal (hypothetical) polar solvent  $\overline{p}^{opt}$  at optimal process conditions  $\overline{x}^{opt}$  are calculated in the CoMT step. The calculations in the CoMT step were carried out using  $k_{ij}$ -estimations ( $k_{ij}^{pred}$ ) and with  $k_{ij}$ =0, separately. The results of the CoMT step for both cases are presented in Table 4.5. The PC-SAFT parameters and the optimal process conditions for the best identified real molecule (propylene carbonate) are given as a reference: The value of  $k_{ij}$  for the binary mixture of propylene carbonate with CO<sub>2</sub> is directly adjusted to experimental data ( $k_{ij}^{fit}$ ). The estimation of  $k_{ij}$  relies on the PC-SAFT parameters. For the set of PC-SAFT parameters of the hypothetical molecule, the estimated value of  $k_{ij}$  for the mixture hypothetical solvent-CO<sub>2</sub> is very close to zero ( $k_{ij,(CO_2-solv.)} = 0.0004$ ). Thus, the results of the CoMT step with  $k_{ij}$ -estimations and with  $k_{ij} = 0$  in Table 4.5 are very similar.

The best performing polar components are identified using the mapping procedure described in Chapter 2: First, the process inequality constraint (solvent emission  $m_s$ ) of 444 polar, non-associating real molecules is approximated using a first-order Taylor series expansion (Eq.(2.4)); then, the performance of the real molecules, that are feasible according to the approximation of the constraint ( $m_s^{appr} \le 20 \text{ mg/Nm}^3$ ), is evaluated using a second-order Taylor approximation of the cost objective function  $f^{appr}$  (Eq.(2.3)); finally, a ranking of the feasible real molecules regarding their performance measured by  $f^{appr}$  delivers the mapping list. The set of the ten best performing components identified in the mapping step is presented in Table 4.6. The results in Table 4.6 confirm the findings of Chapter 2. The mapping procedure successfully identifies the real molecule that lies in the Table 4.5: Comparison of the result of the CoMT step with  $k_{ij}$ -estimations for polar solvents to the result of the CoMT step with  $k_{ij} = 0$  and to the result of individual process optimization for the best identified real molecule (propylene carbonate). The value of  $k_{ij}$  for the binary mixture of propylene carbonate with CO<sub>2</sub> is adjusted to experimental data.

	optimal polar	optimal polar	best polar
	molecule	molecule	real molecule
	hypothetical	hypothetical	propylene carbonate
	$(k_{ij}=0)$	$(k_{ij}^{\text{pred}} = 0.0004)$	$(k_{ij}^{fit} = 0.0314)$
M/g/mol	99.57	98.72	102.09
<i>m/-</i>	3.3116	3.3067	3.3386
σ/Å	3.3689	3.3728	3.3506
$\varepsilon/k/K$	309.80	308.00	312.75
$\mu/D$	4.9669	4.9629	4.9765
		optimal process cor	nditions
P <sup>des</sup> /MPa	0.139	0.139	0.131
P <sup>rg</sup> /MPa	0.893	0.892	0.898
T <sup>lean</sup> /K	277.85	277.18	278.78
m <sub>S</sub> /mg/Nm <sup>3</sup>	3.577	3.828	3.006
f <sub>electr.demand</sub> /€/T <sub>CO2</sub> capt.	5.612	5.624	5.966
f <sub>H2 loss</sub> /€/T <sub>CO2</sub> capt.	0.068	0.101	0.131
f <sub>solvent loss</sub> /€/T <sub>CO2</sub> capt.	0.112	0.118	0.090
$f_{\text{utilities}} \neq T_{\text{CO}_2 \text{ capt.}}$	0.745	0.767	0.894
f/€/T <sub>CO2</sub> capt.	6.537	6.610	7.081

immediate vicinity of the optimal (hypothetical) one, with respect to the molecular parameters and optimal process conditions. Results from individual process optimizations ('real ranking') confirm the validity of the mapping step ('mapping ranking' of the 10 best performing components according to the approximation of the objective function).

Table 4.6: Best polar candidate solvents identified by CoMT-CAMD. The ranking predicted in the mapping step ('mapping ranking') is compared to the ranking after individual process optimization ('real ranking'). The optimal process conditions  $\{P^{\text{des}}, P^{\text{rg}}, T^{\text{lean}}\}^{opt}$  and the value of the objective function  $f(k_{ij}^{\text{pred}})$ from individual process optimizations are given. The value of ms indicates a components' feasibility against the inequality process constraint  $m_S^{opt} < 20 \, \text{mg/nm}^3$ . Components' entries with active constraints at optimum (infeasible components) are noted with a star (\*). The melting point temperature  $T_{\rm mp}$  is the lower bound of temperature allowed in individual process optimizations to avoid solidification of the solvent.

	IUPAC Nam	ne		ranking		-	
			mappin	g real	$(k_{ij}^{\text{pred}})$		
	propylene o	carbonate	1		1	•	
	diethyl sulf	ate	2		2		
	$\gamma$ -valerolac	tone	3		5		
	methyl mal	eic anhydride	4		*		
	N-methyl-2	-pyrrolidone	5		4		
	butyric anh	ydride	6		3		
	$\gamma$ -butyrolad	tone	7		8		
	isobutyric a	nhydride	8		7		
	propionic a	nhydride	9		11		
	diethyl mal	onate	10		12		
-						-	
IUPAC Name		$f(k_{ij}^{\text{pred}})$	ms <sup>opt</sup>	$P_{\rm des}^{opt}$	$P_{ m rg}^{opt}$	T <sup>opt</sup> lean	T <sub>mp</sub>
		€/T <sub>CO2</sub> capt.	mg/Nm <sup>3</sup>	МРа	МРа	К	К
propylene carl	oonate	6.837	1.962	0.144	0.927	274.6	224.9
diethyl sulfate		7.138	2.842	0.148	0.934	260.0	248.2
$\gamma$ -valerolacton	e	7.322	10.952	0.144	0.927	269.4	242.2
methyl maleic	anhydride	*	*	*	*	*	281.1
N-methyl-2-py	rrolidone	7.284	8.077	0.142	0.927	268.1	249.2
butyric anhydı	ride	7.254	4.003	0.155	0.938	255.4	199.9
$\gamma$ -butyrolactor	ne	7.668	15.694	0.135	0.929	275.1	229.8
isobutyric anh	ydride	7.589	7.189	0.160	0.940	251.6	219.7

12.623

1.570

0.151

0.142

0.932

0.948

254.1

253.6

7.816

8.309

propionic anhydride

diethyl malonate

228.2

224.3

In Table 4.7, the 'mapping list' (10 best performing solvents) obtained by CoMT-CAMD with the  $k_{ij}$ -estimation models is compared to the ranking of the same components in the 'mapping list' obtained by CoMT-CAMD with  $k_{ij} = 0$ . Propylene carbonate, N-methyl-2-pyrrolidone and  $\gamma$ -valerolactone are among the best performing solvents in both mapping lists. The difference in the ranking of the components can be attributed to the implementation of the  $k_{ij}$ -estimation models.

Table 4.7: Influence of  $k_{ij}$ -estimations on the mapping ranking. The mapping ranking of the 10 best performing solvents obtained by CoMT-CAMD with  $k_{ij}$ -estimations ( $k_{ij}^{\text{pred}}$ ) is compared to the mapping ranking of the same components obtained by CoMT-CAMD with  $k_{ij} = 0$ .

	mapping ranking		
IUPAC Name	# f <sup>appr</sup>	# f <sup>appr</sup>	
	(k <sub>ij</sub> -estimations)	$(k_{ij}=0)$	
propylene carbonate	1	1	
diethyl sulfate	2	5	
$\gamma$ -valerolactone	3	2	
methyl maleic anhydride	4	3	
N-methyl-2-pyrrolidone	5	4	
butyric anhydride	6	8	
$\gamma$ -butyrolactone	7	6	
isobutyric anhydride	8	10	
propionic anhydride	9	13	
diethyl malonate	10	21	

In the following, results from individual process optimizations with predicted  $k_{ij}$  values for the binary mixture of the solvent with CO<sub>2</sub> are compared to results with  $k_{ij}$  values independently adjusted to experimental data. Due to the scarcity of experimental data for binary mixtures with H<sub>2</sub>, the  $k_{ij}$  values for binary mixtures of the solvent with H<sub>2</sub> were in both cases set equal to the predicted values. A further comparison with results from individual process optimizations with  $k_{ij} = 0$  for the solvent binary mixtures intends to show in which extend the accuracy of the CoMT-CAMD result is improved by the implementation of the  $k_{ij}$ -estimation method. Besides, for the sake of consistency,  $k_{ij}$  values for binary mixtures of the solvent with H<sub>2</sub>O are defined equal to zero throughout. A matrix that summarizes the  $k_{ij}$  estimation method for each case is given in Table 4.8. The results of the individual process optimizations are shown in Table 4.9.

According to the results in Table 4.9, the predicted performance with estimated  $k_{ij}$  values (case 1) is closer to the actual one (reference: case 2). When no correction is used in phase equilibrium calculations ( $k_{ij} = 0$ ), the value of the objective function is consistently underestimated. The phase equilibrium diagrams presented in Figure 4.1 support this observation. Compared to experimental data, PC-SAFT predictions with  $k_{ij} = 0$  overestimate the concentration of CO<sub>2</sub> in the liquid phase. For the binary mixture of propylene carbonate with CO<sub>2</sub>, no significant correction

	k <sub>ij</sub> evaluation method					
	case 1:	case 2:	case 3:			
binary mixture	$f(k_{ij}^{\text{pred}})$	$f(k_{ij}^{\rm fit})$	$f(k_{ij}=0)$			
solvent-CO2	QSPR model	exp. data	0			
solvent-H2	QSPR model	QSPR model	0			
solvent-H2O	0	0	0			

Table 4.8: Comparison matrix for results evaluation, according to the  $k_{ij}$  estimation method.

Table 4.9: Influence of  $k_{ij}$  estimation method to the calculated optimal performance of the system. Results from individual optimizations ('real *f*') and the resulting ranking of the components ('real ranking') are presented for the 3 cases of  $k_{ij}$  estimation methods in Table 4.8. The value of the objective function *f* is given in units  $\epsilon/T_{CO_2}$ .

mapping list	real f			real ranking		
(CoMT-CAMD with	(individual process optimizations)		(individual process optimizations)			
k <sub>ij</sub> -estimations)	case 1	case 2	case 3	case 1	case 2	case 3
	$f(k_{ij}^{\text{pred}})$	$f(k_{ij}^{\text{fit}})$	$f(k_{ij}=0)$	$f(k_{ij}^{\text{pred}})$	$f(k_{ij}^{\text{fit}})$	$f(k_{ij}=0)$
propylene carbonate	6.837	7.081	6.545	1	1	1
diethyl sulfate						
$\gamma$ -valerolactone	7.322	7.433	6.923	3	3	3
methyl maleic anhydride						
N-methyl-2-pyrrolidone	7.284	7.162	6.963	2	2	4
butyric anhydride						
$\gamma$ -butyrolactone	7.668	7.479	6.722	4	4	2
isobutyric anhydride						
propionic anhydride						
diethyl malonate						

is achieved with the estimated  $k_{ij}$  value. As can be seen in Table 4.10, the estimated  $k_{ij}$  value for this mixture is too low, closer to 0 than to the correction actually necessary. However, the evaluation of the results generally shows that phase equilibrium calculations with estimated  $k_{ij}$  values describe the real performance of the examined systems (experimental data) with higher accuracy (Table 4.8).

A final point should be commented, namely the decision not to implement a binary interaction correction for the mixtures of the solvent with H<sub>2</sub>O. Mixtures of H<sub>2</sub>O with dipolar, non-associating components are difficult to predict for thermodynamic models and they require correction ( $k_{ij} \neq 0$ ) for more accurate descriptions of phase equilibria. As already discussed in Chapter 3, mixtures with one dipolar, non-associating component and one associating component are most demanding, due to the effects of induced association [21]. In order to avoid introducing unnecessary uncertainties, more accurate correlations of  $k_{ij}$  are required for this type

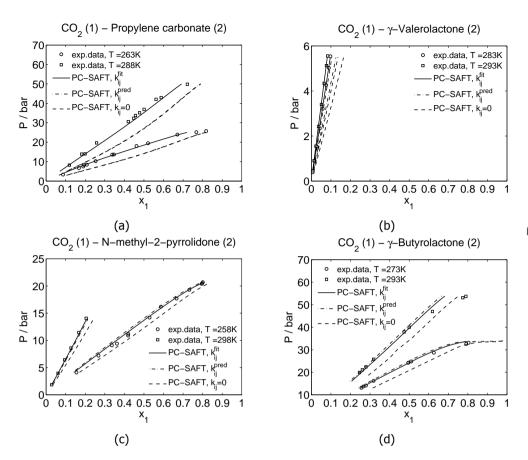


Figure 4.1: Vapor-liquid equilibria for binary mixtures of best performing polar solvents with  $CO_2$ : a)  $CO_2$  - propylene carbonate [16], b)  $CO_2 - \gamma$ -valerolactone [17], c)  $CO_2 - N$ -methyl-2-pyrrolidone [18, 19] and d)  $CO_2 - \gamma$ -butyrolactone [20]. Predictions of PC-SAFT with estimated  $k_{ij}$  values ( $k_{ij}^{pred}$ ) are compared to isothermal experimental data. Correlations with  $k_{ij}$  values adjusted to experimental data ( $k_{ij}^{fit}$ ) and without correction ( $k_{ij} = 0$ ) are also included. The values of the binary interaction parameter ( $k_{ij}^{pred}$  and  $k_{ij}^{fit}$ ) used in the calculations for each binary mixture are given in Table 4.10.

of mixtures. Generally, an improved description of mixtures with  $H_2O$  is necessary. In this case an extension of the process model to include water separation units and the implementation of robust methods for liquid-liquid equilibrium calculations might be needed. 98

Table 4.10: Binary interaction parameters  $k_{ij}$  for the binary mixtures of CO<sub>2</sub> with polar solvents.  $k_{ij}^{\text{fit}}$  was estimated using a QSPR model (Appendix E.5).  $k_{ij}^{\text{fit}}$  was adjusted to experimental data, which were obtained from the Dortmund DataBase [22] and passed the thermodynamic consistency tests [23].

Binary mixture	$k_{ij}^{\text{pred}}$	$k_{ij}^{\rm fit}$	Temp. range	n	Ref.
CO <sub>2</sub> - propylene carbonate	0.0010	0.0314	228 K – 463 K	245	DDB [22]
$CO_2$ - $\gamma$ -valerolactone	0.0243	0.0466	283 K – 323 K	40	DDB [22]
CO <sub>2</sub> - N-methyl-2-pyrrolidone	0.0131	0.0163	258 K – 373 K	139	DDB [ <mark>22</mark> ]
$CO_2 - \gamma$ -butyrolactone	0.0221	0.0184	273 K – 308 K	62	DDB [22]

# 4.4. Conclusions

 $k_{ij}$ -estimation models were implemented in the CoMT-CAMD framework for the binary mixtures of the solvent with CO<sub>2</sub> and H<sub>2</sub>. The implementation of  $k_{ij}$ -estimation models in CoMT-CAMD has an impact on the mapping ranking. QSPR relations for the prediction of  $k_{ij}$  are embedded into the PC-SAFT model. Thereby, the derivatives calculated at optimum for the approximation of the objective function  $f^{appr}(\bar{x}, \bar{y})$  and of the constraint  $m_S^{appr}(\bar{x}, \bar{y})$  are different than the derivatives with  $k_{ij} = 0$ . Although the optimal parameters of the hypothetical molecule (result of the CoMT step) with  $k_{ij}$ -estimations and with  $k_{ij} = 0$  are similar, the mapping ranking is different, because the same change in the molecular parameters results to a different change in the objective function.

A comparison of phase equilibria calculations with predicted  $k_{ij}$ -values and with  $k_{ij} = 0$  to experimental data of vapor-liquid equilibria was carried out for best performing real solvents. The results of phase equilibria calculations with predicted values of  $k_{ij}$  are closer to the experimental data than the results obtained with  $k_{ij} = 0$ . Considering values of the objective function obtained by calculations with  $k_{ij}$  adjusted to experimental data as a reference, the implementation of the  $k_{ij}$ -estimations gives more representative results than when  $k_{ij} = 0$  is used.

The results of this chapter show, that the prediction of  $\vec{k_{ij}}$ -values with the QSPR models developed in this thesis enhances the accuracy in phase equilibria calculations and thereby the accuracy of CoMT-CAMD results.

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# **Conclusions and Perspectives**

## 5.1. Conclusions

### 5.1.1. Further development of the CoMT-CAMD method

In this thesis, the framework of Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD) is further developed and implemented for the simultaneous process and solvent design for  $CO_2$  capture.

The main performance trade-offs of the  $CO_2$ -capture system are evaluated using a single, cost-based, objective function. Limitations about the environmental performance of the solvent are, additionally, considered through a process inequality constraint. The performance of candidate solvents is evaluated by an approximation of the objective function using a Taylor series expansion around the optimal solution of the CoMT optimization problem (mapping step). Evaluation of inequality process constraints was included in the mapping step using a linear approximation. Thereby, real components that do not satisfy the process inequality constraints ("infeasible components"), are excluded from the set of best performing candidates. As proven by individual process optimizations (validation of the CoMT-CAMD results), the best performing components identified in the mapping step are indeed the feasible components with best achievable performance for the problem at hand. The results of the case studies examined in chapters 2 and 4 showed that CoMT-CAMD can be successfully solved for rigorous (reasonably complex) process models and that minor changes in the process model do not alter significantly the set of

and that minor changes in the process model do not alter significantly the set of best performing real solvents. Changes in the objective function are expected, however, to have higher influence on the result of the problem. Here lies also one of the main strengths of CoMT-CAMD, being a deterministic method. In this regard, the objective function should be carefully chosen and consider all major trade-offs of the design problem.

Further, predictions of the ideal gas specific heat capacity  $c_p^{ig}$  and the molar mass M of pure components, as function of the PC-SAFT pure component parameters, were developed. Reasonable correlations of  $c_p^{ig}$  and M are established using QSPR-models, with correlation coefficients R<sup>2</sup> higher than 0.98 and 0.93, respectively. In CoMT-CAMD, the PC-SAFT pure component parameters of the optimized fluid (i.e. solvent) are molecular degrees of freedom for the optimization problem. The proposed QSPR models incorporated in CoMT-CAMD enable the calculation of full caloric properties and mass specific quantities.

Prediction of mixture properties and phase equilibria are particularly demanding for thermodynamic models. Often, binary interaction parameters adjusted to experimental data have to be applied, in order to allow for more accurate calculations of excess properties. In CAMD problems, binary interaction parameters cannot be adjusted to experimental mixture data. Therefore, in the course of this thesis, a QSPR-model, that relates the binary interaction parameter  $k_{ij}$  to the PC-SAFT pure component parameters, has been developed.

Good predictions of  $k_{ij}$  were obtained for binary mixtures of two non-associating substances, of one non-associating and one associating substance and of two associating substances. For these types of binary mixtures,  $k_{ij}$  can be successfully correlated to the PC-SAFT parameters of the mixture components.  $k_{ij}$  predictions

with the proposed QSPR-model for binary mixtures of one dipolar, non-associating and one associating substance were, however, only partially successful. The effects of induced association present in this type of mixtures are not trivial and their influence should be further examined.

In the last chapter of this thesis, the role of binary interaction parameters for an improved prediction of mixture properties has been investigated. CoMT-CAMD was implemented for the simultaneous process and solvent optimization for  $CO_2$ capture, with estimations of  $k_{ij}$  in binary mixtures of the optimized solvent. The evaluation of the results showed that the accuracy of the CoMT-CAMD approach can be further enhanced by using the developed QSPR-models for  $k_{ij}$ .

#### **5.1.2.** Optimal solvents for pre-combustion $CO_2$ capture

The process examined in this thesis resembles in its' key features the process of  $CO_2$  capture of the pre-combustion capture pilot plant at the IGCC power plant in Buggenum. The applied process model considers the main steps of absorption, desorption and  $CO_2$  compression. The performance of the system is measured by a single, process-based cost objective function. The objective function is written as the sum of operating costs covering the primary energy consumption, consumption of raw materials and product loss in the major stages of the process. In addition to an economic penalty for solvent loss, a maximum value for solvent loss was considered as an inequality constraint, reflecting an emission threshold. Thereby the optimization of the overall performance of the system is attained, subject to environmental constraints.

Non-polar and polar solvents were examined separately. The set of best performing real components includes state-of-the-art solvents, like propylene carbonate and N-methyl-2-pyrrolidone. Because the optimization and the mapping procedure are fully deterministic, independent from pre-selection of candidates and heuristics, the presence of state-of-the-art solvents gives some additional confidence regarding the plausibility of the entire list of best performing solvents. Similarities in the molecular structure of the best performing components are also observed. Carbonylic oxygen and phenyl rings are present in the molecule of almost all best performing components. The favorable interactions of carbonylic oxygen and phenyl rings with  $CO_2$  have been already studied by other authors [1–3]. The best components generally correspond to small molecules (low values of the segment number and segment diameter in the PC-SAFT representation), with high dispersive energy and dipole moment.

The best identified polar solvents show a higher potential to improve the overall performance of the process. The best polar solvents outperform DEPGs. DEPGblends have been successfully employed in applications for pre-combustion  $CO_2$  capture. It should be taken into account, though, that such applications (e.g. the Selexol process) are designed for the sequential removal of  $H_2S$  and  $CO_2$ . Here, the removal of  $H_2S$  is not evaluated by the objective function.

A promising result of this work is the identification of  $\gamma$ -valerolactone among the best performing polar solvents.  $\gamma$ -Valerolactone has been classified by some authors [4, 5] as a green solvent for bio-refineries and appears to be a promis-

ing solvent for CO<sub>2</sub> capture as well. For the binary mixture  $\gamma$ -valerolactone - CO<sub>2</sub> only scarce experimental data are available, for low pressure vapor-liquid equilibria. Additional VLE measurements at elevated pressures for the binary systems of  $\gamma$ -valerolactone with CO<sub>2</sub>, H<sub>2</sub> and H<sub>2</sub>O are suggested. A more thorough experimental research may confirm the result of CoMT-CAMD and reveal  $\gamma$ -valerolactone as a prospective, green solvent for pre-combustion CO<sub>2</sub> capture.

## **5.2.** Perspectives

Founded on the use of physically based thermodynamic models, CoMT-CAMD grows fast, together with the PC-SAFT model. Developments in the PC-SAFT model support CoMT-CAMD and broaden its' application range. On the other side, CoMT-CAMD poses constantly challenging questions regarding the prediction of thermodynamic properties with PC-SAFT.

