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Simulations of the flow in the Mahakam river-lake-delta system, Indonesia

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1 Abstract

Large rivers often present a river-lake-delta system, with a wide range of temporal and spatial scales 2 of the flow due to the combined effects of human activities and various natural factors, e.g. river 3 discharge, tides, climatic variability, droughts, floods. Numerical models that allow for simulating 4 the flow in these river-lake-delta systems are essential to study them and predict their evolution 5 under the impact of various forcings. This is because they provide information that cannot be easily 6 measured with sufficient temporal and spatial detail. In this study, we combine one-dimensional 7 sectional-averaged (1D) and two-dimensional depth-averaged (2D) models, in the framework of the 8 finite element model SLIM, to simulate the flow in the Mahakam river-lake-delta system 9 (Indonesia). The 1D model representing the Mahakam River and four tributaries is coupled to the 10 2D unstructured mesh model implemented on the Mahakam Delta, the adjacent Makassar Strait, 11 and three lakes in the central part of the river catchment. Using observations of water elevation at 12 five stations, the bottom friction for river and tributaries, lakes, delta, and adjacent coastal zone is 13 calibrated. Next, the model is validated using another period of observations of water elevation, 14 flow velocity, and water discharge at various stations. Several criteria are implemented to assess the 15 quality of the simulations, and a good agreement between simulations and observations is achieved 16 in both calibration and validation stages. Different aspects of the flow, i.e. the division of water at 17 two bifurcations in the delta, the effects of the lakes on the flow in the lower part of the system, the 18 area of tidal propagation, are also quantified and discussed. 19

20 Keywords

21

Mahakam River, coupled 1D / 2D model, SLIM, river-lake-delta system

22 **1 Introduction**

Large rivers such as the Mekong River (Southeast Asia) hosting a river-lake-delta system consist of 23 various interconnected regions such as a river and its tributaries, lakes, floodplains, delta or estuary, 24 and adjacent coastal ocean. In such river-lake-delta systems, continuous interactions and exchange 25 of water between interconnected regions exist, under the combined effects of riverine and marine 26 forcings (e.g. river discharge, tides), mutual influences of natural processes (e.g. climatic 27 variability, droughts, floods), and human activities [1,2]. As a results, a wide range of temporal and 28 spatial scales of motion can be observed [2]. Such systems also feature complex geometries, 29 especially in deltaic or estuarine regions [2,3]. Therefore, a global system approach that is able to 30 handle the flow in the whole river-lake-delta system is required, to understand the complex flow 31 processes occurring at different temporal and spatial scales and to study related issues, e.g. transport 32 processes of sediment, morphology, ecological status of coastal waters. 33

Detailed and long-term field measurements (e.g. flow velocity, flow depth, water discharge) 34 allow for an accurate study of the flow, but are generally time-consuming and rarely obtained over 35 long time intervals and at different locations due to the highly spatial and temporal variability of the 36 phenomena. As regards numerical simulations, an integrated model, which allows for representing 37 the flow from the upstream end of the system to the coastal ocean and the deep margin, is essential 38 to take into account properly the interactions between river flow, hydraulic processes, and tidal 39 effects on the entire river-lake-delta systems. While existing studies primarily investigate the flow 40 processes locally in each interconnected region of river-lake-delta systems, taken individually, it is 41 becoming computationally feasible to adopt such an integrated approach, without excessive 42 simplification of the physical processes resolved by the model. 43

Using a full three-dimensional (3D) model for simulating the flow in river-lake-delta systems is however likely to exceed the available computer resources because the area of such systems is of the order of thousands of square kilometers. The data required to run such models are also not easily available, as well as field measurements to validate the implementation of the model. Among different simpler models developed for simulating the flow in riverine and marine water environments as well as in continuums such as river-lake-delta systems, a coupled one-dimensional section-averaged and two-dimensional depth-averaged (1D / 2D) model is a tool of choice, for it is more efficient in terms of computational cost than a full 2D or 3D model [3-7].