A prospective future extension of the CoMT-CAMD framework is to consider investment costs in the objective function. Estimating investment costs requires sizing (i.e. dimensioning) of key equipment, which in turn necessitates transport properties, like viscosity, heat transfer and diffusion coefficients. In CoMT-CAMD, the transport properties of the optimized fluid have to be expressed as functions of the PC-SAFT pure component parameters. The prediction of viscosity, heat transfer and diffusion coefficients for pure substances and mixtures with PC-SAFT is an on-going work [6, 7], that will allow, for example, the design of heat exchangers and rate-based models for absorption.

CoMT-CAMD has been implemented for the design of new solvent molecules, beyond an existing substance-database. [8] The procedure for the identification of the optimal molecule at optimal process conditions (CoMT optimization step) remains unchanged. For the design of new solvent molecules, a group-contribution approach of PC-SAFT (GPC-SAFT [9]) is employed and together with feasibility constraints on the molecular structure in the mapping step, as described in ref. [8] by the present author and co-workers. The PC-SAFT pure component parameters of the designed solvent are calculated from the parameters of functional groups, using GPC-SAFT [9]. So far, only molecular structures with a single polar group have been considered. The parameterization of GPC-SAFT to molecules with multiple polar groups will increase accuracy and thus allow for the design of more powerful fluids. Further, the implementation of a hetero-segmented group-contribution approach for PC-SAFT (ref. [9]) may allow for the distinction between isomers.

A first step towards the extension of CoMT-CAMD to the design of fluid mixtures has already been taken by the implementation of the method to working fluid mixtures for ORC applications [10]. For the design of binary fluid mixtures, the pure component parameters of the second fluid are introduced as additional molecular degrees of freedom to the optimization problem. In the mapping step, the implementation of a CAMD approach, with predictions of  $k_{ij}$  values based on GPC-SAFT, seems to be a promising approach.

The presence of water is for many problems a limiting design factor. The implementation of robust methods for the prediction of liquid-liquid phase equilibria with PC-SAFT would help to consider the influence of water in mixture streams with the optimized fluid. Finally, robust liquid-liquid equilibrium calculations will support the implementation of CoMT-CAMD to the optimization of liquid extraction process.

A perspective of CoMT-CAMD on a somewhat longer time scale is given for the modeling of (solid) materials and products determined by structure including interfaces.

CoMT-CAMD is a platform, on which molecular thermodynamics, process engineering and modern algorithmic techniques combine their strengths, in order to approach the demanding problem of integrated process and molecular design. Heuristic decisions give their place to deterministic solutions and CoMT-CAMD allows for a new generation of optimal process and fluid designs.

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# A

# The PC-SAFT EoS

This appendix summarizes the equations used for calculating thermodynamic properties from the PC-SAFT equation-of-state (EoS). The equations presented bellow are directly adopted from ref. [1-5].

## **A.1.** Helmholtz energy

**Hard-chain (reference fluid) contribution.** The contribution of the hard-chain reference fluid is given as

$$\tilde{a}^{hc} = \overline{m}\tilde{a}^{hs} - \sum_{i} x_i \left(m_i - 1\right) \ln g_{ii}^{hs}(\sigma_{ii}) \tag{A.1}$$

with  $\overline{m} = \sum_i x_i m_i$  the mean segment number in the mixture. The contribution of the hard-sphere reference  $\tilde{a}^{hs}$  is given by

$$\tilde{a}^{hs} = \frac{1}{\zeta_0} \cdot \left[ \frac{3\zeta_1 \zeta_2}{(1 - \zeta_3)} + \frac{\zeta_2^3}{\zeta_3 (1 - \zeta_3)^2} + \left( \frac{\zeta_2^3}{\zeta_3^2} - \zeta_0 \right) \ln (1 - \zeta_3) \right]$$
(A.2)

where  $\zeta_n$  is defined as

$$\zeta_n = \frac{\pi}{6} \rho \sum_i x_i m_i d_i^n \quad n \in \{0, 1, 2, 3\}$$
(A.3)

 $\rho$  is the number density of molecules and  $d_i$  is the temperature-dependent diameter of component i, given by

$$d_i = \sigma_i \left[ 1 - 0.12 \exp\left(-3\frac{\varepsilon_{ii}}{kT}\right) \right]$$
(A.4)

The radial distribution function at contact distance of two hard spheres [6, 7] is given by

$$g_{ij}^{hs} = \frac{1}{(1-\zeta_3)} + \frac{d_i d_j}{d_i + d_j} \cdot \frac{3\zeta_2}{(1-\zeta_3)^2} + \left(\frac{d_i d_j}{d_i + d_j}\right)^2 \cdot \frac{2\zeta_2^2}{(1-\zeta_3)^3}$$
(A.5)

**Dispersive contribution.** The contribution due to dispersive intermolecular potentials for chain molecules is given as a sum of first- and second-order contributions [8]:

$$\tilde{a}^{disp} = \tilde{a}_1 + \tilde{a}_2 \tag{A.6}$$

$$\tilde{a}_1 = -2\pi\rho \cdot I_1(\eta, \overline{m}) \cdot \overline{m^2 \varepsilon \sigma^3}$$
(A.7)

$$\tilde{a}_2 = -\pi\rho C_1 \cdot I_2 \left(\eta, \overline{m}\right) \cdot \overline{m^2 \varepsilon^2 \sigma^3} \tag{A.8}$$

where  $\eta$  is the packing fraction defined as  $\eta = \zeta_3$  and the integrals of the perturbation theory  $I_1(\eta, \overline{m})$  and  $I_2(\eta, \overline{m})$  are substituted by power series in density [1]:

$$I_1(\eta, \overline{m}) = \sum_{i=0}^6 a_i(\overline{m})\eta^i$$
(A.9)

$$I_2(\eta, \overline{m}) = \sum_{i=0}^6 b_i(\overline{m})\eta^i$$
(A.10)

The coefficients of Eq.(A.9) and (A.10) are adjusted to experimental pure component data of elongated molecules i.e. the series of n-alkanes and they are given in the work of Gross and Sadowski [1]. The abbreviated terms  $\overline{m^2 \varepsilon \sigma^3}$ ,  $\overline{m^2 \varepsilon^2 \sigma^3}$  and  $C_1$  are given as

$$\overline{m^2 \varepsilon \sigma^3} = \sum_i \sum_j x_i x_j m_i m_j \left(\frac{\varepsilon_{ij}}{kT}\right) \sigma_{ij}^3 \tag{A.11}$$

$$\overline{m^2 \varepsilon^2 \sigma^3} = \sum_i \sum_j x_i x_j m_i m_j \left(\frac{\varepsilon_{ij}}{kT}\right)^2 \sigma_{ij}^3$$
(A.12)

$$C_{1} = kT \left(\frac{\partial \rho}{\partial P}\right)^{hc} = \overline{m} \cdot \left(1 + Z^{hc} + \rho \frac{\partial Z^{hc}}{\partial \rho}\right)^{-1} = \left(1 + \overline{m} \cdot \frac{8\eta - 2\eta^{2}}{(1 - \eta)^{4}} + (1 - \overline{m}) \cdot \frac{20\eta - 27\eta^{2} + 12\eta^{3} - 2\eta^{4}}{[(1 - \eta)(2 - \eta)]^{2}}\right)^{-1}$$
(A.13)

The dispersive parameters of a pair of unlike segments are given by the Lorentz-Berthelot combining rules:

$$\sigma_{ij} = \frac{1}{2} \left( \sigma_i + \sigma_j \right) \tag{A.14}$$

$$\varepsilon_{ij} = (1 - k_{ij})\sqrt{\varepsilon_i \varepsilon_j} \tag{A.15}$$

where  $k_{ij}$  is the binary interaction parameter that corrects the equation-of-state for unlike intermolecular potentials.

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**Association contribution.** The term of the residual Helmholtz energy due to associating intermolecular potentials  $\tilde{a}^{assoc}$  is calculated as described in the work of Chapman et al. [5]. The radial distribution function  $g_{ij}^{hs}$  is here the one defined in Eq.(A.5). For mixtures

$$\tilde{a}^{assoc} = \sum_{i} x_{i} \left[ \sum_{A_{i}} \left[ \ln X^{A_{i}} - \frac{X^{A_{i}}}{2} \right] + \frac{1}{2} M_{i} \right]$$
 (A.16)

where  $M_i$  is the number of associating sites of the molecule of component *i* in the mixture and summation runs over all different types of association sites (A, B, C, ...) in each molecule *i*.  $x_i$  is the mole fraction of all molecules of component *i* and the mole fraction  $X^{A_i}$  of molecules not bonded at site  $A_i$  is given by

$$X^{A_i} = \left[1 + N \cdot \sum_j \sum_{B_j} \rho_j X^{B_j} \Delta^{A_i B_j}\right]^{-1}$$
(A.17)

where  $\sum_{j}$  runs over all mixture components,  $\sum_{B_j}$  runs over all different sites on molecule j ( $A_j$ ,  $B_j$ ,  $C_j$ , ...) and  $\rho_j = x_j \cdot \rho$  is the molar density of component j. The association strength  $\Delta^{A_i B_j}$  between a site of type A in molecule i and a site of type B in molecule j is given by

$$\Delta^{A_i B_j} = \sigma_{ij} g^{hs}(\sigma_{ij}) \kappa^{A_i B_j} \left[ exp\left(\frac{\varepsilon^{A_i B_j}}{kT}\right) - 1 \right]$$
(A.18)

The cross-association parameters are calculated from pure-component association parameters using the Wolbach and Sandler [9] combining rules:

$$\varepsilon^{A_i B_j} = \frac{1}{2} \left( \varepsilon^{A_i B_i} + \varepsilon^{A_j B_j} \right) \tag{A.19}$$

$$\kappa^{A_i B_j} = \sqrt{\kappa^{A_i B_i} \kappa^{A_j B_j}} \cdot \left[\frac{2\left(\sigma_{ii}\sigma_{jj}\right)}{\sigma_{ii} + \sigma_{jj}}\right]^3 \tag{A.20}$$

In the current work the PC-SAFT EoS for associating components is implemented using the 2B-association scheme, according to Huang and Radosz [10]. The assumptions of the 2B-association scheme for mixtures can be summarized as:

$$\Delta^{A_i A_i} = \Delta^{B_i B_i} = \Delta^{A_j A_j} = \Delta^{B_j B_j} = 0$$
  

$$\Delta^{A_i B_i} = \Delta^{A_i B_i} \neq 0$$
  

$$\Delta^{A_i B_j} = \Delta^{A_j B_i}$$
  

$$X^{A_i} = X^{B_i}$$
  

$$X^{A_i} \neq X^{A_j}$$
(A.21)

**Contribution of quadrupole-quadrupole, dipole-dipole and dipole-quadrupole interactions.** The term of the residual Helmholtz energy due to quadrupolar interactions is based on a perturbation theory of third-order, written in the Padè approximation [3, 11]:

$$\tilde{a}^{qq} = \frac{\tilde{a}_2^{qq}}{1 - \tilde{a}_3^{qq}/\tilde{a}_2^{qq}}$$
(A.22)

with

$$\tilde{a}_{2}^{qq} = -\pi \left(\frac{3}{4}\right)^{2} \rho \sum_{i} \sum_{j} x_{i} x_{j} \frac{\varepsilon_{ii}}{kT} \cdot \frac{\varepsilon_{jj}}{kT} \cdot \frac{\sigma_{ii}^{5} \sigma_{jj}^{5}}{\sigma_{ij}^{7}} \cdot Q_{i}^{*2} \cdot Q_{j}^{*2} \cdot J_{2,ij}^{qq}$$
(A.23)

$$\tilde{a}_{3}^{qq} = \frac{\pi}{3} \left(\frac{3}{4}\right)^{3} \rho \sum_{i} \sum_{j} x_{i} x_{j} \left(\frac{\varepsilon_{ii}}{kT}\right)^{3/2} \left(\frac{\varepsilon_{jj}}{kT}\right)^{3/2} \cdot \frac{\sigma_{ii}^{15/2} \sigma_{jj}^{15/2}}{\sigma_{ij}^{1}2} \cdot Q_{i}^{*3} \cdot Q_{j}^{*3} \cdot J_{3,ij}^{qq} + \frac{4\pi^{2}}{3} \left(\frac{3}{4}\right)^{3} \rho^{2} \sum_{i} \sum_{j} \sum_{k} x_{i} x_{j} x_{k} \cdot \frac{\varepsilon_{ii}}{kT} \cdot \frac{\varepsilon_{jj}}{kT} \cdot \frac{\varepsilon_{kk}}{kT} \cdot \frac{\sigma_{ii}^{5} \sigma_{jj}^{5} \sigma_{kk}^{5}}{\sigma_{ij}^{3} \sigma_{ik}^{3} \sigma_{jk}^{3}} \cdot Q_{i}^{*2} \cdot Q_{i}^{*2} \cdot Q_{k}^{*2} \cdot J_{3,ijk}^{qq}$$
(A.24)

where  $Q_i^{*2} = Q_i^2 / (m_i \sigma_{ii}^5 \varepsilon_{ii})$  is the dimensionless squared quadrupole moment.  $J_{2,ij}^{qq}$  and  $J_{3,ij}^{qq}$  are the integrals over the pair correlation function of the reference fluid and  $J_{3,ijk}^{qq}$  is the integral over three-body correlation functions. As described in the work of Gross [3] the integral  $J_{3,ij}^{qq}$  is assumed to be equal to zero. The integral  $J_{2,ij}^{qq}$  for a pure fluid is assumed to be only a function of *T* and  $\rho$  and a functional of elongation (or segment number, *m*):

$$J_{2,ij}^{qq} = \sum_{n=0}^{4} \left( a_{n,ij} + b_{n,ij} \cdot \frac{\varepsilon_{ij}}{kT} \right) \cdot \eta^n$$
(A.25)

The integral  $J_{3,ijk}^{qq}$  is assumed to be temperature-independent and it is approximated as

$$J_{3,ijk}^{qq} = \sum_{n=0}^{4} c_{n,ijk} \cdot \eta^n$$
 (A.26)

Gross [3] adjusted the model constants of Eq.(A.25) and (A.26) to molecular simulation data [12] of spherical and non-spherical molecules respectively. The adjustment of the model constants, that was carried out for varying elongations of a two-centers Lennard-Jones (2CLJ) fluid, allows an expression of quadrupolar interactions, which is valid for varying chain lengths [3].

In an analogous manner the terms of the residual Helmholtz energy due to dipole-dipole and dipole-quadrupole interactions are derived [4, 13].

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B

# Process model and objective function

# **B.1.** Process model for the pre-combustion CO<sub>2</sub> capture

The process topology for the pre-combustion  $CO_2$  capture (Figure B.1) considers the main stages of absorption, desorption and  $CO_2$  compression to pipeline pressure. The number of stages in the absorber has been defined using a sensitivity analysis as described in section 2.3.1 and detailed in B.1.1. Desorption includes two sequential pressure reduction flash stages. The absorber and the two desorption flashes are modeled using a phase equilibrium stage model. Two recycle streams are considered; the H<sub>2</sub> rich gas stream from the first (rich gas) desorption flash ('rg') and the liquid stream of the lean solvent ('lean'). The process simulation problem is formulated as a system of non-linear equations

$$\mathbf{r}(\overline{y}) = 0 \tag{B.1}$$

where  $\overline{y}$  is the vector of the iterated process variables. The equations in (B.1) are formulated on the residuals between the iterated and calculated values of the process variables for: a) the internal streams of the absorber  $\mathbf{r}^{abs}(\overline{y})$  and b) the process variables of the two recycle streams  $\mathbf{r}^{rec,rg}(\overline{y})$  and  $\mathbf{r}^{lean}(\overline{y})$ . Finally, (B.1) includes the equation of the process specification for constant CO<sub>2</sub> capture rate in the absorber  $\mathbf{r}^{spec}(\overline{y})$ .

$$\mathbf{r}(\overline{y}) := \{\mathbf{r}^{abs}(\overline{y}), \quad \mathbf{r}^{rec,rg}(\overline{y}), \quad \mathbf{r}^{rec,lean}(\overline{y}), \quad \mathbf{r}^{spec}(\overline{y})\}$$
(B.2)

In process optimization as well as in simultaneous process and solvent optimization, the equations in (B.2) represent the equality process constraints of the optimization problem.

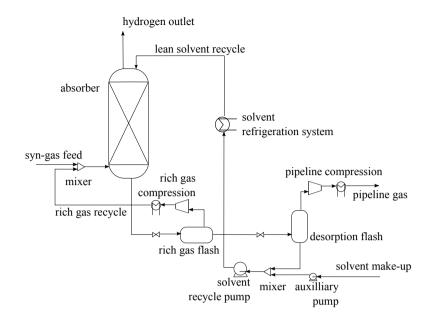
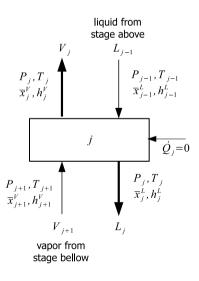
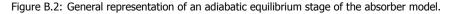


Figure B.1: Process topology of pre-combustion CO<sub>2</sub> capture system (adopted from Stavrou et al. [1]).

#### B.1.1. Absorption

For the absorber an equilibrium stage model is considered. Figure B.2 gives a general schematic representation of the j-th stage of the absorber. The so-called





MESH equations used to model the equilibrium stages j are: the component balance equations (M), the equilibrium relations (E), the summation equations (S) and the energy balance equations (H). [2]

The summation equations for the vapor and liquid streams are

$$\sum_{i=1}^{N_c} x_{i,j}^V = 1 \quad \text{and} \quad \sum_{i=1}^{N_c} x_{i,j}^L = 1$$
(B.3)

where  $x_{i,j}^V$  and  $x_{i,j}^L$  are the mole fractions of each system component *i* in the vapor  $V_j$  and the liquid  $L_j$  stream exiting stage *j* and  $N_c$  is the total number of components. The component balance equation for component *i*, for the *j*-th stage of the absorber writes

$$x_{i,j+1}^V \cdot V_{j+1} + x_{i,j-1}^L \cdot L_{j-1} - x_{i,j}^V \cdot V_j - x_{i,j}^L \cdot L_j = 0$$
(B.4)

When Eq. (B.4) is formulated for all  $N_c$  components, the equation of the total mass balance is redundant.

For the *j*-th stage of the adiabatic absorber, where the heat stream  $\dot{Q}_j = 0$ , the energy balance equation writes

$$h_{j+1}^{V} \cdot V_{j+1} + h_{j-1}^{L} \cdot L_{j-1} - h_{j}^{V} \cdot V_{j} - h_{j}^{L} \cdot L_{j} = 0$$
(B.5)

where  $h_j^V$  and  $h_j^L$  denote the molar enthalpy of the vapor and the liquid stream, respectively.

The phase equilibrium condition is solved for all components *i* using the isofugacity condition

$$x_{i,j}^{V} \cdot \varphi_{i,j}^{V} - x_{i,j}^{L} \cdot \varphi_{i,j}^{L} = 0$$
(B.6)

where  $\varphi_{i,j}^V$  and  $\varphi_{i,j}^L$  are the fugacity coefficients of component *i* in the vapor and liquid phase, respectively.

#### Calculation of internal streams using a simultaneous correction method

Equilibrium stage models for multi-stage, multi-component separation problems have been extensively studied in the literature. A summary of the various solution methods for equilibrium stage models can be found in ref. [3] and [2].

In the current work, the absorber model is solved using a simultaneous correction method [2]. Simultaneous correction methods are computationally efficient and are considered as robust regarding the convergence in physical property calculations. [2] The MESH equations are solved simultaneously.

The variables used in the current implementation are slightly different from the variables shown in Figure B.2. The iterated variables are the component vapor and liquid molar flows and the temperature of the internal streams of the absorber. More specifically, for the *j*-th stage of the absorber (with j = 2, ..., N - 1) the temperatures  $T_j^V$  and  $T_j^L$  of the exiting vapor and liquid streams are iterated alongside with the component molar flows  $\overline{v}_j := \{v_{1,j}, ..., v_{N_c,j}\}$  and  $\overline{l}_j := \{l_{1,j}, ..., l_{N_c,j}\}$ . The

molar enthalpies of the exiting streams are calculated as function of the pressure  $P_i$ , the iterated temperature and component molar flows:

$$h_{j}^{V} = h_{j}^{V} \left( P_{j}, T_{j}^{V}, \overline{x}_{j}^{V} \right) \quad \text{and} \quad h_{j}^{L} = h_{j}^{L} \left( P_{j}, T_{j}^{L}, \overline{x}_{j}^{L} \right)$$

$$\text{with} \quad x_{i,j}^{V} = \frac{v_{i,j}}{\sum_{i=1}^{N_{c}} v_{i,j}} \quad \text{and} \quad x_{i,j}^{L} = \frac{l_{i,j}}{\sum_{i=1}^{N_{c}} l_{i,j}}$$

$$(B.7)$$

For a countercurrent multi-equilibrium-stage model, such as an absorption column, one needs to iteratively solve internal variables. For the 1<sup>st</sup> stage of the absorber (j = 1) we define as iterated variables the temperature  $T_1^L$  and component molar flows of the exiting liquid stream  $\bar{l}_1$ ; for the last stage of the absorber (j = N) only the temperature  $T_N^V$  and component molar flows of the exiting vapor stream  $\bar{v}_N$  are iterated.

The pressure drop along the absorption column is neglected, thus

$$P_i = P^{\text{abs}} = P. \tag{B.8}$$

A schematic representation of the equilibrium stage model with the modified simulation variables is given in Figure B.3.

Phase equilibrium calculations are carried out using an adiabatic-isobaric flash algorithm (PQ-flash). For every stage j (with j = 1, ..., N) a pseudo-feed stream with total molar flow  $F_j$ , composition  $\overline{x}_j^F$  and molar enthalpy  $h_j^F$  is defined. The pseudo-feed stream is calculated from the iterated streams entering stage j, namely the liquid stream exiting stage j - 1 and the vapor stream exiting stage j + 1:

$$F_j = \sum_{i=1}^{N_c} l_{i,j-1} + \sum_{i=1}^{N_c} v_{i,j+1}$$
(B.9)

$$x_{i,j}^{\rm F} = \frac{l_{i,j+1} + v_{i,j-1}}{F_j}$$
(B.10)

and 
$$h_j^{\rm F} = \frac{\sum_{i=1}^{N_c} l_{i,j-1}}{F_j} \cdot h_{j-1}^{\rm L} + \frac{\sum_{i=1}^{N_c} v_{i,j+1}}{F_j} \cdot h_{j-1}^{\rm V}.$$
 (B.11)

For the 1<sup>st</sup> stage the pseudo-feed stream is calculated using Eq.(B.9) to (B.11) with the iterated component molar flows  $\overline{v}_2$  of the vapor stream exiting stage 2 and the iterated component molar flows  $\overline{l}^{\text{lean}}$  of the lean solvent recycle that enters the absorber in stage 1. The pseudo-feed stream for the last stage *N* is calculated using Eq.(B.9) to (B.11) with the iterated component molar flows  $\overline{l}_{N-1}$  of the liquid stream exiting stage N - 1 and the iterated component molar flows of the rich gas recycle stream  $\overline{v}^{\text{rg}}$  entering the absorber in stage *N*.

Using the pseudo-feed stream defined in Eq.(B.9) to (B.11), phase equilibrium calculations deliver for every stage *j* the calculated values of the component molar flows  $\overline{\hat{v}}_j := {\hat{v}_{1,j}, ..., \hat{v}_{N_c,j}}$  and  $\overline{\hat{l}}_j := {\hat{l}_{1,j}, ..., \hat{l}_{N_c,j}}$ , the temperatures  $\hat{T}_j^V = \hat{T}_j^L = \hat{T}_j$ 

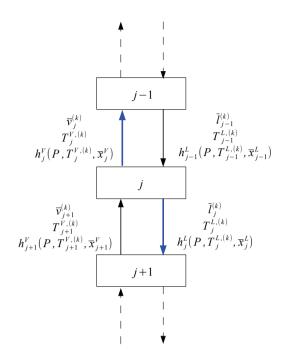


Figure B.3: In the *k*-th iteration for stage *j* of the absorber (with j = 2, ..., N - 1) the component molar flows  $\overline{v}_j^{(k)}$  and  $\overline{l}_j^{(k)}$  and the temperatures  $T_j^{V,(k)}$  and  $T_j^{L,(k)}$  of the vapor and the liquid exiting streams are iterated, respectively.

and thereby the molar enthalpies  $\hat{h}_j^V$  and  $\hat{h}_j^L$  of the exiting vapor and liquid streams (Figure B.4). For the *j*-th stage of the absorber (with j = 2, ..., N - 1) the equations of the residuals between iterated variables and their calculated values then write

$$\mathbf{r}_{j}^{\text{abs}} = \begin{pmatrix} h_{j}^{V} - \hat{h}_{j}^{V} \\ h_{j}^{L} - \hat{h}_{j}^{L} \\ v_{1,j} - \hat{v}_{1,j} \\ v_{2,j} - \hat{v}_{2,j} \\ \vdots \\ v_{N_{c},j} - \hat{v}_{N_{c},j} \\ l_{1,j} - \hat{l}_{1,j} \\ l_{2,j} - \hat{l}_{2,j} \\ \vdots \\ l_{N_{c},j} - \hat{l}_{N_{c},j} \end{pmatrix}, \quad \text{for} \quad j \neq 1 \quad \text{and} \quad j \neq N$$
(B.12)

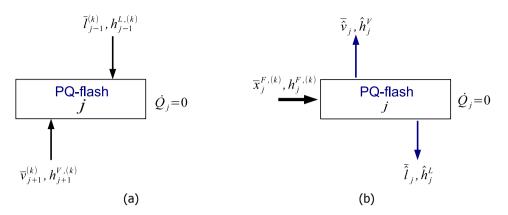


Figure B.4: Generic representation of the input and output variables of the adiabatic-isobaric flash (PQ-Flash) calculations for stage j. (a): The actual input variables for PQ-flash are the iterated component molar flows and molar enthalpies (function of the iterated temperature) of the streams entering the equilibrium stage. Stage j is considered adiabatic ( $\dot{Q}_j = 0$ ). (b): A pseudo-feed stream is defined for stage j as function of the iterated variables of the liquid and vapor streams entering stage j, as presented in (a). Phase equilibrium calculations with PQ-flash give the component molar flows and the molar enthalpies of the vapor and liquid streams exiting stage j in equilibrium.

For the 1<sup>st</sup> stage

$$\mathbf{r}_{1}^{\text{abs}} = \begin{pmatrix} h_{1}^{L} - h_{1}^{L} \\ l_{1,1} - \hat{l}_{1,1} \\ l_{2,1} - \hat{l}_{2,1} \\ \vdots \\ l_{N_{c},1} - \hat{l}_{N_{c},1} \end{pmatrix}$$
(B.13)

while for the last stage N

$$\mathbf{r}_{N}^{\text{abs}} = \begin{pmatrix} h_{N}^{V} - \hat{h}_{N}^{V} \\ v_{1,N} - \hat{v}_{1,N} \\ v_{2,N} - \hat{v}_{2,N} \\ \vdots \\ v_{N_{c},N} - \hat{v}_{N_{c},N} \end{pmatrix}$$
(B.14)

The residual equations for the internal streams of the absorber formulate the square  $2(N_c + 1)(N - 1)$  equation system

$$\mathbf{r}^{\mathrm{abs}}(\overline{y}) := \{\mathbf{r}_1^{\mathrm{abs}}, \mathbf{r}_2^{\mathrm{abs}}, \dots, \mathbf{r}_{N-1}^{\mathrm{abs}}, \mathbf{r}_N^{\mathrm{abs}}\}$$
(B.15)

 $\mathbf{r}^{abs}(\overline{y}^{abs})$  is a subset of the equation system in (B.2).

#### B.1. Process model for the pre-combustion $CO_2$ capture

#### Phase equilibrium calculations

For phase equilibrium calculations in the absorber the adiabatic-isobaric flash problem (PQ-flash) is solved for every stage j (Figure B.4). The isothermal-isobaric two-phase flash problem (PT-flash), which is a sub-problem of PQ-flash, is solved using the successive substitution Rachford-Rice algorithm (according to Michelsen and Mollerup) [4]. The required caloric properties (residual part) and fugacities in the PT-flash and PQ-flash problems are calculated with the PC-SAFT EoS.

#### Process specifications

For the examined pre-combustion CO<sub>2</sub> capture system a constant CO<sub>2</sub> capture rate in the absorber of 90% is specified. In this work, the CO<sub>2</sub> capture rate  $\alpha_{CO_2}$  is defined as CO<sub>2</sub> captured in the absorber with respect to the CO<sub>2</sub> molar flow in the syngas stream  $v_{CO_2}^{sg}$ 

$$\alpha_{\rm CO_2} = 1 - \frac{\dot{v}_{\rm CO_2,1}}{v_{\rm CO_2}^{\rm sg}} \tag{B.16}$$

where  $\hat{v}_{CO_2,1}$  is the (calculated) value of the CO<sub>2</sub> molar flow in the gas stream exiting the 1<sup>st</sup> stage of the absorber. The residual equation  $\mathbf{r}^{spec}(\bar{y})$  then writes

$$\mathbf{r}^{spec}(\bar{y}) = (1 - \alpha_{CO_2}) \cdot v_{CO_2}^{sg} - \hat{v}_{CO_2,1}$$
 (B.17)

The independent variable for the specification in Eq.(B.17) is the molar flow of the solvent make-up stream  $l_s^{MU}$ .

#### Estimation of the number of absorption stages

Note: Parts of this section have been published as Supporting Information to the work of Stavrou et al. [1].

For the simultaneous process and solvent optimization in the CoMT step an economic objective function is minimized. The degrees of freedom for the optimization are the pressure levels in the rich gas and desorption flash P<sup>rg</sup> and P<sup>des</sup>, the temperature of the lean solvent  $T^{lean}$  and the PC-SAFT molecular parameters of the solvent  $\overline{p} = \{m, \sigma, \varepsilon/k, \mu\}$ . In the current work the number of stages in the absorber is not considered as degree of freedom for the CoMT optimization problem (Eq. (2.2)), because such an optimization would require consideration of investment costs as part of the objective function. In order to define a reasonable number of equilibrium stages, a sensitivity analysis was carried out and the influence of the number of absorption stages on the CoMT optimization results was examined. Figures B.5 and B.6 show that the number of absorption stages has a low impact on the optimal molecular parameters of the solvent calculated in the CoMT step. Figures B.7 and B.8 show that increasing the number of absorption stages above 7 will only have a moderate effect on the optimal process conditions and the optimal value of the objective function. The absorber is therefore defined with a fixed number of  $N_{abs} = 7$  equilibrium stages.

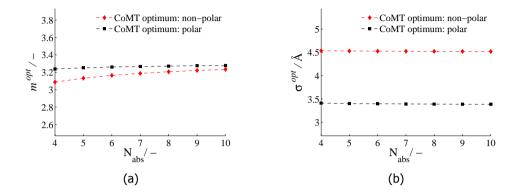


Figure B.5: Sensitivity of the optimal molecular parameters of the solvent: (a) segment number  $m^{opt}$  and (b) segment diameter  $\sigma^{opt}$  for varying number of absorption stages  $N_{abs}$  for non-polar (red diamond symbols) and polar molecules (black square symbols).

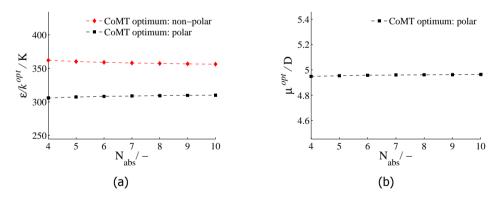


Figure B.6: Sensitivity of the optimal molecular parameters of the solvent: (a) dispersion energy  $\varepsilon/k^{opt}$  and (b) dipole moment  $\mu^{opt}$  for varying number of absorption stages  $N_{abs}$  for non-polar (red diamond symbols) and polar molecules (black square symbols).

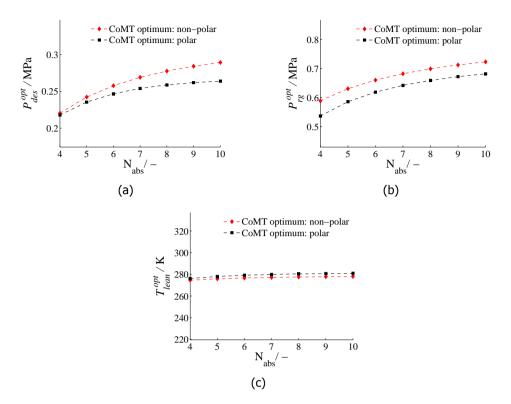


Figure B.7: Sensitivity of the optimal process conditions: (a) optimal pressure of the second desorption flash  $P_{des}^{opt}$ , (b) optimal pressure of the hydrogen-rich gas desorption flash  $P_{rg}^{opt}$  and (c) optimal temperature of the lean solvent  $T_{lean}^{opt}$  for varying number of absorption stages  $N_{abs}$  for non-polar (red diamond symbols) and polar molecules (black square symbols).

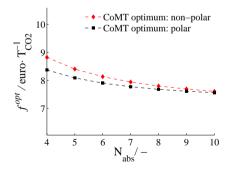


Figure B.8: Sensitivity of the optimal value of the objective function for varying number of absorption stages  $N_{abs}$  in the absorber for non-polar (red diamond symbols) and polar molecules (black square symbols).

#### **B.1.2.** Desorption

The desorption flash units are modeled using the equilibrium stage model described in Section B.1.1. For each flash unit the phase equilibrium problem is solved for the adiabatic-isobaric flash using the PQ-flash algorithm (Figure B.4). The solution of the phase equilibrium problem for the desorption flashes is, however, more simple than in the case of the absorber. The phase equilibrium problems for the two desorption flashes are solved independently and do not require the simultaneous convergence of internal variables.

#### **B.1.3.** Recycle streams

The examined process topology includes two recycle streams entering the absorber: the (vapor) recycle stream returning from the first desorption stage (rich gas flash) after compression and cooling (hereafter noted with the superscript 'rg') and the (liquid) recycle stream of the lean solvent after pumping and cooling (hereafter noted with the superscript 'lean') (Figure B.1). For both recycle streams the iterated variables are the component molar flows and the temperature

$$\overline{y}^{rg} := \{T^{rg}, \overline{v}^{rg}\}$$
 and  $\overline{y}^{lean} := \{T^{lean}, \overline{l}^{lean}\}$ 

The molar enthalpies of the recycle streams are calculated as function of the pressure and the iterated temperature and component molar flows

$$h^{\rm rg} = h^{\rm rg} \left( P^{\rm abs}, T^{\rm rg}, \overline{\nu}^{\rm rg} \right)$$
 and  $h^{\rm lean} = h^{\rm lean} \left( P^{\rm abs}, T^{\rm lean}, \overline{\nu}^{\rm lean} \right)$  (B.18)

In addition, calculated values for the component molar flows and the molar enthalpy of the rich gas recycle are obtained through process calculations for the units following the absorber. The equations of the residuals between the iterated and calculated values of the variables form the equation subsystem  $\mathbf{r}^{\mathrm{rec},\mathrm{rg}}(\bar{y})$  in (B.2)

$$\mathbf{r}^{\text{rec,rg}} = \begin{pmatrix} h^{\text{rg}} - \hat{h}^{\text{rg}} \\ v_1^{\text{rg}} - \hat{v}_1^{\text{rg}} \\ v_2^{\text{rg}} - \hat{v}_2^{\text{rg}} \\ \vdots \\ v_{N_c}^{\text{rg}} - \hat{v}_{N_c}^{\text{rg}} \end{pmatrix}$$
(B.19)

In a similar fashion, the equation subsystem  $\mathbf{r}^{\mathrm{rec},\mathrm{lean}}(\overline{y})$  is defined for the recycle stream of the lean solvent entering the absorber at stage 1 after pumping and cooling

$$\mathbf{r}^{\text{rec,lean}} = \begin{pmatrix} h^{\text{lean}} - \hat{h}^{\text{lean}} \\ l_1^{\text{lean}} - \hat{l}_1^{\text{lean}} \\ l_2^{\text{lean}} - \hat{l}_2^{\text{lean}} \\ \vdots \\ l_{N_c}^{\text{lean}} - \hat{l}_{N_c}^{\text{lean}} \end{pmatrix}$$
(B.20)

#### **B.1.4.** Pressure change units

#### Compressors

The vapor stream exiting the rich gas flash is recycled to the absorber and is compressed to the absorption pressure  $P^{abs}$ . The vapor stream that exits the desorption flash is being compressed to the pipeline pressure  $P^{ppl}$ .

In both cases polytropic, staged compressors are considered according to the model described in ref. [5]. The duty required for the gas compression  $\dot{W}_{\rm comp}$  (here defined as a positive stream) is

$$\dot{W}_{\text{comp}} = \left|\frac{1}{\eta_{\text{comp}}}N_{\text{comp}} \cdot P_{\text{in}} \cdot \dot{V}_{\text{in}} \cdot \left[1 - r_{\text{comp}}^{\left(\frac{n}{n-1}\right)}\right] \cdot \left(\frac{n}{n-1}\right)\right|$$
(B.21)

with  $\eta_{\rm comp}$  the efficiency of the compressor, n the polytropic exponent,  $N_{\rm comp}$  the number of compression stages,  $P_{\rm in}$  the inlet pressure,  $\dot{V}_{\rm in}$  the volumetric molar flow of the stream entering the compressor, and  $r_{\rm comp}$  the pressure ratio for minimum work for  $N_{\rm comp}$  stages.

Regarding compression both vapor streams are treated as ideal gas streams. Thereby, the polytropic exponent *n* is assumed to be approximately equal to the heat capacity ratio  $\gamma = \frac{c_p}{c_v}$ . The heat capacity ratio  $\gamma$  is held constant equal to 1.3, which is a fair assumption for gas streams containing mainly CO<sub>2</sub> and H<sub>2</sub> in the temperature range between 250 and 400 K [6].

The pressure ratio  $r_{\rm comp}$  is given by:

$$r_{\rm comp} = \left(\frac{P_{\rm out}}{P_{\rm in}}\right)^{1/N_{\rm comp}} \tag{B.22}$$

where  $P_{out}$  is the outlet pressure of the compressed stream ( $P^{abs}$  and  $P^{ppl}$  respectively). The inlet pressures  $P_{in}$  of both compressors ( $P^{rg}$  for the compressor after the rich gas flash and  $P^{des}$  for compressor after the desorption flash) are degrees of freedom in the simultaneous process and solvent optimization problem.

#### Pumps

The lean solvent stream is recycled to the absorber with a recirculating pump. The duty required by the pump  $\dot{W}_{pump}$  is

$$\dot{W}_{\text{pump}} = \frac{1}{\eta_{\text{pump}}} \cdot \dot{V}^{\text{RL}} \cdot (P_{\text{out}} - P_{\text{in}})$$
(B.23)

with  $\eta_{\text{pump}}$  the efficiency of the pump,  $\dot{V}^{\text{lean}}$  the volumetric molar flow of the lean solvent stream,  $P_{\text{out}}$  the pressure in the absorber  $P^{\text{abs}}$  and  $P_{\text{in}}$  the pressure of the desorption flash  $P^{\text{des}}$ .

The liquid stream exiting the desorption flash is mixed with the fresh solvent makeup to the lean solvent stream. The work required by the auxiliary pump of the makeup stream (Figure B.1) is calculated according to Eq.(B.23) for  $P_{\rm in} = 0.1013 \,\text{MPa}$ and  $P_{\rm out} = P^{\rm des}$ .

#### **B.1.5.** Heat exchange units

In the examined process topology heat exchangers are considered for the cooling of gas and liquid streams after compression and pumping respectively (Figure B.1).

#### Cooling of compressed gas streams

First, the rich gas recycle is compressed to the absorption pressure  $P^{\text{abs}}$  and mixed with the syngas stream. After compression and before mixing, the rich gas recycle has to be cooled to the temperature of the syngas stream  $T^{\text{sg}} = 313$  K. Second, the vapor stream exiting the desorption flash is compressed to the pipeline pressure and has to be cooled to the specified temperature for the pipeline gas  $T^{\text{ppl}}$  (here  $T^{\text{ppl}} = 313$  K). In both cases simple coolers with water as cooling medium are considered. No pressure drop is assumed. The required cooling duty  $\dot{Q}_{\text{cool,comp}}$  is

$$\dot{Q}_{\text{cool,comp}} = \dot{n} \cdot (h_{\text{cold}} - h_{\text{hot}})$$
 (B.24)

with  $\dot{n}$  as the molar flow of the compressed gas stream. For the cooling of the compressed rich gas stream

$$h_{\text{cold}} = h_{\text{cold}} \left( T^{\text{sg}}, P^{\text{abs}}, \overline{x}^{\text{v,RG}} \right)$$
$$h_{\text{hot}} = h_{\text{hot}} \left( T^{\text{comp}}_{\text{out}}, P^{\text{abs}}, \overline{x}^{\text{v,RG}} \right)$$

while for the cooling of the compressed gas stream after desorption

$$\begin{split} h_{\text{cold}} &= h_{\text{cold}} \left( T^{\text{ppl}}, P^{\text{ppl}}, \overline{x}^{\text{v,des}} \right) \\ h_{\text{hot}} &= h_{\text{hot}} \left( T^{\text{comp}}_{\text{out}}, P^{\text{ppl}}, \overline{x}^{\text{v,des}} \right). \end{split}$$

The required molar flow of the cooling medium  $\dot{n}^w_{\rm cool}$  (here liquid water) can be calculated as

$$\dot{n}_{\rm cool}^w = \frac{Q_{\rm cool,comp}}{\overline{c}_n^w \cdot \Delta T} \tag{B.25}$$

considering a minimum temperature difference  $\Delta T$  of 10 K for the heat transfer and an average specific heat capacity for water  $\overline{c}_p^w = 0.5 \cdot (c_p^w(283 \text{ K}) + c_p^w(293 \text{ K}))$ . In the current implementation, the values of  $c_p^w(T)$  were obtained from the DIPPR database [6].

#### Lean solvent cooling

The temperature of the lean solvent entering the absorber  $T^{\text{lean}}$  is an additional degree of freedom in the process and solvent optimization problem. For the cooling of the lean solvent to the temperature  $T^{\text{lean}}$  a vapor-compression refrigeration (VCR) system is considered. Here a simple VCR cycle is implemented (Figure B.9). Simple VCR cycles can provide cooling as low as typically 233 K [5] and possess an adequate operating range for the requirements of the optimization problem ( $T^{\text{lean}}_{lb} = 253$  K). The cooling of the lean solvent is provided in the evaporator. The required duty

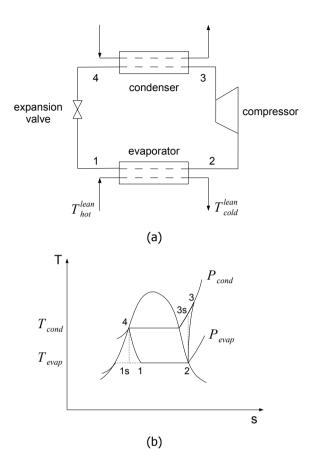


Figure B.9: Vapor-compression refrigeration cycle (VCR) [5, 7]. (a): Schematic of a simple VCR system. (b): Temperature-entropy diagram for the VCR system presented in (a). The vapor-liquid mixture of the refrigerant is evaporated at  $T_{evap}$  (process '1-2') and provides the required duty  $\dot{Q}_{cool,pump}$  to cool the lean solvent from  $T_{hot}^{lean}$  to  $T_{cold}^{lean} = T^{lean}$ . The refrigerant (saturated vapor at state '2') is compressed from  $P_{evap}$  to  $P_{cond}$  (process '2-3'). The refrigerant enters the condenser as superheated vapor (state '3'), where it is cooled and condensed at  $T_{cond}$  (process '3-4'). The (saturated) liquid refrigerant (state '4') is isenthalpically expanded to the pressure  $P_{evap}$  (process '4-1').

 $\dot{Q}_{\rm cool,pump}$  is

$$\dot{Q}_{\text{cool,pump}} = \dot{L}^{\text{lean}} \cdot \left(h_{\text{cold}}^{\text{lean}} - h_{\text{hot}}^{\text{lean}}\right)$$
 (B.26)

where  $\dot{L}^{\text{lean}}$  is the molar flow of the lean solvent stream,  $h_{\text{hot}}^{\text{lean}}$  is the molar enthalpy of the lean solvent stream entering the refrigeration system and  $h_{\text{cold}}^{\text{lean}}$  is the molar enthalpy of the cooled lean solvent stream.  $h_{\text{hot}}^{\text{lean}}$  is given by the energy balance for the pump

$$h_{\rm hot}^{\rm lean} = h_{\rm pump,in}^{\rm lean} + \frac{\dot{W}_{\rm pump}}{\dot{L}^{\rm lean}}.$$
 (B.27)

 $h_{\text{cold}}^{\text{lean}}$  is calculated using the PC-SAFT EoS (with QSPR estimations for the ideal gas specific heat capacity of the solvent  $c_{p,s}^{ig}$ ) as

$$h_{\text{cold}}^{\text{lean}} = h^{\text{lean}} \left( T_{\text{cold}}^{\text{lean}}, P^{\text{abs}}, \overline{x}^{\text{lean}} \right)$$

with  $T_{\text{cold}}^{\text{lean}} = T^{\text{lean}}$  and  $\overline{x}^{\text{lean}}$  the vector of component mole fractions of the lean solvent stream exiting the pump.

The compression duty  $\dot{W}_{refr}^{rev}$  for the reversible refrigeration process (process '1s-2-3s-4' in Figure B.9b) is

$$\dot{W}_{\rm refr}^{\rm rev} = \dot{Q}_{\rm cool,pump} \left( \frac{T_{\rm cond}}{T_{\rm evap}} - 1 \right)$$
 (B.28)

where  $T_{\rm cond}$  and  $T_{\rm evap}$  are the condensation and evaporation temperatures of the refrigerant. The coefficient of performance of the reversible process  $\rm COP_{rev}$  [5, 7] is

$$COP_{rev} = \frac{\dot{Q}_{cool,pump}}{\dot{W}_{refr}^{rev}}.$$
(B.29)

Accordingly, for the real process (process '1-2-3-4' in Figure B.9b) the coefficient of performance COP is

$$COP = \frac{Q_{cool,pump}}{\dot{W}_{refr}}$$
(B.30)

where  $\dot{W}_{refr}$  is the real compression duty. Here a constant ratio  $\frac{COP}{COP_{rev}}$  equal to 0.25 [8] is assumed. The real compression duty  $\dot{W}_{refr}$  is then calculated as

$$\dot{W}_{\text{refr}} = \dot{W}_{\text{refr}}^{\text{rev}} \cdot \left(\frac{\text{COP}}{\text{COP}_{\text{rev}}}\right)^{-1}.$$
 (B.31)

The temperature  $T_{evap}$  in Eq.(B.28) is defined by the temperature of the lean solvent  $T^{lean}$ , considering a minimum temperature difference  $\Delta T_{min}$  of 10 K in the evaporator:

$$T_{\rm evap} = T^{\rm lean} - \Delta T_{\rm min}. \tag{B.32}$$

In the condenser, the temperature  $T_{\text{cond}}$  at which heat is transferred from the refrigerant is set to 323.15 K. The constant value of  $T_{\text{cond}}$  is estimated as follows: For  $T_{\text{cond}} \ge T_{\text{evap}}$  should hold:

$$T_{\rm cond} \ge T^{\rm lean} - \Delta T_{\rm min}.$$
 (B.33)

The temperature  $T^{\text{lean}}$  is a degree of freedom in the process and solvent optimization problem. Thus,

$$(T_{\rm cond})_{\rm min} = T_{\rm ub}^{\rm lean} - \Delta T_{\rm min}$$
 (B.34)

where  $T_{ub}^{lean}$  is the upper bound of  $T^{lean}$  during the optimization, equal to 333.15 K.

## **B.2.** Definition of the objective function

Note: Parts of this Appendix have been published as Supporting Information to the work of Stavrou et al. [1].

The total specific cost per ton of captured CO<sub>2</sub> accounts for the specific cost contributions as: electricity demand, hydrogen loss, fresh solvent consumption and demand in cooling utilities, according to

$$f_{\text{tot}} = f_{\text{electr.demand}} + f_{\text{H2 loss}} + f_{\text{solvent loss}} + f_{\text{utilities}}$$
(B.35)

**Cost term for the electric energy demand,**  $f_{\text{electr.demand}}$ . The specific cost associated with the electricity demand  $f_{\text{electr.demand}}$  accounts for the costs of: the pump with duty  $\dot{W}_{\text{pump}}$ , the CO<sub>2</sub> compression to pipeline pressure with duty  $\dot{W}_{\text{comp.ppl}}$  and the rich gas compression with duty  $\dot{W}_{\text{comp.rg}}$  (in MW):

$$f_{\text{electr.demand}} = \frac{\left(\dot{W}_{\text{comp,ppl}} + \dot{W}_{\text{comp,rg}} + \dot{W}_{\text{pump}}\right) \cdot c_{\text{el}}}{\dot{m}_{\text{CO}_2,\text{capt}}}$$
(B.36)

where  $c_{el}$  is the electricity production price [9] equal to  $55 \notin Mwh$  and  $\dot{m}_{CO_2,capt}$  is the mass flow rate of CO<sub>2</sub> captured in absorber (in T/s).

The mass flow of captured CO<sub>2</sub>  $\dot{m}_{CO_2,capt}$  is expressed in terms of the CO<sub>2</sub>-capture rate  $\alpha_{CO_2}$  (Eq.(B.16)) from the absorber and the molar flow rate of CO<sub>2</sub> in the syngas  $\dot{n}_{CO_2,sg}$ , as

$$\dot{m}_{\rm CO_2,capt} = \alpha_{\rm CO_2} \cdot \dot{n}_{\rm CO_2,sg} \cdot M_{\rm CO_2}.$$
(B.37)

**Cost term for hydrogen loss,**  $f_{\rm H_2 loss}$ . The specific cost associated with the hydrogen unintentionally captured and stored with the CO<sub>2</sub>-rich stream is evaluated according to lost opportunity to produce electricity from the hydrogen with

$$f_{\rm H_2 loss} = \frac{\dot{n}_{\rm H2}^{\rm ppl} \cdot \Delta H_{H_2}^{\rm comb}}{\dot{m}_{\rm CO_2, capt}} \cdot \eta_{\rm el} \cdot c_{\rm el}$$
(B.38)

where  $\Delta H_{H_2}^{comb}$  is the enthalpy of combustion for hydrogen,  $\dot{n}_{H_2}^{ppl}$  is the molar flow of hydrogen in the vapor stream exiting the desorption flash (in kmol/sec) and  $\eta_{el}$  is the efficiency of power production for the combined cycle, once hydrogen is present at high pressure, set equal to 65 %.<sup>1</sup>

**Cost term for solvent loss,**  $f_{\text{solventloss}}$ . The specific cost of solvent loss  $f_{\text{solventloss}}$  measures the required fresh solvent make-up stream  $\dot{n}^{\text{MU}}$  (in kmol/sec) and accounts for the solvent loss both in the absorption and desorption stage:

$$f_{\text{solventloss}} = \frac{\dot{n}^{\text{MU}} \cdot v_{\text{S}}}{\dot{m}_{\text{CO}_2, \text{capt}}} \cdot c_{\text{bulk}}$$
(B.39)

<sup>1</sup>Note that  $\eta_{el}$  is set equal to 61 % for the case study presented in Chapter 4.

The specific molar volume of the solvent  $v_S$  is calculated with the PC-SAFT EoS at constant temperature (298.15 K) and pressure (0.1013 MPa). For the fresh solvent cost we consider an average price of high molecular weight chemicals of 4,000 e/T. We estimate the price for bulk chemicals  $c_{\text{bulk}}$  equal to  $4,040 \text{ }\text{e}/\text{m}^3$  using the molar volume of DEPG-5 by 298.15 K and 0.1013 MPa.

**Cost term for the utilities demand,**  $f_{\text{utilities}}$ . The specific cost of utilities  $f_{\text{utilities}}$  takes into account the electric energy demand for the operation of the cooling systems [5], with three contributions from the duties  $\dot{W}_{\text{aux-pump,rg}}$ ,  $\dot{W}_{\text{aux-pump,ppl}}$  and  $\dot{W}_{\text{refr}}$  according to

$$f_{\text{utilities}} = \frac{\left(\dot{W}_{\text{aux-pump,rg}} + \dot{W}_{\text{aux-pump,ppl}} + \dot{W}_{\text{refr}}\right)}{\dot{m}_{\text{CO}_2,\text{capt}}} \cdot c_{\text{el}}$$
(B.40)

The coolers, after the rich-gas compression and after the pipeline compression (section B.1.5) are operated with cooling water, so that the cost contribution is due to the electrical duty of the cooling-water pumps,  $\dot{W}_{aux-pump,rg}$  and  $\dot{W}_{aux-pump,ppl}$ , respectively. The required molar flow of cooling water is given by Eq.(B.25). The duty  $\dot{W}_{refr}$  required by the vapor-compression system for the lean solvent cooling is given by Eq.(B.26) to (B.31).

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# C

## Database of candidate components for solvent selection

This Appendix has been published as Supporting Information to the work of Stavrou et al. [1].

Table C.1 presents the 168 non-polar, non-associating components considered in our study as the mapping database of non-polar components. Table C.2 presents the 444 polar, non-associating components considered as the mapping database of polar components. For each component in the list we give its CAS number and name according to the DIPPR database [2].

Table C.1: List of the 168 non-polar, non-associating components comprising the database of non-polar components. Each component is denoted with its CAS number and name [2].

CAS Number	Name	CAS Number	Name
109660	n-PENTANE	291645	CYCLOHEPTANE
110543	n-HEXANE	292648	CYCLOOCTANE
107835	2-METHYLPENTANE	1072055	2,6-DIMETHYLHEPTANE
96140	3-METHYLPENTANE	6747323	2,2-DIMETHYL-3-ETHYLPENTANE
75832	2,2-DIMETHYLBUTANE	1068877	2,4-DIMETHYL-3-ETHYLPENTANE
79298	2,3-DIMETHYLBUTANE	646048	trans-2-PENTENE
142825	n-HEPTANE	4050457	trans-2-HEXENE
591764	2-METHYLHEXANE	3269528	trans-3-HEXENE
589344	3-METHYLHEXANE	3769231	4-METHYL-1-HEXENE
617787	3-ETHYLPENTANE	760214	2-ETHYL-1-BUTENE
590352	2,2-DIMETHYLPENTANE	563780	2,3-DIMETHYL-1-BUTENE
108087	2,4-DIMETHYLPENTANE	558372	3,3-DIMETHYL-1-BUTENE
562492	3,3-DIMETHYLPENTANE	563791	2,3-DIMETHYL-2-BUTENE
464062	2,2,3-TRIMETHYLBUTANE	3404715	2-ETHYL-1-PENTENE
111659	n-OCTANE	4686136	trans-2-HEPTENE

### C. Database of candidate components for solvent selection

592278	2-METHYLHEPTANE	4686147	trans-3-HEPTENE
589811	3-METHYLHEPTANE	4038044	3-ETHYL-1-PENTENE
589537	4-METHYLHEPTANE	3404613	3-METHYL-1-HEXENE
590738	2,2-DIMETHYLHEXANE	594569	2,3,3-TRIMETHYL-1-BUTENE
592132	2,5-DIMETHYLHEXANE	3389429	trans-2-OCTENE
563166	3,3-DIMETHYLHEXANE	107391	2,4,4-TRIMETHYL-1-PENTENE
609267	2-METHYL-3-ETHYLPENTANE	107404	2,4,4-TRIMETHYL-2-PENTENE
1067089	3-METHYL-3-ETHYLPENTANE	1632162	2-ETHYL-1-HEXENE
564023	2,2,3-TRIMETHYLPENTANE	5026766	6-METHYL-1-HEPTENE
540841	2,2,4-TRIMETHYLPENTANE	4919018	trans-3-OCTENE
560214	2,3,3-TRIMETHYLPENTANE	4850238	trans-4-OCTENE
565753	2,3,4-TRIMETHYLPENTANE	693890	1-METHYLCYCLOPENTENE
111842	n-NONANE	6746864	2,3-DIMETHYL-1-HEXENE
3522949	2,2,5-TRIMETHYLHEXANE	592450	1,4-HEXADIENE
7154805	3,3,5-TRIMETHYLHEPTANE	706310	1,5,9-CYCLODODECATRIENE
6747301	2,4,4-TRIMETHYLHEXANE	764136	2,5-DIMETHYL-2,4-HEXADIENE
1067205	3,3-DIETHYLPENTANE	629209	1,3,5,7-CYCLOOCTATETRAENE
7154792	2,2,3,3-TETRAMETHYLPENTANE	928494	3-HEXYNE
1186534	2,2,3,4-TETRAMETHYLPENTANE	71432	BENZENE
1070877	2,2,4,4-TETRAMETHYLPENTANE	106423	p-XYLENE
6747389	2,3,3,4-TETRAMETHYLPENTANE	622968	p-ETHYLTOLUENE
111013	SQUALANE	108678	MESITYLENE
124185	n-DECANE	99876	p-CYMENE
3475815	2,2,3,3-TETRAMETHYLHEXANE	105055	p-DIETHYLBENZENE
1071814	2,2,5,5-TETRAMETHYLHEXANE	877441	1,2,4-TRIETHYLBENZENE
3178221	tert-BUTYLCYCLOHEXANE	1078713	n-HEPTYLBENZENE
1120214	n-UNDECANE	104723	n-DECYLBENZENE
112403	n-DODECANE	538681	n-PENTYLBENZENE
629505	n-TRIDECANE	1077163	n-HEXYLBENZENE
629594	n-TETRADECANE	2189608	n-OCTYLBENZENE
629629	n-PENTADECANE	1081772	n-NONYLBENZENE
544763	n-HEXADECANE	6742547	n-UNDECYLBENZENE
629787	n-HEPTADECANE	123024	n-TRIDECYLBENZENE
5911046	3-METHYLNONANE	1459105	n-TETRADECYLBENZENE
871830	2-METHYLNONANE	123013	n-DODECYLBENZENE
7301949	4-METHYLNONANE	1074551	1-METHYL-4-n-PROPYLBENZENE
5869859	5-METHYLNONANE	2765186	1-n-PROPYLNAPHTHALENE
3221612	2-METHYLOCTANE	939275	2-ETHYLNAPHTHALENE
2216333	3-METHYLOCTANE	7058017	sec-BUTYLCYCLOHEXANE
2216344	4-METHYLOCTANE	123911	1,4-DIOXANE
5869804	3-ETHYLHEPTANE	93969	BIS(alpha-METHYLBENZYL) ETHER
1071267	2,2-DIMETHYLHEPTANE	56235	CARBON TETRACHLORIDE
287923	CYCLOPENTANE	110576	1,4-DICHLORO-trans-2-BUTENE
96377	METHYLCYCLOPENTANE	127184	TETRACHLOROETHYLENE
1640897	ETHYLCYCLOPENTANE	156605	trans-1,2-DICHLOROETHYLENE
1638262	1,1-DIMETHYLCYCLOPENTANE	355420	PERFLUORO-n-HEXANE
1192183	cis-1,2-DIMETHYLCYCLOPENTANE	509148	TETRANITROMETHANE
822504	trans-1,2-DIMETHYLCYCLOPENTANE	26047	TETRACHLOROSILANE
2532583	cis-1,3-DIMETHYLCYCLOPENTANE	75150	CARBON DISULFIDE
2040962	n-PROPYLCYCLOPENTANE	7146603	2,3-DIMETHYLOCTANE
3875512	ISOPROPYLCYCLOPENTANE	4032944	2,4-DIMETHYLOCTANE
6747505	1-METHYL-1-ETHYLCYCLOPENTANE	5869893	2,5-DIMETHYLOCTANE

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2040951	n-BUTYLCYCLOPENTANE	2051301	2,6-DIMETHYLOCTANE
			•
110827	CYCLOHEXANE	1072168	2,7-DIMETHYLOCTANE
108872	METHYLCYCLOHEXANE	3524730	5-METHYL-1-HEXENE
1678917	ETHYLCYCLOHEXANE	5870107	2-METHYL-1-HEPTENE
590669	1,1-DIMETHYLCYCLOHEXANE	2131182	n-PENTADECYLBENZENE
6876239	trans-1,2-DIMETHYLCYCLOHEXANE	678262	PERFLUORO-n-PENTANE
638040	cis-1,3-DIMETHYLCYCLOHEXANE	335579	PERFLUORO-n-HEPTANE
2207036	trans-1,3-DIMETHYLCYCLOHEXANE	7550450	TITANIUM TETRACHLORIDE
624293	cis-1,4-DIMETHYLCYCLOHEXANE	2980714	2-METHYL-1-NONENE
1795262	1-trans-3,5-TRIMETHYLCYCLOHEXANE	111966	DIETHYLENE GLYCOL
			DIMETHYL ETHER
1678928	n-PROPYLCYCLOHEXANE	· 112492	TRIETHYLENE GLYCOL
			DIMETHYL ETHER
696297	ISOPROPYLCYCLOHEXANE	· 143248	TETRAETHYLENE GLYCOL
			DIMETHYL ETHER
1678939	n-BUTYLCYCLOHEXANE	1191873	PENTAETHYLENE GLYCOL
			DIMETHYL ETHER
493016	cis-DECAHYDRONAPHTHALENE	1072408	HEXAETHYLENE GLYCOL
			DIMETHYL ETHER
493027	trans-DECAHYDRONAPHTHALENE	1191919	HEPTAETHYLENE GLYCOL
			DIMETHYL ETHER
92513	BICYCLOHEXYL	n.a	OCTAETHYLENE GLYCOL
			DIMETHYL ETHER
1795160	n-DECYLCYCLOHEXANE	n.a.	NONAETHYLENE GLYCOL
			DIMETHYL ETHER

Table C.2: List of the 444 polar, non-associating components comprising the database of polar compo
nents. Each component is denoted with its CAS number and name [2].

CAS Number	Name	CAS Number	Name
78784	ISOPENTANE	110009	FURAN
1678984	iso-BUTYLCYCLOHEXANE	109999	TETRAHYDROFURAN
109671	1-PENTENE	61015	cis-1,3-DICHLOROPROPENE
627203	cis-2-PENTENE	61026	trans-1,3-DICHLOROPROPENE
563462	2-METHYL-1-BUTENE	628762	1,5-DICHLOROPENTANE
513359	2-METHYL-2-BUTENE	75092	DICHLOROMETHANE
592416	1-HEXENE	67663	CHLOROFORM
7688213	cis-2-HEXENE	75343	1,1-DICHLOROETHANE
7642093	cis-3-HEXENE	107062	1,2-DICHLOROETHANE
763291	2-METHYL-1-PENTENE	79005	1,1,2-TRICHLOROETHANE
760203	3-METHYL-1-PENTENE	78875	1,2-DICHLOROPROPANE
691372	4-METHYL-1-PENTENE	71556	1,1,1-TRICHLOROETHANE
625274	2-METHYL-2-PENTENE	630206	1,1,1,2-TETRACHLOROETHANE
922623	3-METHYL-cis-2-PENTENE	79345	1,1,2,2-TETRACHLOROETHANE
691383	4-METHYL-cis-2-PENTENE	75296	ISOPROPYL CHLORIDE
674760	4-METHYL-trans-2-PENTENE	96184	1,2,3-TRICHLOROPROPANE
592767	1-HEPTENE	513360	ISOBUTYL CHLORIDE
6443921	cis-2-HEPTENE	507200	tert-BUTYL CHLORIDE
6094026	2-METHYL-1-HEXENE	616217	1,2-DICHLOROBUTANE
7642106	cis-3-HEPTENE	79016	TRICHLOROETHYLENE

		1	
111660	1-OCTENE	107051	3-CHLOROPROPENE
124118	1-NONENE	87683	HEXACHLORO-1,3-BUTADIENE
872059	1-DECENE	100447	BENZYL CHLORIDE
821954	1-UNDECENE	108907	MONOCHLOROBENZENE
112414	1-DODECENE	95501	o-DICHLOROBENZENE
2437561	1-TRIDECENE	541731	m-DICHLOROBENZENE
1120361	1-TETRADECENE	95498	o-CHLOROTOLUENE
3360617	1-PENTADECENE	106434	p-CHLOROTOLUENE
629732	1-HEXADECENE	156592	cis-1,2-DICHLOROETHYLENE
112889	1-OCTADECENE	126998	CHLOROPRENE
142290	CYCLOPENTENE	540545	n-PROPYL CHLORIDE
110838	CYCLOHEXENE	109693	n-BUTYL CHLORIDE
628922	CYCLOHEPTENE	78864	sec-BUTYL CHLORIDE
931884	CYCLOOCTENE	543599	1-CHLOROPENTANE
7642048	cis-2-OCTENE	76017	PENTACHLOROETHANE
7642151	cis-4-OCTENE	75354	1,1-DICHLOROETHYLENE
4850227	cis-3-OCTENE	124732	1,2-DIBROMO-
			TETRAFLUOROETHANE
6765395	1-HEPTADECENE	74964	BROMOETHANE
5989275	d-LIMONENE	79276	1,1,2,2-TETRABROMOETHANE
1574410	cis-1,3-PENTADIENE	106945	1-BROMOPROPANE
2004708	trans-1,3-PENTADIENE	75263	2-BROMOPROPANE
591935	1,4-PENTADIENE	109659	1-BROMOBUTANE
78795	ISOPRENE	629049	1-BROMOHEPTANE
598254	3-METHYL-1,2-BUTADIENE	557915	1,1-DIBROMOETHANE
5194514	trans,trans-2,4-HEXADIENE	354585	1,1,1-TRICHLORO-
			TRIFLUOROETHANE
542927	CYCLOPENTADIENE	108861	BROMOBENZENE
513815	2,3-DIMETHYL-1,3-BUTADIENE	74884	METHYL IODIDE
592574	1,3-CYCLOHEXADIENE	75036	ETHYL IODIDE
628411	1,4-CYCLOHEXADIENE	107084	n-PROPYL IODIDE
111784	1,5-CYCLOOCTADIENE	75309	ISOPROPYL IODIDE
237347	trans-1,3-HEXADIENE	306832	2,2-DICHLORO-
237317		500052	1,1,1-TRIFLUOROETHANE
1647161	1,9-DECADIENE	91667	N,N-DIETHYLANILINE
503173	DIMETHYLACETYLENE	96548	N-METHYLPYRROLE
627190	1-PENTYNE	120945	N-METHYLPYRROLIDINE
693027	1-HEXYNE	110861	PYRIDINE
629050	1-OCTYNE	121697	N,N-DIMETHYLANILINE
598232	3-METHYL-1-BUTYNE	109068	2-METHYLPYRIDINE
108883	TOLUENE		ETHYL MERCAPTAN
		75081	
100414		107039	n-PROPYL MERCAPTAN
95476	o-XYLENE	75661	tert-BUTYL MERCAPTAN
108383	m-XYLENE	513440	ISOBUTYL MERCAPTAN
103651	n-PROPYLBENZENE	513531	SEC-BUTYL MERCAPTAN
98828	CUMENE	111319	n-HEXYL MERCAPTAN
611143	o-ETHYLTOLUENE	1455216	n-NONYL MERCAPTAN
620144	m-ETHYLTOLUENE	111886	n-OCTYL MERCAPTAN
526738	1,2,3-TRIMETHYLBENZENE	75332	ISOPROPYL MERCAPTAN
95636	1,2,4-TRIMETHYLBENZENE	1569693	CYCLOHEXYL MERCAPTAN
104518	n-BUTYLBENZENE	100538	BENZYL MERCAPTAN
538932	ISOBUTYLBENZENE	624895	METHYL ETHYL SULFIDE

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135988	sec-BUTYLBENZENE	3877154	METHYL n-PROPYL SULFIDE
98066	tert-BUTYLBENZENE	6163640	METHYL t-BUTYL SULFIDE
527844	o-CYMENE	111477	DI-n-PROPYL SULFIDE
535773	m-CYMENE	352932	DIETHYL SULFIDE
141935	m-DIETHYLBENZENE	3698940	ETHYL n-OCTYL SULFIDE
488233	1,2,3,4-TETRAMETHYLBENZENE	75183	DIMETHYL SULFIDE
7364194	p-tert-BUTYL ETHYLBENZENE	110021	THIOPHENE
717748	1,3,5-TRIISOPROPYLBENZENE	110816	DIETHYL DISULFIDE
605016	PENTAETHYLBENZENE	5332525	UNDECYL MERCAPTAN
934747	5-ETHYL-m-XYLENE	143102	n-DECYL MERCAPTAN
1074175	1-METHYL-2-n-PROPYLBENZENE	110667	n-PENTYL MERCAPTAN
1827870	1,2,4-TRIMETHYL-3-ETHYLBENZENE	624920	DIMETHYL DISULFIDE
7851273	1,2,4-TRIMETHYL-5-ETHYLBENZENE	629196	DI-n-PROPYL DISULFIDE
100425	STYRENE	112550	n-DODECYL MERCAPTAN
611154	o-METHYLSTYRENE	1639094	n-HEPTYL MERCAPTAN
100801	m-METHYLSTYRENE	109795	n-BUTYL MERCAPTAN
7564638	o-ETHYLSTYRENE	108985	PHENYL MERCAPTAN
7525624	m-ETHYLSTYRENE	110010	TETRAHYDROTHIOPHENE
622979	p-METHYLSTYRENE	67685	DIMETHYL SULFOXIDE
98839	alpha-METHYLSTYRENE	75365	ACETYL CHLORIDE
536743	ETHYNYLBENZENE	79049	CHLOROACETYL CHLORIDE
766905	cis-1-PROPENYLBENZENE	76028	TRICHLOROACETYL CHLORIDE
1746232	p-tert-BUTYLSTYRENE	98884	BENZOYL CHLORIDE
90120	1-METHYLNAPHTHALENE	98566	p-CHLOROBENZOTRIFLUORIDE
119642	1,2,3,4-TETRAHYDRONAPHTHALENE	462066	FLUOROBENZENE
95136	INDENE	107302	CHLOROMETHYL METHYL ETHER
496117	INDANE	392563	HEXAFLUOROBENZENE
123386	PROPANAL	111444	DI(2-CHLOROETHYL)ETHER
123728	BUTANAL	97938	TRIETHYL ALUMINUM
78842	2-METHYLPROPANAL	3268493	3-(METHYLMERCAPTO)PROPANAL
110623	PENTANAL	68122	N,N-DIMETHYLFORMAMIDE
111717	HEPTANAL	106898	alpha-EPICHLOROHYDRIN
66251	HEXANAL	98011	FURFURAL
124130	OCTANAL	108656	PROPYLENE GLYCOL
			MONOMETHYL ETHER ACETATE
124196	NONANAL	7719122	PHOSPHORUS TRICHLORIDE
623369	2-METHYL-2-PENTENAL	25873	PHOSPHORUS OXYCHLORIDE
112312	DECANAL	25782	TRICHLOROSILANE
112447	UNDECANAL	7791255	SULFUR CHLORIDE
112549	DODECANAL	7719097	THIONIL CHLORID
486198	TRIDECANAL	107460	HEXAMETHYLDISILOXANE
96173	2-METHYLBUTYRALDEHYDE	141639	DODECAMETHYLPENTASILOXANE
590863	3-METHYLBUTYRALDEHYDE	124709	METHYL VINYL DICHLOROSILANE
107028	ACROLEIN	4814096	[3-(MERCAPTO)PROPYL]
			TRIETHOXYSILANE
123739	trans-CROTONALDEHYDE	556672	OCTAMETHYLCYCLOTETRASILOXANE
93538	2-PHENYLPROPIONALDEHYDE	7789200	DEUTERIUM OXIDE
100527	BENZALDEHYDE	925780	3-NONANONE
123637	PARALDEHYDE	616126	3-METHYL-trans-2-PENTENE
67641	ACETONE	616024	METHYL MALEIC ANHYDRIDE
78933	METHYL ETHYL KETONE	589402	sec-BUTYL FORMATE
96220	3-PENTANONE	540885	tert-BUTYL ACETATE
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### C. Database of candidate components for solvent selection

108101	METHYL ISOBUTYL KETONE	547637	METHYL ISOBUTYRATE
565617	3-METHYL-2-PENTANONE	97621	ETHYL ISOBUTYRATE
109499	5-HEXEN-2-ONE	622457	CYCLOHEXYL ACETATE
106354	3-HEPTANONE	108327	PROPYLENE CARBONATE
123193	4-HEPTANONE	84662	DIETHYL PHTHALATE
589388	3-HEXANONE	131113	DIMETHYL PHTHALATE
107879	2-PENTANONE	123251	DIETHYL SUCCINATE
563804	METHYL ISOPROPYL KETONE	111820	METHYL DODECANOATE
591786	2-HEXANONE	141059	DIETHYL MALEATE
110430	2-HEPTANONE	624486	DIMETHYL MALEATE
141797	MESITYL OXIDE	2998085	sec-BUTYL ACRYLATE
75978	3,3-DIMETHYL-2-BUTANONE	616386	DIMETHYL CARBONATE
108838	DIISOBUTYL KETONE	2315686	n-PROPYL BENZOATE
565800	DIISOPROPYL KETONE	628557	DIISOBUTYL ETHER
872504	N-METHYL-2-PYRROLIDONE	628717	1-HEPTYNE
624420	ETHYL ISOAMYL KETONE	462953	ETHYLAL
502567	5-NONANONE	629141	1,2-DIETHOXYETHANE
821556	2-NONANONE	1191997	2,3-DIHYDROFURAN
120923	CYCLOPENTANONE	8970440	1-ETHYL-2-ISOPROPYLBENZENE
108941	CYCLOHEXANONE	142289	1,3-DICHLOROPROPANE
111137	2-OCTANONE	78886	2,3-DICHLOROPROPENE
98862	ACETOPHENONE	98088	BENZOTRIFLUORIDE
57578	beta-PROPIOLACTONE	74953	DIBROMOMETHANE
108292	gamma-VALEROLACTONE	74975	BROMOCHLOROMETHANE
565695	ETHYL ISOPROPYL KETONE	151677	HALOTHANE
814788	METHYL ISOPROPENYL KETONE	75627	BROMOTRICHLOROMETHANE
108247	ACETIC ANHYDRIDE	354234	1,2-DICHLORO-
			1,1,2-TRIFLUOROETHANE
123626	PROPIONIC ANHYDRIDE	1717006	1,1-DICHLORO-
			1-FLUOROETHANE
106310	BUTYRIC ANHYDRIDE	76120	1,1,2,2-TETRACHLORO-
			DIFLUOROETHANE
107313	METHYL FORMATE	638459	n-HEXYL IODIDE
109944	ETHYL FORMATE	542698	n-BUTYL IODIDE
110747	n-PROPYL FORMATE	108758	2,4,6-TRIMETHYLPYRIDINE
592847	n-BUTYL FORMATE	108485	2,6-DIMETHYLPYRIDINE
542552	ISOBUTYL FORMATE	108996	3-METHYLPYRIDINE
638493	n-PENTYL FORMATE	108894	4-METHYLPYRIDINE
79209	METHYL ACETATE	420122	THIACYCLOPROPANE
141786	ETHYL ACETATE	628295	METHYL n-BUTYL SULFIDE
109604	n-PROPYL ACETATE	4290927	ETHYL t-BUTYL SULFIDE
123864	n-BUTYL ACETATE	287274	TRIMETHYLENE SULFIDE
110190	ISOBUTYL ACETATE	554143	2-METHYLTHIOPHENE
123922	ISOPENTYL ACETATE	616444	3-METHYLTHIOPHENE
108214	ISOPROPYL ACETATE	127195	N,N-DIMETHYLACETAMIDE
105464	sec-BUTYL ACETATE	105395	ETHYLCHLOROACETATE
108054	VINYL ACETATE	4394858	4-FORMYLMORPHOLINE
554121	METHYL PROPIONATE	1184583	DIMETHYLALUMINUM CHLORIDE
105373	ETHYL PROPIONATE	107517	OCTAMETHYLTRISILOXANE
106365	n-PROPYL PROPIONATE	556694	OCTADECAMETHYLOCTASILOXANE
590012	n-BUTYL PROPIONATE	631367	TETRAETHYL SILANE
105668	n-PROPYL n-BUTYRATE	541015	HEXADECAMETHYLHEPTASILOXANE
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623427	METHYL n-BUTYRATE	96106	DIETHYLALUMINUM CHLORIDE
105544	ETHYL n-BUTYRATE	97723	ISOBUTYRIC ANHYDRIDE
96333	METHYL ACRYLATE	6737117	sec-BUTENYL ACETATE
140885	ETHYL ACRYLATE	3938952	ETHYL TRIMETHYL ACETATE
141322	n-BUTYL ACRYLATE	106650	DIMETHYL SUCCINATE
108645	ETHYL ISOVALERATE	1795091	2-METHYLTHIACYCLOPENTANE
80626	METHYL METHACRYLATE	1551322	2-ETHYL-TETRAHYDROTHIOPHENE
628637	n-PENTYL ACETATE	872559	2-ETHYLTHIOPHENE
103093	2-ETHYLHEXYL ACETATE	1551275	2-n-PROPYLTHIOPHENE
140114	BENZYL ACETATE	638028	2,5-DIMETHYLTHIOPHENE
659701	ISOPENTYL ISOVALERATE	453317	ETHYL PROPYL DISULFIDE
142927	n-HEXYL ACETATE	100685	METHYL PHENYL SULFIDE
120514	BENZYL BENZOATE	544401	DI-n-BUTYL SULFIDE
136607	n-BUTYL BENZOATE	4110503	ETHYL PROPYL SULFIDE
112061	n-HEPTYL ACETATE	143226	2-(2-(2-BUTOXYETHOXY)ETHOXY) ETHANOL
112141	n-OCTYL ACETATE	124630	METHANESULFONYL CHLORIDE
112174	n-DECYL ACETATE	585079	tert-BUTYL METHACRYLATE
131168	DI-n-PROPYL PHTHALATE	7784341	ARSENIC (III) CHLORIDE
109217	n-BUTYL n-BUTYRATE	78104	TETRAETHOXYSILANE
103117	2-ETHYLHEXYL ACRYLATE	75547	METHYL DICHLOROSILANE
97869	ISOBUTYL METHACRYLATE	75796	METHYL TRICHLOROSILANE
97881	n-BUTYL METHACRYLATE	75945	VINYLTRICHLOROSILANE
93583	METHYL BENZOATE	1067534	TRIS(2-METHOXYETHOXY)VINYLSILANE
93890	ETHYL BENZOATE	681845	METHYL SILICATE
105588	DIETHYL CARBONATE	545990	SULFUR DICHLORIDE
95921	DIETHYL OXALATE	75241	TRIMETHYLALUMINUM
105533	DIETHYL MALONATE	78002	TETRAETHYL LEAD
110429	METHYL DECANOATE	1066359	DIMETHYLCHLOROSILANE
110270	ISOPROPYL MYRISTATE	75774	TRIMETHYLCHLOROSILANE
60297	DIETHYL ETHER	75785	DIMETHYLDICHLOROSILANE
108203	DIISOPROPYL ETHER	541026	DECAMETHYLCYCLOPENTASILOXANE
142961	DI-n-BUTYL ETHER	540976	DODECAMETHYLCYCLOHEXASILOXANE
1634044	METHYL tert-BUTYL ETHER	80104	DIPHENYLDICHLOROSILANE
557175	METHYL n-PROPYL ETHER	115219	ETHYLTRICHLOROSILANE
598538	METHYL ISOPROPYL ETHER	1719535	DICHLORODIETHYLSILANE
628284	METHYL n-BUTYL ETHER	75876	TRICHLOROACETALDEHYDE
628320	ETHYL PROPYL ETHER	78400	TRIETHYL PHOSPHATE
104461	ANETHOLE	2768027	VINYLTRIMETHOXYSILANE
693652	DI-n-PENTYL ETHER	2487903	TRIMETHOXYSILANE
637923	tert-BUTYL ETHYL ETHER	1112396	DIMETHYLDIMETHOXYSILANE
919948	ETHYL tert-PENTYL ETHER	98135	PHENYLTRICHLOROSILANE
109875	METHYLAL	149746	PHENYLMETHYLDICHLOROSILANE
105577	ACETAL	107528	TETRADECAMETHYLHEXASILOXANE
75569	1,2-PROPYLENE OXIDE	141628	DECAMETHYLTETRASILOXANE
109922	ETHYL VINYL ETHER	625605	ETHYL THIOLACETATE
111433	DI-n-PROPYL ETHER	77781	DIMETHYL SULFATE
628819	n-BUTYL ETHYL ETHER	64675	DIETHYL SULFATE
110714	1,2-DIMETHOXYETHANE	111159	ETHOXYETHYL ACETATE
100663	ANISOLE	141979	ETHYL ACETOACETATE
103731	PHENETOLE	594445	ETHANESULFONYL CHLORIDE
103504	DIBENZYL ETHER	540636	1,2-ETHANEDITHIOL

534156         1,1-DIMETHOXYETHANE         108225         METHYLVINYL ACETATE           1708298         2,5-DIHYDROFURAN         5878193         METHOXYACETONE	9177049	1-METHYL-3-(METHYLETHOXY)BENZENE	763699	ETHYL-3-ETHOXYPROPIONATE
1708298 2,5-DIHYDROFURAN 5878193 METHOXYACETONE	534156	1,1-DIMETHOXYETHANE	108225	METHYLVINYL ACETATE
,	1708298	2,5-DIHYDROFURAN	5878193	METHOXYACETONE

### References

- M. Stavrou, M. Lampe, A. Bardow, and J. Gross, *Continuous molecular targeting-computer-aided molecular design (CoMT-CAMD) for simultaneous process and solvent design for* CO<sub>2</sub> *capture*, Ind. Eng. Chem. Res. **53**, 18029 (2014).
- [2] AIChE-DECHEMA, Pure Component Database DIPPR-801, Tech. Rep. (AIChE-DECHEMA, 2011).

# D

# QSPR models for the prediction of $c_p^{ig}$ and molar mass

The size of the training sets and the squared correlation coefficients  $R^2$  of the QSPR multivariable regression model for the prediction of  $c_p^{ig}$  and of the molar mass M are given in Table D.1.

Table D.1: QSPR multivariable regression model for the prediction of molar mass and  $c_p^{ig}$ : Size of the training set (number of components) used to adjust the coefficients of the QSPR-model and the resulting squared correlation coefficient  $R^2$  for non-polar and polar components.

	non-polar components	polar components
Ideal gas s	specific heat capacity $c_p^{ig}$ (	by <i>T</i> = 300 K
training set size	156	525
$R^2$	0.997	0.987
	Molar mass M	
training set size	168	445
$R^2$	0.966	0.932

Tables D.2 and D.3 present the QSPR model coefficients used in Eq.(2.8) and Eq.(2.7) of Chapter 2 for the prediction of the ideal gas heat capacity  $c_p^{ig}$  and of the molar mass M, respectively. The coefficients of the QSPR models were adjusted for the PC-SAFT pure component database, as described in Chapter 2.

QSPR coefficients - Ideal gas specific heat capacity $c_p^{ig}$ by $T = 300 \text{ K}$		
	non-polar components	polar components
$\gamma_0$	-16955.243	-20257.909
$\gamma_1$	-3829.1124	13051.796
$\gamma_2$	1279.9093	914.33815
$\gamma_3$	-327.68470	-227.59750

Table D.2: Coefficients of the QSPR model for the prediction of the ideal gas heat capacity  $c_p^{ig}$  given by Eq.(2.8).

Table D.3: Coefficients of the QSPR model for the prediction of the molar mass M given by Eq.(2.7).

	QSPR coefficients - Mo	olar mass M
	non-polar components	polar components
$\beta_1$	0.0978500	0.0011995
$\beta_2$	-0.0020034	0.5673782
$\beta_3$	0.0006309	0.0001554
$\beta_4$	0	0.0308482

# E

# QSPR models for the prediction of *k*<sub>*ij*</sub>

The contents of Appendices E.1 to E.3 are published as Supporting Information to the work of Stavrou et al. [1].

### **E.1.** Comparison with k<sub>ij</sub> predictions based on London's dispersive theory

Table E.1: Mixtures of two non-associating, non-polar components (group 1): For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the value of  $k_{ij}$  fitted to experimental data ( $k_{ij}^{fit}$ ), the value of  $k_{ij}$  prediction with the QSPR model ( $k_{ij}^{QSPR}$ ) and the value of  $k_{ij}$  prediction with the Hudson-McCoubrey expression[2] ( $k_{ij}(I, \sigma)$ ).

		Group 1 (nA	nP - nAnP)				
#	component <i>i</i>	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	$k_{ij}(I,\sigma)$
1	3-METHYLPENTANE	OCTANE	96140	111659	-0.0003	0.0000	0.0001
2	CARBON-MONOXIDE	PROPANE	630080	74986	0.0517	0.0622	0.0161
3	CARBON-MONOXIDE	METHANE	630080	74828	0.0287	0.0301	0.0141
4	CARBON-MONOXIDE	ETHANE	630080	74840	0.0258	0.0462	0.0094
5	PROPANE	METHYLCYCLOHEXANE	74986	108872	0.0102	0.0153	0.0095
6	ETHANE	METHYLCYCLOHEXANE	74840	108872	0.0169	0.0226	0.0162
7	METHANE	PROPANE	74828	74986	0.0012	0.0082	0.0029
8	METHANE	METHYLCYCLOHEXANE	74828	108872	0.0338	0.0357	0.0133
9	METHANE	ETHANE	74828	74840	-0.0046	0.0041	0.0029
10	PROPANE	CYCLOHEXANE	74986	110827	0.0141	0.0119	0.0042
11	METHANE	HEXADECANE	74828	544763	0.0545	0.0259	0.0000
12	METHANE	OCTANE	74828	111659	0.0174	0.0198	0.0088
13	METHANE	ETHYLCYCLOHEXANE	74828	1678917	0.0278	0.0436	0.0174
14	METHANE	HEXANE	74828	110543	0.0135	0.0174	0.0064
15	PROPANE	ISOBUTANE	74986	75285	-0.0048	0.0022	0.0012

17         ETHANE         HEXANE         74840         110543         0.0066         0.0095         0.0065           18         HEXANE         HEXADECANE         110543         544763         0.0011         0.0032         0.0000           19         HEXANE         OCTANE         110543         544763         0.0011         0.0032         0.0000           20         ETHANE         OCTANE         110543         111659         -0.0130         0.0009         0.0002           20         ETHANE         OCTANE         74840         111659         0.0174         0.0112         0.0089           21         METHANE         BUTANE         74828         106978         0.0014         0.0126         0.0040           22         METHANE         NONANE         74828         111842         0.0148         0.0204         0.0095           23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110827         108057         0.0016	16	HEPTANE	METHYLCYCLOHEXANE	142825	108872	0.0021	0.0065	0.0020
19         HEXANE         OCTANE         110543         111659         -0.0030         0.0009         0.0022           20         ETHANE         OCTANE         74840         111659         0.0174         0.0112         0.0089           21         METHANE         BUTANE         74828         106978         0.0014         0.0126         0.0040           22         METHANE         NONANE         74828         111842         0.0148         0.0204         0.0095           23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0011	17	ETHANE	HEXANE	74840	110543	0.0066	0.0095	0.0065
20         ETHANE         OCTANE         74840         111659         0.0174         0.0112         0.0089           21         METHANE         BUTANE         74828         106978         0.0014         0.0126         0.0040           22         METHANE         NONANE         74828         111842         0.0148         0.0204         0.0095           23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0011	18	HEXANE	HEXADECANE	110543	544763	0.0011	0.0032	0.0000
21         METHANE         BUTANE         74828         106978         0.0014         0.0126         0.0040           22         METHANE         NONANE         74828         111842         0.0148         0.0204         0.0095           23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.00011	19	HEXANE	OCTANE	110543	111659	-0.0030	0.0009	0.0002
22         METHANE         NONANE         74828         111842         0.0148         0.0204         0.0095           23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0001	20	ETHANE	OCTANE	74840	111659	0.0174	0.0112	0.0089
23         CYCLOHEXANE         METHYLCYCLOHEXANE         110827         108872         0.0016         0.0012           24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0001	21	METHANE	BUTANE	74828	106978	0.0014	0.0126	0.0040
24         METHANE         HEPTANE         74828         142825         0.0112         0.0180         0.0076           25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0001	22	METHANE	NONANE	74828	111842	0.0148	0.0204	0.0095
25         HEXANE         CYCLOHEXANE         110543         110827         0.0016         0.0045         0.0002           26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0001	23	CYCLOHEXANE	METHYLCYCLOHEXANE	110827	108872	0.0016	0.0016	0.0012
26         2-METHYLPENTANE         OCTANE         107835         111659         -0.0019         0.0005         0.0001	24	METHANE	HEPTANE	74828	142825	0.0112	0.0180	0.0076
	25	HEXANE	CYCLOHEXANE	110543	110827	0.0016	0.0045	0.0002
27 METHANE DECANE 74828 124185 0.0244 0.0201 0.0098	26	2-METHYLPENTANE	OCTANE	107835	111659	-0.0019	0.0005	0.0001
27 FIETHANE DECANE 74020 124105 0.0244 0.0201 0.0050	27	METHANE	DECANE	74828	124185	0.0244	0.0201	0.0098
28 HEXANE METHYLCYCLOPENTANE 110543 96377 0.0007 0.0029 0.0001	28	HEXANE	METHYLCYCLOPENTANE	110543	96377	0.0007	0.0029	0.0001
29 METHANE PENTANE 74828 109660 0.0104 0.0156 0.0054	29	METHANE	PENTANE	74828	109660	0.0104	0.0156	0.0054
30 PROPANE BUTANE 74986 106978 -0.0051 0.0024 0.0006	30	PROPANE	BUTANE	74986	106978	-0.0051	0.0024	0.0006
31 METHANE ISOBUTANE 74828 75285 0.0062 0.0121 0.0040	31	METHANE	ISOBUTANE	74828	75285	0.0062	0.0121	0.0040
32 ETHANE DECANE 74840 124185 0.0196 0.0114 0.0096	32	ETHANE	DECANE	74840	124185	0.0196	0.0114	0.0096
33 BUTANE DECANE 106978 124185 0.0071 0.0034 0.0018	33	BUTANE	DECANE	106978	124185	0.0071	0.0034	0.0018
34         ISOBUTANE         BUTANE         75285         106978         -0.0006         0.0002         0.0001	34	ISOBUTANE	BUTANE	75285	106978	-0.0006	0.0002	0.0001
35 PENTANE DECANE 109660 124185 0.0051 0.0018 0.0007	35	PENTANE	DECANE	109660	124185	0.0051	0.0018	0.0007
36         HEPTANE         OCTANE         142825         111659         0.0047         0.0007         0.0001	36	HEPTANE	OCTANE	142825	111659	0.0047	0.0007	0.0001
37         PROPANE         DECANE         74986         124185         0.0060         0.0066         0.0046	37	PROPANE	DECANE	74986	124185	0.0060	0.0066	0.0046
38         HEPTANE         p-XYLENE         142825         106423         0.0053         0.0040         0.0033	38	HEPTANE	p-XYLENE	142825	106423	0.0053	0.0040	0.0033
39         CYCLOHEXANE         HEPTANE         110827         142825         0.0012         0.0042         0.0001	39	CYCLOHEXANE	HEPTANE	110827	142825	0.0012	0.0042	0.0001
40 2-3-DIMETHYLBUTANE HEXANE 79298 110543 0.0005 0.0023 0.0012	40	2-3-DIMETHYLBUTANE	HEXANE	79298	110543	0.0005	0.0023	0.0012
41 PENTANE HEXANE 109660 110543 0.0067 0.0007 0.0001	41	PENTANE	HEXANE	109660	110543	0.0067	0.0007	0.0001
42 HEXADECANE ETHANE 544763 74840 0.0064 0.0156 0.0000	42	HEXADECANE	ETHANE	544763	74840	0.0064	0.0156	0.0000
43 2-METHYLPENTANE HEPTANE 107835 142825 -0.0007 0.0002 0.0002	43	2-METHYLPENTANE	HEPTANE	107835	142825	-0.0007	0.0002	0.0002
44 3-METHYLPENTANE HEPTANE 96140 142825 -0.0001 0.0007 0.0002	44	3-METHYLPENTANE	HEPTANE	96140	142825	-0.0001	0.0007	0.0002
45 HEXANE HEPTANE 110543 142825 -0.0038 0.0002 0.0001	45	HEXANE	HEPTANE	110543	142825	-0.0038	0.0002	0.0001
46 CYCLOHEXANE OCTANE 110827 111659 0.0004 0.0034 0.0000	46	CYCLOHEXANE	OCTANE	110827	111659	0.0004	0.0034	0.0000
47         PENTANE         OCTANE         109660         111659         0.0047         0.0017         0.0005	47	PENTANE	OCTANE	109660	111659	0.0047	0.0017	0.0005

Table E.2: Mixtures of a non-associating, dipolar and a non-associating, quadrupolar component (group 4): For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the value of  $k_{ij}$  fitted to experimental data ( $k_{ij}^{fit}$ ), the value of  $k_{ij}$  prediction with the QSPR model ( $k_{ij}^{QSPR}$ ) and the value of  $k_{ij}$  prediction with the Hudson-McCoubrey expression[2] ( $k_{ij}(I,\sigma)$ ).

		Group	4 (nAdP - nAqP)	)			
#	component <i>i</i>	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sup>QSPR</sup>	$k_{ij}(I,\sigma)$
1	ACETONE	NITROGEN	67641	7727379	0.0336	0.0146	0.0284
2	NITROGEN	PROPYLBENZENE	7727379	103651	0.1658	0.1433	0.0527
3	BENZENE	1-BROMOBENZENE	71432	108861	-0.0082	0.0033	0.0002
4	CARBON-DIOXIDE	1-BROMOBENZENE	124389	108861	0.0462	0.0407	0.0446
5	SULFUR-DIOXIDE	BENZENE	7446095	71432	0.0494	0.0529	0.0864
6	CARBON-DIOXIDE	PROPYLBENZENE	124389	103651	0.0382	0.0533	0.0516
7	DIMETHYL-ETHER	CARBON-DIOXIDE	115106	124389	-0.0574	-0.0285	0.0132
8	PROPYLENE	NITROGEN	115071	7727379	0.0642	0.0466	0.0282
9	BUTYLBENZENE	BENZENE	104518	71432	-0.0101	0.0013	0.0011

10	CARBON-DIOXIDE	1-HEXENE	124389	592416	0.0125	0.0244	0.0346
11	VINYL-ACETATE	ETHYLENE	108054	74851	-0.0159	0.0071	0.0045
12	CARBON-DIOXIDE	o-XYLENE	124389	95476	0.0343	0.0445	0.0477
13	CARBON-DIOXIDE	ISOPROPYL-ETHANOATE	124389	108214	0.0019	-0.0158	0.0181
14	PROPYLENE	BENZENE	115071	71432	0.0087	0.0166	0.0035
15	DIETHYL-ETHER	CARBON-DISULFIDE	60297	75150	0.0057	0.0206	0.0026
16	CARBON-DIOXIDE	TOLUENE	124389	108883	0.0246	0.0461	0.0427
17	NITROGEN	TOLUENE	7727379	108883	0.1223	0.1304	0.0462
18	CARBON-DIOXIDE	CHLOROBENZENE	124389	108907	0.0351	0.03	0.0412
19	PROPYLENE	ETHYLENE	115071	74851	-0.0004	0.0054	0.001
20	1-HEXENE	ETHYLENE	592416	74851	0.0443	0.013	0.0054
21	1-HEXENE	BENZENE	592416	71432	0.0011	0.0076	0.0002
22	BENZENE	CHLOROBENZENE	71432	108907	-0.002	0.0016	0.0000
23	CARBON-DIOXIDE	ETHYLBENZENE	124389	100414	0.0345	0.0451	0.0471
24	BENZENE	TOLUENE	71432	108883	-0.0062	0.0015	0.0003

## E.2. Binary mixture database of the QSPR method Results and comparison with k<sub>ij</sub> values adjusted to experimental VLE data

Table E.3: Regression results for mixtures of two non-associating, non-polar components (group 1). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted on experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 1 (nAnF	P - nAnP)				
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo
		Training	set				
1	3-METHYLPENTANE	OCTANE	96140	111659	-0.0003	0	0
2	CARBON-MONOXIDE	PROPANE	630080	74986	0.0517	0.0622	0
3	CARBON-MONOXIDE	METHANE	630080	74828	0.0287	0.0301	0
4	CARBON-MONOXIDE	ETHANE	630080	74840	0.0258	0.0462	0
5	PROPANE	METHYLCYCLOHEXANE	74986	108872	0.0102	0.0153	0
6	ETHANE	METHYLCYCLOHEXANE	74840	108872	0.0169	0.0226	0
7	METHANE	PROPANE	74828	74986	0.0012	0.0082	0
8	METHANE	METHYLCYCLOHEXANE	74828	108872	0.0338	0.0357	0
9	METHANE	ETHANE	74828	74840	-0.0046	0.0041	0
10	PROPANE	CYCLOHEXANE	74986	110827	0.0141	0.0119	0
11	METHANE	HEXADECANE	74828	544763	0.0545	0.0259	0
12	METHANE	OCTANE	74828	111659	0.0174	0.0198	0
13	METHANE	ETHYLCYCLOHEXANE	74828	1678917	0.0278	0.0436	0
14	METHANE	HEXANE	74828	110543	0.0135	0.0174	0
15	PROPANE	ISOBUTANE	74986	75285	-0.0048	0.0022	0
16	HEPTANE	METHYLCYCLOHEXANE	142825	108872	0.0021	0.0065	0
17	ETHANE	HEXANE	74840	110543	0.0066	0.0095	0
18	HEXANE	HEXADECANE	110543	544763	0.0011	0.0032	0
19	HEXANE	OCTANE	110543	111659	-0.003	0.0009	0
20	ETHANE	OCTANE	74840	111659	0.0174	0.0112	0

21	METHANE	BUTANE	74828	106978	0.0014	0.0126	0
22	METHANE	NONANE	74828	111842	0.0148	0.0204	0
23	CYCLOHEXANE	METHYLCYCLOHEXANE	110827	108872	0.0016	0.0016	0
24	METHANE	HEPTANE	74828	142825	0.0112	0.018	0
25	HEXANE	CYCLOHEXANE	110543	110827	0.0016	0.0045	0
26	2-METHYLPENTANE	OCTANE	107835	111659	-0.0019	0.0005	0
27	METHANE	DECANE	74828	124185	0.0244	0.0201	0
28	HEXANE	METHYLCYCLOPENTANE	110543	96377	0.0007	0.0029	0
29	METHANE	PENTANE	74828	109660	0.0104	0.0156	0
30	PROPANE	BUTANE	74986	106978	-0.0051	0.0024	0
31	METHANE	ISOBUTANE	74828	75285	0.0062	0.0121	0
32	ETHANE	DECANE	74840	124185	0.0196	0.0114	0
33	BUTANE	DECANE	106978	124185	0.0071	0.0034	0
34	ISOBUTANE	BUTANE	75285	106978	-0.0006	0.0002	0
35	PENTANE	DECANE	109660	124185	0.0051	0.0018	0
36	HEPTANE	OCTANE	142825	111659	0.0047	0.0007	0
37	PROPANE	DECANE	74986	124185	0.006	0.0066	0
38	HEPTANE	p-XYLENE	142825	106423	0.0053	0.004	0
39	CYCLOHEXANE	HEPTANE	110827	142825	0.0012	0.0042	0
40	2-3-DIMETHYLBUTANE	HEXANE	79298	110543	0.0005	0.0023	0
41	PENTANE	HEXANE	109660	110543	0.0067	0.0007	0
		Test se	t				
42	HEXADECANE	ETHANE	544763	74840	0.0064	0.0156	0
43	2-METHYLPENTANE	HEPTANE	107835	142825	-0.0007	0.0002	0
44	3-METHYLPENTANE	HEPTANE	96140	142825	-0.0001	0.0007	0
45	HEXANE	HEPTANE	110543	142825	-0.0038	0.0002	0
46	CYCLOHEXANE	OCTANE	110827	111659	0.0004	0.0034	0
47	PENTANE	OCTANE	109660	111659	0.0047	0.0017	0

Table E.4: Regression results for mixtures of non-associating, non-polar with non-associating, dipolar components (group 2). For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 2 (nAnP - r	nAdP)				
#	component <i>i</i>	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sup>QSPR</sup>	azeo
		Training set					
1	CARBON-MONOXIDE	1-OCTENE	630080	111660	0.0705	0.0944	0
2	CYCLOHEXANE	N-METHYL-	110827	872504	0.0166	0.0203	0
		2-PYRROLIDONE					
3	METHANE	PROPYLBENZENE	74828	103651	0.0318	0.0341	0
4	CYCLOHEXANE	TOLUENE	110827	108883	0.0144	0.0019	0
5	ETHYL-ETHANOATE	METHYLCYCLOHEXANE	141786	108872	0.0508	0.0274	1
6	METHYLCYCLOHEXANE	CHLOROBENZENE	108872	108907	0.0121	0.0085	0
7	ETHANE	PROPYLBENZENE	74840	103651	0.0252	0.0219	0
8	CHLOROBUTANE	METHYLCYCLOHEXANE	109693	108872	0.0122	0.017	0
9	PROPANE	TOLUENE	74986	108883	0.0201	0.0135	0
10	HEXANE	CHLOROBENZENE	110543	108907	0.0075	0.0154	0

11	METHANE	PROPYLENE	74828	115071	-0.0046	0.0091	0
12	CHLOROBUTANE	HEPTANE	109693	142825	0.009	0.0115	0
13	CYCLOHEXANE	ISOPROPYL-ETHANOATE	110827	108214	0.0303	0.0199	1
14	NONANE	PROPYLBENZENE	111842	103651	0.0047	0.0057	1
15	ETHYL-ETHANOATE	CYCLOHEXANE	141786	110827	0.0501	0.0238	1
16	HEXANE	N-METHYL-	110543	872504	0.0093	0.0239	0
		2-PYRROLIDONE					
17	PROPANE	DIMETHYL-ETHER	74986	115106	0.026	0.0136	1
18	HEPTANE	BUTYL-ETHANOATE	142825	123864	0.0289	0.0112	0
19	ETHANE	PROPYLENE	74840	115071	-0.0058	0.0044	0
20	CYCLOHEXANE	BUTYL-ETHANOATE	110827	123864	0.0265	0.0163	0
21	DIMETHYL-ETHER	ISOBUTANE	115106	75285	0.0281	0.0165	1
22	OCTANE	o-XYLENE	111659	95476	-0.0032	0.0068	0
23	CYCLOHEXANE	CHLOROBENZENE	110827	108907	0.0121	0.0101	0
24	METHYLCYCLOHEXANE	TOLUENE	108872	108883	0.012	0.0035	0
25	CHLOROBENZENE	DECANE	108907	124185	-0.0082	0.0139	0
26	1-HEXENE	HEXANE	592416	110543	0.0033	0.0034	0
27	METHYLCYCLOHEXANE	BUTYL-ETHANOATE	108872	123864	0.0276	0.0189	0
28	HEXANE	ETHYLBENZENE	110543	100414	0.0076	0.0077	0
29	TOLUENE	DECANE	108883	124185	0.0054	0.0049	0
30	ETHYLBENZENE	p-XYLENE	100414	106423	0.0003	0.0033	0
31	1-HEXENE	OCTANE	592416	111659	0.0006	0.0044	0
32	ETHYL-ETHANOATE	HEPTANE	141786	142825	0.0419	0.0169	1
33	1-BUTENE	BUTANE	106989	106978	0	0.0037	0
34	ETHYLBENZENE	NONANE	100414	111842	0.0072	0.0063	0
35	HEPTANE	TOLUENE	142825	108883	0.0046	0.0059	0
36	PROPYLENE	PROPANE	115071	74986	0.0069	0.0039	0
37	HEPTANE	o-XYLENE	142825	95476	0.0051	0.0077	0
38	HEPTANE	CHLOROBENZENE	142825	108907	0.0073	0.0151	0
39	OCTANE	PROPYLBENZENE	111659	103651	0.0066	0.006	0
40	HEPTANE	ETHYLBENZENE	142825	100414	0.0073	0.0075	0
		Test set					
41	HEXANE	CHLOROBUTANE	110543	109693	0.008	0.0117	1
42	1-HEXENE	HEPTANE	592416	142825	0.0039	0.0037	0
43	HEPTANE	N-METHYL-2-PYRROLIDONE	142825	872504	0.01	0.0236	0
44	TOLUENE	OCTANE	108883	111659	0.0072	0.005	0
45	CYCLOHEXANE	PROPYL-ETHANOATE	110827	109604	0.0355	0.0197	1

Table E.5: Regression results for mixtures of non-associating, non-polar with non-associating, quadrupolar components (group 3). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

	Group 3 (nAnP - nAqP)									
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo			
	Training set									
1	NITROGEN	METHYLCYCLOHEXANE	7727379	108872	0.1245	0.1592	0			
2	BENZENE	p-XYLENE	71432	106423	-0.0049	0.0017	0			

3	CARBON-DIOXIDE	ETHYLCYCLOHEXANE	124389	1678917	0.0707	0.0797	0
4	NITROGEN	ISOBUTANE	7727379	75285	0.1001	0.0741	0
5	CARBON-DIOXIDE	BUTANE	124389	106978	0.0358	0.0312	0
6	NITROGEN	METHANE	7727379	74828	0.0226	0.0309	0
7	CARBON-DIOXIDE	PENTADECANE	124389	629629	0.0551	0.0528	0
8	NITROGEN	NONANE	7727379	111842	0.1232	0.1038	0
9	METHANE	BENZENE	74828	71432	0.0265	0.0323	1
10	CARBON-DIOXIDE	p-XYLENE	124389	106423	0.0282	0.0539	0
11	CARBON-DIOXIDE	ETHANE	124389	74840	0.0195	0.0174	1
12	NITROGEN	ETHANE	7727379	74840	0.039	0.0444	0
13	ETHYLENE	OCTANE	74851	111659	0.0182	0.0171	0
14	NITROGEN	PROPANE	7727379	74986	0.0623	0.0593	0
15	CARBON-DIOXIDE	METHYLCYCLOHEXANE	124389	108872	0.0573	0.067	0
16	CARBON-DIOXIDE	OCTANE	124389	111659	0.0451	0.0428	0
17	NITROGEN	PENTANE	7727379	109660	0.089	0.0865	0
18	CARBON-DIOXIDE	PROPANE	124389	74986	0.0327	0.0241	0
19	NITROGEN	HEPTANE	7727379	142825	0.1098	0.095	0
20	DODECANE	CARBON-DIOXIDE	112403	124389	0.0501	0.0479	0
21	CARBON-DIOXIDE	CYCLOHEXANE	124389	110827	0.0608	0.056	0
22	CARBON-DIOXIDE	PENTANE	124389	109660	0.0384	0.0362	0
23	CARBON-DISULFIDE	CYCLOPENTANE	75150	287923	0.0011	0.0078	1
24	CARBON-DIOXIDE	HEPTANE	124389	142825	0.0427	0.0399	0
25	ETHANE	BENZENE	74840	71432	0.0196	0.0208	0
26	BENZENE	OCTANE	71432	111659	0.0038	0.0052	0
27	BENZENE	METHYLCYCLOHEXANE	71432	108872	0.0089	0.0027	0
28	NITROGEN	OCTANE	7727379	111659	0.1222	0.1016	0
29	CARBON-DIOXIDE	OCTADECANE	124389	593453	0.0843	0.0544	0
30	ETHYLENE	ETHANE	74851	74840	0.0124	0.0031	0
31	BENZENE	DODECANE	71432	112403	-0.0005	0.0039	0
32	HEXANE	BENZENE	110543	71432	0.006	0.0063	1
33	CARBON-DIOXIDE	NONANE	124389	111842	0.0332	0.0437	0
34	METHYLCYCLOPENTANE	BENZENE	96377	71432	0.0076	0.003	1
35	NITROGEN	DECANE	7727379	124185	0.1109	0.1026	0
36	CARBON-DIOXIDE	UNDECANE	124389	1120214	0.0605	0.0474	0
		Test se					
37	CARBON-DISULFIDE	CYCLOHEXANE	75150	110827	-0.0029	0.0049	0
38	BENZENE	DECANE	71432	124185	0.00025	0.005	0
39	CARBON-DIOXIDE	DECANE	124389	124185	0.0518	0.0432	0
40	METHANE	ETHYLENE	74828	74851	0.0095	0.0432	0
40 41	BENZENE	HEPTANE	71432	142825	0.0095	0.0029	0
-11			, 1472	172023	0.005	0.000	0

Table E.6: Regression results for mixtures of non-associating, dipolar with non-associating, quadrupolar components (group 4). For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data  $(k_{ij}^{fit})$  and the values of  $k_{ij}$  predicted with the QSPR model  $(k_{ij}^{QSPR})$ . The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

	Group 4 (nAdP - nAqP)							
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sup>QSPR</sup>	azeo	

		Traini	ng set				
1	ACETONE	NITROGEN	67641	7727379	0.0336	0.0146	0
2	NITROGEN	PROPYLBENZENE	7727379	103651	0.1658	0.1433	0
3	BENZENE	1-BROMOBENZENE	71432	108861	-0.0082	0.0033	0
4	CARBON-DIOXIDE	1-BROMOBENZENE	124389	108861	0.0462	0.0407	0
5	SULFUR-DIOXIDE	BENZENE	7446095	71432	0.0494	0.0529	0
6	CARBON-DIOXIDE	PROPYLBENZENE	124389	103651	0.0382	0.0533	0
7	DIMETHYL-ETHER	CARBON-DIOXIDE	115106	124389	-0.0574	-0.0285	0
8	PROPYLENE	NITROGEN	115071	7727379	0.0642	0.0466	0
9	BUTYLBENZENE	BENZENE	104518	71432	-0.0101	0.0013	0
10	CARBON-DIOXIDE	1-HEXENE	124389	592416	0.0125	0.0244	0
11	VINYL-ACETATE	ETHYLENE	108054	74851	-0.0159	0.0071	0
12	CARBON-DIOXIDE	o-XYLENE	124389	95476	0.0343	0.0445	0
13	CARBON-DIOXIDE	ISOPROPYL-ETHANOATE	124389	108214	0.0019	-0.0158	0
14	PROPYLENE	BENZENE	115071	71432	0.0087	0.0166	0
15	DIETHYL-ETHER	CARBON-DISULFIDE	60297	75150	0.0057	0.0206	1
16	CARBON-DIOXIDE	TOLUENE	124389	108883	0.0246	0.0461	0
17	NITROGEN	TOLUENE	7727379	108883	0.1223	0.1304	0
18	CARBON-DIOXIDE	CHLOROBENZENE	124389	108907	0.0351	0.03	1
19	PROPYLENE	ETHYLENE	115071	74851	-0.0004	0.0054	0
20	1-HEXENE	ETHYLENE	592416	74851	0.0443	0.013	0
21	1-HEXENE	BENZENE	592416	71432	0.0011	0.0076	0
		Test	t set				
22	BENZENE	CHLOROBENZENE	71432	108907	-0.002	0.0016	0
23	CARBON-DIOXIDE	ETHYLBENZENE	124389	100414	0.0345	0.0451	0
24	BENZENE	TOLUENE	71432	108883	-0.0062	0.0015	0

Table E.7: Regression results for mixtures of two non-associating, quadrupolar components (group 5). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

	Group 5 (nAqP - nAqP)									
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo			
	Training set									
1	CARBON-DIOXIDE	BENZENE	124389	71432	0.0502	0.0479	0			
2	CARBON-DISULFIDE	BENZENE	75150	71432	0.0134	0.0032	0			
3	NITROGEN	BENZENE	7727379	71432	0.1374	0.1365	0			
	Test set									
4	NITROGEN	ETHYLENE	7727379	74851	0.0616	0.0326	0			

Table E.8: Regression results for mixtures of two non-associating, dipolar components (group 6). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 6 (nAdP	' - nAdP)				
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo
		Training	set				
1	N-N-DIMETHYL-	1-METHYLNAPHTHALENE	68122	90120	-0.0059	0	0
	FORMAMIDE						
2	m-XYLENE	o-XYLENE	108383	95476	0	0.002	0
3	DICHLOROMETHANE	o-XYLENE	75092	95476	-0.0002	0.0199	0
4	ISOBUTENE	N-METHYL-2	115117	872504	-0.014	-0.0246	0
		PYRROLIDONE					
5	DIETHYL-ETHER	ACETONE	60297	67641	0.0028	-0.001	0
6	ACETONE	TOLUENE	67641	108883	0.0007	0.0138	0
7	PROPYLENE	DIMETHYL-ETHER	115071	115106	0	0.0078	0
8	ACETONE	3-PENTANONE	67641	96220	0.0031	0.0085	0
9	2-METHYLPROPANAL	N-N-DIMETHYL-	78842	68122	-0.0013	-0.001	0
		FORMAMIDE					
10	ACETALDEHYDE	ACETONITRILE	75070	75058	-0.0017	0.0014	0
		Test se	t				
11	ACETONITRILE	PROPIONITRILE	75058	107120	0	0.0078	0
12	ACETONE	o-XYLENE	67641	95476	0.0095	0.013	0

Table E.9: Regression results for mixtures of non-associating, non-polar with associating, dipolar components (group 7). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 7 (nA	nP - AdP)							
#	component <i>i</i>	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sup>QSPR</sup>	azeo			
	Training set									
1	ETHANE	1-OCTANOL	74840	111875	0.0011	0.0011	0			
2	CARBON-MONOXIDE	PROPIONIC-ACID	630080	79094	0.0708	0.1111	0			
3	DIETHYLAMINE	HEPTANE	109897	142825	-0.0333	-0.004	0			
4	DODECANE	epsilon-CAPROLACTAM	112403	105602	-0.0136	0.0033	1			
5	CYCLOHEXANE	n-HEXANOIC-ACID	110827	142621	-0.0236	-0.0119	0			
6	HEXANE	ISOPROPANOL	110543	67630	0.0402	0.0338	1			
7	METHYLAMINE	HEXANE	74895	110543	0.01	0.0073	0			
8	METHANOL	HEPTANE	67561	142825	-0.0093	0.0097	1			
9	TRIDECANE	1-DODECANOL	629505	112538	0.012	-0.0075	0			
10	1-OCTANOL	n-HEPTYLBENZENE	111875	1078713	0.0274	0.0217	0			
11	ETHANOL	NONANE	64175	111842	0.0189	0.02	1			
12	HEXANE	1-HEXADECANOL	110543	36653824	0.0008	-0.013	0			
13	HEPTANE	NEOPENTANOIC-ACID	142825	75989	0.01	0.025	0			
14	HEPTANE	2-METHYL-1-BUTANOL	142825	137326	0.0149	0.0094	1			

16         PENTANE         1-PENTANOL         109660         71410         0.01         0.0081         0           17         1-PROPANOL         HEPTANE         71238         142825         0.026         0.0193         1           18         METHANOL         CYCLOHEXANE         67561         110827         0.0122         0.0205         1           19         CYCLOHEXANE         1-HEXANOL         110827         111273         0.0217         0.0114         0           20         PROPANE         1-DECANOL         74986         112301         0.0042         -0.0018         0           21         CYCLOHEXANE         PYRROLIDINE         110827         123751         -0.0158         -0.0049         1	0 1 1 0 0 1 1 1 0 0 0
18         METHANOL         CYCLOHEXANE         67561         110827         0.0122         0.0205         1           19         CYCLOHEXANE         1-HEXANOL         110827         111273         0.0217         0.0114         0           20         PROPANE         1-DECANOL         74986         112301         0.0042         -0.0018         0           21         CYCLOHEXANE         PYRROLIDINE         110827         123751         -0.0158         -0.0049         1	1 0 1 1 1 0
19         CYCLOHEXANE         1-HEXANOL         110827         111273         0.0217         0.0114         0           20         PROPANE         1-DECANOL         74986         112301         0.0042         -0.0018         0           21         CYCLOHEXANE         PYRROLIDINE         110827         123751         -0.0158         -0.0049         1	0 0 1 1 1 0
19         CYCLOHEXANE         1-HEXANOL         110827         111273         0.0217         0.0114         0           20         PROPANE         1-DECANOL         74986         112301         0.0042         -0.0018         0           21         CYCLOHEXANE         PYRROLIDINE         110827         123751         -0.0158         -0.0049         1	0 1 1 1 0
21 CYCLOHEXANE PYRROLIDINE 110827 123751 -0.0158 -0.0049	1 1 1 0
	1 1 0
	1 0
22 BUTANE ETHANOL 106978 64175 0.0105 0.0108	0
23 CYCLOHEXANE 1-BUTANOL 110827 71363 0.0426 0.0335	
24 2-2-DIMETHYLBUTANE 1-PENTANOL 75832 71410 0.0141 0.0158 (	0
25 HEXANE 1-HEXANOL 110543 111273 0.011 0.0027 (	0
26 METHYLCYCLOHEXANE 1-BUTANOL 108872 71363 0.0467 0.041	1
27 DECANE 1-OCTANOL 124185 111875 0.0201 0.0073	1
28 1-BUTANOL DODECANE 71363 112403 0.0246 0.0256 (	0
29 PROPANE 1-PROPANOL 74986 71238 -0.0044 0.0078 (	0
30 ETHANOL HEXADECANE 64175 544763 0.0167 0.0266 (	0
31 CYCLOHEXANE 1-PROPANOL 110827 71238 0.0321 0.0329	1
32 CYCLOPENTANE CYCLOHEXANOL 287923 108930 0.019 0.0132 (	0
33 CYCLOHEXANE CYCLOHEXANOL 110827 108930 0.0245 0.0195 (	0
34 1-PROPANOL UNDECANE 71238 1120214 0.0289 0.0247 (	0
35 ETHYLAMINE HEXANE 75047 110543 -0.0006 0.0009 (	0
36 HEXANE 1-DECANOL 110543 112301 0.0054 -0.0059 (	0
37 BUTANE ETHYLAMINE 106978 75047 0.003 0.0049	1
38 3-METHYLPENTANE 1-PENTANOL 96140 71410 0.0157 0.0118 (	0
39 HEXANE ETHANOL 110543 64175 0.0102 0.0165	1
40 1-BUTANOL DECANE 71363 124185 0.0351 0.0223	1
41 PENTANE 1-PROPANOL 109660 71238 0.022 0.0165 (	0
42 1-PROPANOL NONANE 71238 111842 0.0296 0.0221	1
43 METHYLAMINE NONANE 74895 111842 0.0106 0.0094 (	0
44 HEPTANE 1-OCTANOL 142825 111875 0.01 0.0056 (	0
Test set	
45 OCTANE 1-OCTANOL 111659 111875 0.0223 0.0071 (	0
46 2-3-DIMETHYLBUTANE 1-PENTANOL 79298 71410 0.016 0.0153 (	0
47 2-METHYLPENTANE 1-PENTANOL 107835 71410 0.0134 0.0106 (	0
48 HEPTANE 1-PENTANOL 142825 71410 0.0255 0.0102	1
49 HEXANE 1-PENTANOL 110543 71410 0.0179 0.0097 (	0
50 HEXANE 1-PROPANOL 110543 71238 0.0238 0.0186	1

Table E.10: Regression results for mixtures of non-associating, dipolar with associating, dipolar components (group 8). For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

	Group 8 (nAdP - AdP)								
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo		
Training set									
1	ETHANOL	ACETONITRILE	64175	75058	-0.0313	-0.0571	1		
2	ACETONE	ANILINE	67641	62533	-0.0286	0.0079	0		

3	DIETHYLAMINE	CHLOROBENZENE	109897	108907	-0.0446	-0.0313	0
4	WATER	SULFOLANE	7732185	126330	-0.0244	-0.0405	0
5	PHENOL	NITROBENZENE	108952	98953	-0.0151	-0.0406	0
6	ACETONE	METHANOL	67641	67561	-0.033	-0.0358	1
7	ETHANOL	TOLUENE	64175	108883	0.0332	0.0205	1
8	DIETHYLAMINE	ETHYL-ETHANOATE	109897	141786	-0.0036	0.0192	0
9	NITROMETHANE	1-HEXANOL	75525	111273	0.0078	-0.0264	0
10	METHYLAMINE	TRIMETHYLAMINE	74895	75503	-0.024	-0.0019	1
11	METHANOL	gamma-	67561	96480	-0.0212	-0.0334	0
	BUTYROLACTONE						
12	CHLOROBENZENE	PROPIONIC-ACID	108907	79094	-0.0335	-0.0541	0
13	1-PROPANOL	N-METHYL-2- PYRROLIDONE	71238	872504	-0.0594	-0.0183	0
14	1-BROMOBENZENE	CYCLOHEXANOL	108861	108930	0.0337	0.0241	1
15	METHANOL	DIMETHYL-DISULFIDE	67561	624920	0.0275	-0.0005	1
16	ACRYLONITRILE	WATER	107131	7732185	-0.05	-0.0416	1
17	1-HEXENE	PROPIONIC-ACID	592416	79094	-0.0154	-0.0508	0
18	CHLOROBENZENE	ANILINE	108907	62533	-0.0051	-0.0508	0
19	METHYL-PROPANOATE	1-BUTANOL	554121	71363	0.006	-0.0015	0
20	METHANOL	METHYL-	67561	628284	-0.0355	-0.0089	1
20		n-BUTYL-ETHER					
21	ACETONITRILE	1-PROPANOL	75058	71238	-0.0381	-0.0427	1
22	DIETHYLAMINE	TRIETHYLAMINE	109897	121448	-0.0381	-0.0059	0
23	METHYL-ACETATE	ETHANOL	79209	64175	-0.0327	-0.0157	0
		PROPYLENE-GLYCOL-					
24	DIISOPROPYL-ETHER	MONOMETHYL-ETHER	108203	107982	-0.0035	-0.0067	0
25	1-PROPANOL FORMAMIDE	N-N-DIMETHYL-	71238	68122	-0.0593	-0.0302	0
26	ACETONITRILE	WATER	75058	7732185	-0.0485	-0.0349	1
27	ETHANOL	N-METHYL-2-	64175	872504	-0.078	-0.0299	0
		PYRROLIDONE					
28	TOLUENE	ANILINE	108883	62533	-0.005	-0.0388	0
29	ACETONE	CYCLOHEXANOL	67641	108930	0.0031	-0.013	0
30	1-2-DICHLOROETHANE	1-PROPANOL	107062	71238	0.0361	0.0095	1
31	ETHANOL	N-N-DIMETHYL-	64175	127195	-0.078	-0.0302	0
	ACETAMIDE						
32	TOLUENE	1-BUTANOL	108883	71363	0.0433	0.0268	1
33	METHANOL	ACETONITRILE	67561	75058	-0.0284	-0.0613	1
34	DIISOPROPYL-ETHER	1-BUTANOL	108203	71363	0.0132	0.0044	0
35	CYCLOHEXANONE	CYCLOHEXANOL	108941	108930	0.0049	0.0086	0
36	METHANOL	4-HEPTANONE	67561	123193	-0.0266	-0.0106	0
37	ACETONE	ETHANOL	67641	64175	-0.0376	-0.0256	1
38	ETHANOL	DI-n-BUTYL-ETHER	64175	142961	0.0022	0.0026	0
39	METHANOL	1-2-DICHLOROETHANE	67561	107062	0.0039	-0.0086	1
40	ETHYL-PROPANOATE	PROPIONIC-ACID	105373	79094	-0.0745	-0.0542	0
41	TOLUENE	n-BUTYRIC-ACID	108883	107926	-0.0235	-0.0413	0
42	METHANOL	VINYL-ACETATE	67561	108054	-0.0255	-0.0214	1
43	DIETHYL-ETHER	ETHANOL	60297	64175	-0.0173	-0.0078	0
44	PROPYLENE	ETHANOL	115071	64175	0.0223	-0.008	0
45	ETHANOL	1-2-DICHLOROETHANE	64175	107062	0.0269	0.0017	1
46		ETHYLBENZENE	109897	100414	-0.0539	-0.0236	0
47	PROPYLBENZENE	PHENOL	103651	108952	0.0234	0.0055	1

48	NITROMETHANE	1-BUTANOL	75525	71363	0.0137	-0.0214	1
49	METHANOL	BUTYL-ETHANOATE	67561	123864	-0.0514	-0.0117	0
50	DIETHYL-SULFIDE	1-PROPANOL	352932	71238	0.03	0.0168	1
51	CHLOROFORM	ETHANOL	67663	64175	-0.0032	-0.0014	1
52	DI-n-PROPYL-ETHER	1-OCTANOL	111433	111875	0.0043	-0.0028	0
53	THIOPHENE	PHENOL	110021	108952	0.0221	0.0006	0
54	1-2-DICHLOROETHANE	1-BUTANOL	107062	71363	0.0356	0.0121	0
55	DIISOPROPYL-ETHER	ETHANOL	108203	64175	-0.0009	-0.0032	1
56	DI-n-PROPYL-ETHER	1-BUTANOL	111433	71363	0.0122	0.0091	0
		Test s	set				
57	METHYL-BUTANOATE	1-BUTANOL	623427	71363	0.0065	0.002	0
58	ETHYLBENZENE	ANILINE	100414	62533	-0.008	-0.0408	0
59	DICHLOROMETHANE	ETHANOL	75092	64175	0.0101	-0.0153	1
60	ETHANOL	METHYL-PROPANOATE	64175	554121	-0.0033	-0.0122	1
61	TOLUENE	PHENOL	108883	108952	0.0181	0.0034	0
62	DIETHYLAMINE	TOLUENE	109897	108883	-0.0396	-0.0222	0
63	TOLUENE	p-CRESOL	108883	106445	0.0151	0.0029	0

Table E.11: Regression results for mixtures of non-associating, quadrupolar with associating, dipolar components (group 9). For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data  $(k_{ij}^{fit})$  and the values of  $k_{ij}$  predicted with the QSPR model  $(k_{ij}^{QSPR})$ . The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 9 (r	nAqP - AdP)				
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sub>ij</sub> k	azeo
		Traini	ng set				
1	ETHYLENE	1-DECANOL	74851	112301	-0.0054	0.0067	0
2	CARBON-DIOXIDE	ACETIC-ACID	124389	64197	-0.0341	-0.0174	0
3	CARBON-DIOXIDE	METHANOL	124389	67561	-0.0081	-0.0017	0
4	BENZENE	ACETIC-ACID	71432	64197	-0.0565	-0.072	0
5	NITROGEN	1-DECANOL	7727379	112301	0.153	0.0955	0
6	AMMONIA	BENZENE	7664417	71432	0.0416	0.0237	0
7	CARBON-DIOXIDE	n-DECANOIC-ACID	124389	334485	-0.0176	-0.0182	0
8	CARBON-DIOXIDE	1-BUTANOL	124389	71363	-0.0094	-0.0068	0
9	CARBON-DIOXIDE	METHYL-LACTATE	124389	547648	-0.0205	-0.049	0
10	NITROGEN	CYCLOHEXANOL	7727379	108930	0.1133	0.0621	0
11	BENZENE	PROPIONIC-ACID	71432	79094	-0.0638	-0.0375	0
12	DIETHYLAMINE	BENZENE	109897	71432	-0.0601	-0.0345	0
13	BENZENE	1-PROPANOL	71432	71238	0.0256	0.0247	1
14	NITROGEN	ETHANOL	7727379	64175	0.0355	0.0382	0
15	CARBON-DIOXIDE	PHENOL	124389	108952	-0.0041	0.0205	0
16	BENZENE	ANILINE	71432	62533	-0.0328	-0.0427	0
17	CARBON-DIOXIDE	ETHANOL	124389	64175	-0.0112	-0.0029	0
18	NITROGEN	1-OCTANOL	7727379	111875	0.1203	0.0665	0
		ETHYLENE-GLYCOL-					
19	CARBON-DIOXIDE	MONOPROPYL-ETHER	124389	2807309	-0.0179	0.0119	0
20	CARBON-DIOXIDE	1-DECANOL	124389	112301	0.0146	-0.0046	0
21	NITROGEN	1-PROPANOL	7727379	71238	-0.0154	0.0361	0

22	CARBON-DISULFIDE	1-PENTANOL	75150	71410	0.0114	0.027	0
23	ETHANOL	BENZENE	64175	71432	0.0165	0.0248	1
24	ISOPROPANOL	BENZENE	67630	71432	0.0444	0.0432	1
25	BENZENE	PHENOL	71432	108952	0.0034	0.0004	0
26	CARBON-DIOXIDE	1-HEPTANOL	124389	111706	0.0092	-0.0019	0
27	CARBON-DISULFIDE	1-BUTANOL	75150	71363	0.0265	0.0418	0
28	NITROGEN	2-HEXANOL	7727379	626937	0.0818	0.053	0
29	CARBON-DIOXIDE	1-PROPANOL	124389	71238	-0.0194	-0.0058	0
30	CARBON-DIOXIDE	1-PENTANOL	124389	71410	-0.0012	0.0007	0
31	CARBON-DIOXIDE	1-OCTANOL	124389	111875	0.0065	-0.0029	0
		Test	set				
32	CARBON-DIOXIDE	1-HEXANOL	124389	111273	0.001	-0.001	0
33	CARBON-DISULFIDE	1-PROPANOL	75150	71238	0.0293	0.0412	0
34	CARBON-DIOXIDE	2-METHYL-1-BUTANOL	124389	137326	0.0143	-0.004	0
35	CARBON-DIOXIDE	n-DODECANOIC-ACID	124389	143077	-0.0069	-0.0151	0
36	CARBON-DIOXIDE	p-CRESOL	124389	106445	-0.0032	0.0164	0

Table E.12: Regression results for mixtures of two associating, dipolar components (group 10). For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column. The mixtures are listed separately for the training and the test set.

		Group 10 (Ad	IP - AdP)				
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	$k_{ij}^{QSPR}$	azeo
		Training	set				
1	ACETIC-ACID	ACETAMIDE	64197	60355	-0.0993	-0.0734	0
2	CYCLOHEXYLAMINE	CYCLOHEXANOL	108918	108930	-0.1334	-0.1459	0
3	PROPIONIC-ACID	n-BUTYRIC-ACID	79094	107926	-0.0164	-0.0744	0
4	METHANOL	ANILINE	67561	62533	0.0558	0.0467	0
5	WATER	1-2-BENZENEDIOL	7732185	120809	-0.1136	-0.1507	0
	PROPYLENE-GLYCOL-						
6	MONOMETHYL-ETHER	1-2-PROPYLENE-GLYCOL	107982	57556	-0.003	-0.0379	0
		PROPYLENE-GLYCOL-					
7	ISOPROPANOL	MONOMETHYL-ETHER	67630	107982	0.0328	0.0265	0
8	p-CRESOL	1-2-BENZENEDIOL	106445	120809	-0.0486	-0.0633	0
9	CYCLOHEXYLAMINE	ANILINE	108918	62533	-0.1601	-0.1225	0
10	METHANOL	1-DECANOL	67561	112301	-0.0193	-0.0186	0
11	ANILINE	ETHYLENE-GLYCOL	62533	107211	0.0608	-0.007	1
12	3-METHYL-2-BUTANOL	1-PENTANOL	598754	71410	0.0035	-0.0089	0
13	WATER	PROPIONIC-ACID	7732185	79094	-0.1378	-0.1047	1
14	AMMONIA	DIETHYLAMINE	7664417	109897	0.0827	0.0438	0
15	ACETIC-ACID	n-BUTYRIC-ACID	64197	107926	-0.0513	-0.021	0
16	ACETIC-ACID	1-DODECANOL	64197	112538	-0.0451	0.0048	0
17	WATER	GLYCEROL	7732185	56815	-0.0679	-0.0845	0
18	PROPIONIC-ACID	PHENOL	79094	108952	-0.0625	-0.0471	0
19	n-BUTYLAMINE	1-BUTANOL	109739	71363	0.0025	0.0422	0
20	AMMONIA	HYDRAZINE	7664417	302012	0.0158	-0.0031	0
		PROPYLENE-GLYCOL-					
21	WATER	MONOMETHYL-ETHER	7732185	107982	-0.094	-0.0334	1

22	ETHANOL	WATER	64175	7732185	-0.0997	-0.0665	1
23	ETHANOL	1-PROPANOL	64175	71238	0.0001	-0.0443	0
24	n-BUTYLAMINE	PIPERIDINE	109739	110894	0.0058	-0.0012	0
25	METHANOL	2-BUTANOL	67561	78922	-0.0443	-0.0339	0
26	WATER	ETHYLENE-GLYCOL	7732185	107211	-0.0546	-0.0951	0
27	WATER	2-ETHOXYETHANOL	7732185	110805	-0.0987	-0.0264	1
28	1-PROPANOL	WATER	71238	7732185	-0.0736	-0.0413	1
29	1-BUTANOL	PYRROLE	71363	109977	0.0081	0.0033	1
30	ISOPROPANOL	WATER	67630	7732185	-0.0958	-0.0264	1
31	METHANOL	WATER	67561	7732185	-0.0994	-0.0871	0
32	ETHANOL	2-METHYL-1-PROPANOL	64175	78831	0.0011	-0.0344	0
33	ISOBUTYRIC-ACID	n-PENTANOIC-ACID	79312	109524	-0.0091	-0.011	0
34	ISOPROPANOL	1-PROPANOL	67630	71238	0.0002	-0.0233	0
35	WATER	1-BUTANOL	7732185	71363	-0.0762	-0.0304	1
36	2-METHYL-1-BUTANOL	1-PENTANOL	137326	71410	-0.0015	-0.0215	0
		Test s	et				
37	2-BUTANOL	1-BUTANOL	78922	71363	0.0006	-0.0172	0
38	ETHANOL	1-BUTANOL	64175	71363	-0.0083	-0.0359	0
39	METHANOL	ETHANOL	67561	64175	-0.0156	-0.0717	0
40	ACETIC-ACID	PROPIONIC-ACID	64197	79094	-0.0297	-0.0316	0
41	1-PROPANOL	PYRROLE	71238	109977	0.0068	-0.0009	0

Table E.13: List of the binary mixtures identified as outliers. These mixtures are not included neither in the training nor in the test set. For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the group of mixtures they are categorized to (*group*). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column.

	excluded mixtures (outliers)						
#	component i	component j	CAS-i	CAS-j	group	$k_{ij}^{fit}$	azeo
1	'CARBON-MONOXIDE'	'p-XYLENE'	630080	106423	1	0.0902	0
2	'ETHYL-METHANOATE'	'CYCLOHEXANE'	109944	110827	2	0.0686	1
3	'ETHYLENE'	'DODECANE'	74851	112403	3	-0.0412	0
4	'NITROGEN'	'ETHYLCYCLOHEXANE'	7727379	1678917	3	0.1241	0
5	'NITROGEN'	'HEXADECANE'	7727379	544763	3	0.1693	0
6	'CARBON-DIOXIDE'	'ACETONE'	124389	67641	4	-0.0045	0
7	'DICHLOROMETHANE'	'CARBON-DIOXIDE'	75092	124389	4	0.0089	0
8	'NITROGEN'	'CARBON-DIOXIDE'	7727379	124389	4	-0.0910	1
9	'CARBON-DIOXIDE'	'ETHYL-ETHANOATE'	124389	141786	4	-0.1641	0
10	'CARBON-DIOXIDE'	'ETHYL-METHANOATE'	124389	109944	4	-0.1446	0
11	'CARBON-DIOXIDE'	'ETHYL-PROPANOATE'	124389	105373	4	-0.1016	0
12	'CARBON-DIOXIDE'	'PROPYL-ETHANOATE'	124389	109604	4	-0.1413	0
13	'CARBON-DIOXIDE'	'PROPYL-PROPIONATE'	124389	106365	4	-0.0652	0
14	'CARBON-DIOXIDE'	'CARBON-DISULFIDE'	124389	75150	5	0.1145	0
15	'ACETONE'	'ACETIC-ACID'	67641	64197	6	-0.0898	0
16	'DIETHYL-ETHER'	'METHANOL'	60297	67561	6	-0.0602	1
17	'CHLOROFORM'	'PIPERIDINE'	67663	110894	6	-0.0845	0
18	'WATER'	'PROPYLENE-CARBONATE'	7732185	108327	6	-0.0097	0
19	'1-METHYLNAPHTHALENE'	'TRIETHYLENE-GLYCOL'	90120	112276	6	0.0416	0
20	'HYDROGEN-CHLORIDE'	'TRIFLUOROACETIC-ACID'	7647010	76051	6	0.0928	0

21	'ACETONE'	'WATER'	67641	7732185	6	-0.1167	0
22	'ETHYLENE-OXIDE'	'WATER'	75218	7732185	6	-0.0702	0
23	'TETRAHYDROFURAN'	'WATER'	109999	7732185	6	-0.0910	1
24	'HYDROGEN'	'1-OCTANOL'	1333740	111875	8	0.0514	0
25	'METHANE'	'1-PROPANOL'	74828	71238	8	-0.0373	0
26	'CARBON-MONOXIDE'	'ACETIC-ACID'	630080	64197	8	0.0662	0
27	'HYDROGEN'	'ACETIC-ACID'	1333740	64197	8	0.0850	0
28	'CYCLOHEXANE'	'ANILINE'	110827	62533	8	0.0255	0
29	'METHYLCYCLOHEXANE'	'ANILINE'	108872	62533	8	0.0078	0
30	'PHENOL'	'DODECANE'	108952	112403	8	0.0386	1
31	'CARBON-MONOXIDE'	'ETHANOL'	630080	64175	8	-0.0253	0
32	'HYDROGEN'	'METHANOL'	1333740	67561	8	-0.0259	0
33	'OCTANE'	'epsilon-CAPROLACTAM'	111659	105602	8	-0.0217	0
34	'WATER'	'3-HEPTANONE'	7732185	106354	10	-0.0644	0
35	'ETHYLAMINE'	'ETHANOL'	75047	64175	10	-0.1002	0
36	'Ammonia'	'METHANOL'	7664417	67561	10	-0.1388	0
37	'FORMIC-ACID'	'PROPIONIC-ACID'	64186	79094	10	-0.1562	0
38	'AMMONIA'	'WATER'	7664417	7732185	10	-0.1768	0

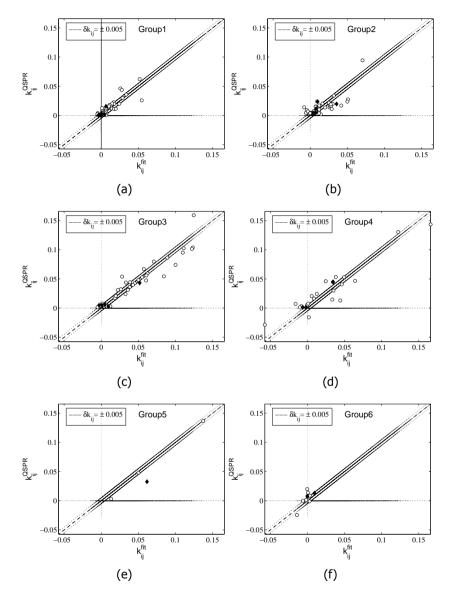


Figure E.1: Parity plots for the prediction in mixtures of non-associating components (groups 1 to 6). The fitted  $k_{ij}$  values  $(k_{ij}^{fit})$  are plotted against the predicted  $k_{ij}$  values  $(k_{ij}^{QSPR})$ . The white circles correspond to the mixtures of the training set and the black diamonds correspond to the mixtures of the test set. The dashed lines designate the  $\pm 0.005$  absolute deviation on the value of  $(k_{ij}^{fit})$ .

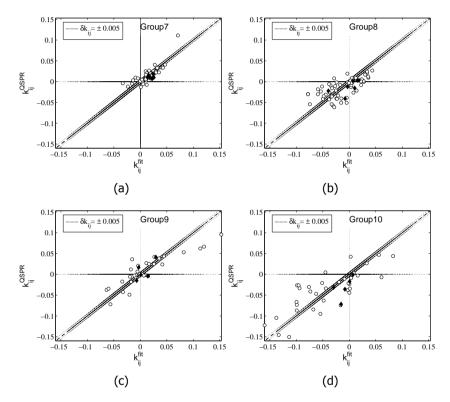


Figure E.2: Parity plots for the prediction in mixtures including associating components (groups 7 to 10). The fitted  $k_{ij}$  values ( $k_{ij}^{fit}$ ) are plotted against the predicted  $k_{ij}$  values ( $k_{ij}^{QSPR}$ ). The white circles correspond to the mixtures of the training set and the black diamonds correspond to the mixtures of the test set. The dashed lines designate the  $\pm 0.005$  absolute deviation on the value of ( $k_{ij}^{fit}$ ).

E.3. Evaluation of phase equilibrium calculations with the estimated  $k_{ij}$  values 157

**E.3.** Evaluation of phase equilibrium calculations with the estimated  $k_{ij}$  values

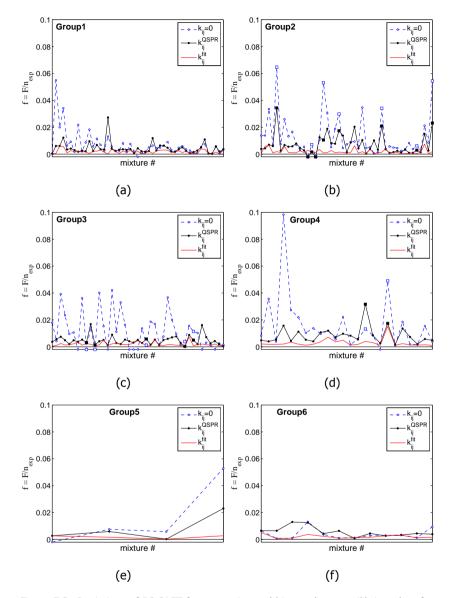


Figure E.3: Deviations of PC-SAFT from experimental binary phase equilibrium data for mixtures of non-associating components (groups 1 to 6). The deviations are defined as  $f = F/n_{exp}$  according to Eq.(3.23). The red line serves as a reference and is obtained for individually optimized  $k_{ij}^{fit}$  values. The symbols (connected by black line) are obtained using estimated values  $k_{ij}^{QSPR}$ . The blue dashed line represent phase equilibrium calculations, when the PC-SAFT EoS is not corrected ( $k_{ij} = 0$ ). The negative values indicate cases, when either the isobaric-isothermal flash calculations or the bubble point calculations did not converge for certain equilibrium data points. Azeotropic mixtures are marked with a square instead of a circle.



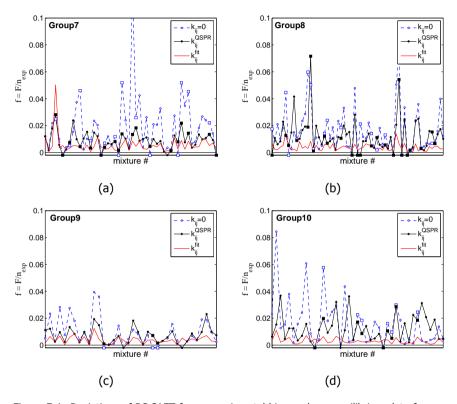


Figure E.4: Deviations of PC-SAFT from experimental binary phase equilibrium data for mixtures with at least one associating component (groups 7 to 10). The deviations are defined as  $f = F/n_{exp}$  according to Eq.(3.23). The red line serves as a reference and is obtained for individually optimized  $k_{ij}^{\text{ff}}$  values. The symbols (connected by black line) are obtained using estimated values  $k_{ij}^{\text{QSPR}}$ . The blue dashed line represent phase equilibrium calculations, when the PC-SAFT EoS is not corrected ( $k_{ij} = 0$ ). The negative values indicate cases, when either the isobaric-isothermal flash calculations or the bubble point calculations did not converge for certain equilibrium data points. Azeotropic mixtures are marked with a square instead of a circle.

## **E.4.** Estimation of $k_{ij}$ for binary mixtures with $H_2$

Table E.14: Results of the regressed model coefficients for mixtures of non-associating components with H<sub>2</sub>. The values of the coefficients  $c_L$  and their 95% confidence interval  $\Delta c_{L,95}$  for the QSPR model defined in Eq. (3.19) and (3.21), with  $c^{\text{assoc,s}} = 0$ ,  $c^{\text{assoc,c}} = 0$  and  $c^{\text{assoc,sc}} = 0$ .

mixtures of non-associating components with $H_2$				
	$c_L \cdot 10^4$	$\Delta c_{L,95} \cdot 10^4$		
c <sup>LJ</sup>	-21.671	±1.031		
c <sup>dd,a</sup>	-1315.516	$\pm 64.438$		
c <sup>dd,b</sup>	0.000	$\pm 0.000$		
cqq	-0.766	±0.355		
$c^{dq}$	0.000	±0		

Table E.15: Regression results for mixtures of non-associating components with H<sub>2</sub>. For each mixture the component names are given (*component i*, *component j*), their CAS-Numbers (*CAS-i*, *CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column.

						0.00-	
#	component i	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sup>QSPR</sup>	azeo
		Train	ing set				
1	HYDROGEN	BICYCLOHEXYL	1333740	92513	0.3774	0.4919	0
2	HYDROGEN	PROPANE	1333740	74986	0.2133	0.1309	0
3	HYDROGEN	CYCLOHEXANE	1333740	110827	0.2901	0.2842	0
4	HYDROGEN	DECANE	1333740	124185	0.2610	0.2160	0
5	HYDROGEN	PENTANE	1333740	109660	0.2398	0.1841	0
6	HYDROGEN	TETRADECANE	1333740	629594	0.2848	0.2542	0
7	HYDROGEN	BUTANE	1333740	106978	0.2069	0.1623	0
8	HYDROGEN	HEXANE	1333740	110543	0.1511	0.1971	0
9	HYDROGEN	1-METHYLNAPHTHALENE	1333740	90120	0.2633	0.3703	0
10	HYDROGEN	PROPYLENE-CARBONATE	1333740	108327	-0.7299	-0.5732	0
11	HYDROGEN	1-HEXENE	1333740	592416	0.1498	0.1030	0
12	HYDROGEN	CYCLOHEXANONE	1333740	108941	0.1460	-0.1330	0
13	HYDROGEN	BENZENE	1333740	71432	0.2007	0.2007	0
		Tes	st set				
14	HYDROGEN	2-2-4-TRIMETHYLPENTANE	1333740	540841	0.3907	0.2756	0
15	HYDROGEN	HEXADECANE	1333740	544763	0.3022	0.2582	0
16	HYDROGEN	1-OCTENE	1333740	111660	0.1424	0.1250	0
17	HYDROGEN	CHLOROBENZENE	1333740	108907	0.2080	0.0772	0

### **E.5.** Estimation of $k_{ij}$ for binary mixtures with CO<sub>2</sub>

Table E.16: Results of the regressed model coefficients for mixtures of non-associating dipolar with nonassociating quadrupolar components. The values of the coefficients  $c_L$  are adjusted only for mixtures of group 4 (Table E.17). The 95% confidence interval  $\Delta c_{L,95}$  for the QSPR model defined in Eq. (3.19) and (3.21), with  $c^{\text{assoc,s}} = 0$ ,  $c^{\text{assoc,sc}} = 0$  and  $c^{\text{assoc,sc}} = 0$ .

mixtures of non-associating dipolar with					
non-as	non-associating quadrupolar components				
$c_L \cdot 10^4 \qquad \Delta c_{L,95} \cdot 10^4$					
$c^{LJ}$	-118.756	±0.261			
c <sup>dd,a</sup>	-33.984	$\pm 1.373$			
$c^{\mathrm{dd,b}}$	0.000	$\pm 0.000$			
cqq	-0.300	$\pm 0.003$			
c <sup>dq</sup>	-0.132	$\pm 0.007$			

Table E.17: Regression results for mixtures of a non-associating dipolar with a non-associating quadrupolar component (group 4) for the QSPR model coefficients adjusted only to mixtures of this group. For each mixture the component names are given (*component i, component j*), their CAS-Numbers (*CAS-i, CAS-j*), the values of  $k_{ij}$  fitted to experimental VLE data ( $k_{ij}^{fit}$ ) and the values of  $k_{ij}$  predicted with the QSPR model ( $k_{ij}^{QSPR}$ ). The mixtures that demonstrate azeotropic behavior are noted with "ones" in the last column.

#	component <i>i</i>	component j	CAS-i	CAS-j	$k_{ij}^{fit}$	k <sub>ij</sub>	azeo
		Trainin	5				
1	NITROGEN	PROPYLBENZENE	7727379	103651	0.1658	0.1527	0
2	CARBON-DIOXIDE	PROPYLENE-CARBONATE	124389	108327	0.0314	0.0010	0
3	BUTYLBENZENE	BENZENE	104518	71432	-0.0101	-0.0026	0
4	CARBON-DIOXIDE	ACETYLACETONE	124389	123546	0.0502	0.0637	0
5	CARBON-DIOXIDE	BUTYLBENZENE	124389	104518	0.0473	0.0328	0
6	SULFUR-DIOXIDE	BENZENE	7446095	71432	0.0494	0.0373	0
7	CARBON-DIOXIDE	BENZALDEHYDE	124389	100527	0.0355	0.0230	0
8	PROPYLENE	NITROGEN	115071	7727379	0.0642	0.0484	0
9	CARBON-DIOXIDE	n-HEXYL-ACETATE	124389	142927	0.0004	0.0043	0
10	CARBON-DIOXIDE	1-BROMOBENZENE	124389	108861	0.0462	0.0447	0
11	VINYL-ACETATE	ETHYLENE	108054	74851	-0.0159	-0.0040	0
12	ACETONE	NITROGEN	67641	7727379	0.0336	0.0354	0
13	CARBON-DIOXIDE	gamma-VALEROLACTONE	124389	108292	0.0466	0.0243	0
14	CARBON-DIOXIDE	DIETHYL-OXALATE	124389	95921	-0.0314	-0.0023	0
15	CARBON-DIOXIDE	1-PENTENE	124389	109671	0.0276	0.0082	0
16	CARBON-DIOXIDE	1-METHYLNAPHTHALENE	124389	90120	0.0422	0.0604	0
17	CARBON-DIOXIDE	METHYL-BENZOATE	124389	93583	0.0096	0.0179	0
18	DIETHYL-ETHER	CARBON-DISULFIDE	60297	75150	0.0057	0.0155	1
19	CARBON-DIOXIDE	ETHYL-BENZOATE	124389	93890	0.0212	0.0255	0
20	CARBON-DIOXIDE	METHYL-DODECANOATE	124389	111820	0.0210	0.0105	0
21	CARBON-DIOXIDE	STYRENE	124389	100425	0.0260	0.0329	0
22	CARBON-DIOXIDE	gamma-BUTYROLACTONE	124389	96480	0.0184	0.0221	0
23	CARBON-DIOXIDE	PHENYL-ACETATE-	124389	122792	-0.0077	0.0092	0
24	PROPYLENE	BENZENE	115071	71432	0.0087	0.0136	0
25	CARBON-DIOXIDE	DIETHYL-PHTHALATE	124389	84662	0.0050	0.0071	0
26	CARBON-DIOXIDE	DECANAL	124389	112312	-0.0080	0.0058	0
27	BENZENE	1-BROMOBENZENE	71432	108861	-0.0082	-0.0037	0
28	CARBON-DIOXIDE	o-XYLENE	124389	95476	0.0343	0.0323	0
29	CARBON-DIOXIDE	CYCLOHEXANONE	124389	108941	0.0157	0.0273	0
30	NITROGEN	TOLUENE	7727379	108883	0.1223	0.1402	0
31	CARBON-DIOXIDE	DIISOPROPYL-ETHER	124389	108203	0.0178	-0.0003	0
32	CARBON-DIOXIDE	ACETOPHENONE	124389	98862	0.0241	0.0227	0
33	CARBON-DIOXIDE	1-HEPTENE	124389	592767	0.0271	0.0133	0
34	CARBON-DIOXIDE	METHYL-tert-BUTYL-ETHER	124389	1634044	-0.0301	0.0037	0
35	CARBON-DIOXIDE	ISOPROPYL-ETHANOATE	124389	108214	0.0019	-0.0026	0
36	CARBON-DIOXIDE	CYCLOPENTENE	124389	142290	0.0312	0.0224	0
37	CARBON-DIOXIDE	CHLOROBENZENE	124389	108907	0.0351	0.0352	1
38	CARBON-DIOXIDE	N-METHYL-2-	124389	872504	0.0163	0.0131	0
		PYRROLIDONE					
39	CARBON-DIOXIDE	NONANAL	124389	124196	0.0033	0.0026	0
40	CARBON-DIOXIDE	TOLUENE	124389	108883	0.0246	0.0311	0
41	1-HEXENE	BENZENE	592416	71432	0.0011	0.0044	0
42	CARBON-DIOXIDE	DIETHYLENE-GLYCOL-	124389	111966	-0.0287	0.0078	0
		DIMETHYL-ETHER					

43	CARBON-DIOXIDE	1-OCTENE	124389	111660	0.0287	0.0109	0
44	CARBON-DIOXIDE	n-OCTYL-ACETATE	124389	112141	0.0294	0.0068	0
45	1-HEXENE	ETHYLENE	592416	74851	0.0443	0.0099	0
46	CARBON-DIOXIDE	2-METHYL-1-PENTENE	124389	763291	0.0028	0.0108	0
47	CARBON-DIOXIDE	DIETHYL-SUCCINATE	124389	123251	-0.0229	0.0012	0
48	CARBON-DIOXIDE	CUMENE	124389	98828	0.0432	0.0306	0
49	CARBON-DIOXIDE	1-HEXENE	124389	592416	0.0125	0.0091	0
	Test set						
50	BENZENE	CHLOROBENZENE	71432	108907	-0.0020	-0.0057	0
51	CARBON-DIOXIDE	CYCLOHEXYL-ACETATE	124389	622457	0.0073	0.0072	0
52	CARBON-DIOXIDE	ETHYLBENZENE	124389	100414	0.0345	0.0313	0
53	PROPYLENE	ETHYLENE	115071	74851	-0.0004	0.0015	0
54	CARBON-DIOXIDE	PROPYLBENZENE	124389	103651	0.0382	0.0339	0
55	BENZENE	TOLUENE	71432	108883	-0.0062	-0.0022	0
56	CARBON-DIOXIDE	m-XYLENE	124389	108383	0.0287	0.0304	0

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### Curriculum Vitæ

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#### Education

- 1993–1999 Pre-university education (Gymnasium-Lyceum), Athens, Greece.
- 1999–2005 Diploma in Chemical Engineering National Technical University of Athens *Thesis:* Contribution to anti-corrosive protection of steel using environmental friendly pigments. *Supervisor:* Prof. Panagiota Vassiliou
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2011–2015 PhD student Delft University of Technology *Thesis:* Integrated process and solvent design for CO<sub>2</sub> capture using Continuous Molecular Targeting - Computer Aided Molecular Design (CoMT-CAMD). *Promotors:* Prof. Dr.- Ing. Joachim Gross, Prof. Dr.- Ing. André Bardow

### Professional

2003	Internship
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2008–2011	Chemical engineer
2000 2011	AGET Heracles (Lafarge) - Cement Division, Evoia, Greece.
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	· · · · · · · · · · · · · · · · · · ·
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2013	Best Poster - CAST Directors Award 2013 from the Computing and
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2014	Second place award in the competition for best lecture in the $24^{\rm th}$
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### List of Journal Publications

- Stavrou, M.; Bardow, A.; Gross, J., Estimation of the binary interaction parameter k<sub>ij</sub> of the PC-SAFT Equation of State based on pure component parameters using a QSPR method, Fluid Phase Equilib. 416, 138 (2016)
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"As you set out for Ithaca hope the voyage is a long one, full of adventure, full of discovery. Laistrygonians and Cyclops, angry Poseidon—don't be afraid of them: you'll never find things like that on your way as long as you keep your thoughts raised high. as long as a rare excitement stirs your spirit and your body. Laistrygonians and Cyclops, wild Poseidon—you won't encounter them unless you bring them along inside your soul, unless your soul sets them up in front of you. Hope the vovage is a long one. May there be many a summer morning when, with what pleasure, what joy, vou come into harbors seen for the first time: may you stop at Phoenician trading stations to buy fine things. mother of pearl and coral, amber and ebony, sensual perfume of every kindas many sensual perfumes as you can; and may you visit many Egyptian cities to gather stores of knowledge from their scholars. Keep Ithaca always in your mind. Arriving there is what you are destined for. But do not hurry the journey at all. Better if it lasts for years, so you are old by the time you reach the island, wealthy with all you have gained on the way, not expecting Ithaca to make you rich. Ithaca gave you the marvelous journey. Without her you would not have set out. She has nothing left to give you now. And if you find her poor, Ithaca won't have fooled you. Wise as you will have become, so full of experience, you will have understood by then what these Ithacas mean."

(C.P. Cavafy, Collected Poems. Translated by Edmund Keeley and Philip Sherrard. Edited by George Savidis. Revised Edition. Princeton University Press, 1992)

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> Marina Mannheim, June 2017