Wu and Li [4] applied a coupled 1D / 2D quasi-steady model to study the flow in the fluctuating 52 backwater region of the Yangtze River while Zhang [5] used a 1D / 2D unsteady model to simulate 53 the flow in the offshore area near the Yellow River mouth (China). Martini et al. [6] applied a 54 coupled 1D / 2D model for simulating the flood flows in the Brenta River (Veneto, Italy). Later, 55 Cook and Merwade [7] combined the simulation results from a coupled 1D / 2D model and datasets 56 obtained from different river bathymetry sources in order to quantify the resulting differences in the 57 inundation maps for Strouds Creek reach and Brazos River (USA). Recently, de Brye et al. [3] 58 developed a coupled 1D / 2D finite element model for reproducing the flow dynamics in the Scheldt 59 Estuary and tidal river network. These examples strongly suggest that a coupled 1D / 2D model can 60 be used to reproduce the flow in river-lake-delta systems. 61

In the framework of a coupled 1D / 2D model, the 2D model is often developed in the part of the 62 domain of interest, e.g. delta or estuary, where the accurate representation of the topography and 63 complex coastlines is required. In this 2D calculation area, different numerical methods and grids 64 were used, for example, finite difference method by Wu and Li [4] and Zhang [5], finite element 65 method and structured mesh by Cook and Marwade [7], finite element method and an unstructured 66 mesh by Martini et al. [6] and de Brye et al. [3]. Finite-element or finite-volume models using 67 unstructured meshes constitute a promising option to deal with the multi-physics and multi-scale 68 features of the problem [8,9], especially in deltaic and estuarine regions exhibiting a large number 69 of narrow channels [3]. This is because unstructured meshes allow for a more accurate 70 representation of complex topographies and an increase in spatial resolution in areas of interest, as 71 was done, for example, in the simulations of the flow in the Great Barier Reef [10]. 72

73

The present study aims at (i) applying an existing unstructured-mesh, finite element model, i.e.

SLIM (www.climate.be/slim), in which one-dimensional sectional-averaged and two-dimensional 74 depth-averaged shallow-water equations are coupled, to simulate the flow in the Mahakam 75 river-lake-delta system, (ii) accurately reproducing the observations of the flow (i.e. water elevation, 76 flow velocity, and water discharge) at various locations in the system, (iii) investigating the division 77 of water at two bifurcations in the deltaic region, (iv) providing a preliminary investigation of the 78 effects of the lakes on the flow in the lower part of the system, and (v) identifying the area of tidal 79 propagation in the system. Besides these objectives, the study also allowed to represent the 80 numerous distributaries in the deltaic region with a refined accuracy and to determine appropriate 81 values of the bottom friction coefficients in different parts of the considered river-lake-delta system. 82 The paper first introduces the Mahakam river-lake-delta system. Then, the finite element model 83 used in the study and the model established for the studied system are described. The detailed 84 calibration procedure of the modelling parameters and the validation of the model using available 85 observations of the flow (e.g. water elevation, flow velocity, and water discharge) are also presented 86

⁸⁷ before discussing related issues, e.g. effects of grid resolution. Finally, conclusions are drawn.

88 2 The Mahakam river-lake-delta system

The Mahakam River is located in the East Kalimantan province of Borneo, Indonesia (Fig. 1). The 89 river-lake-delta system consists of the Mahakam River and its tributaries, lakes, the Mahakam Delta, 90 and the adjacent Makassar Strait. The river meanders over 900 km and its catchment area covers 91 about 75,000 km², with a mean annual river discharge of the order of 3,000 m³/s [11]. The river is 92 characterized by a tropical rain forest climate with a dry season from May to September and a wet 93 season from October to April. In the river catchment, the mean daily temperature varies from 24 to 94 29°C while the relative humidity lies between 77 and 99% [12]. The mean annual rainfall varies 95 between 4,000 and 5,000 mm/year in the central highlands and decreases from 2,000 to 3,000 96 mm/year near the coast [13]. A bimodal rainfall pattern with two peaks of rainfall occurring 97 generally in December and May is reported in the river catchment [12]. Due to the regional climate 98 and the global air circulation, the hydrological conditions in the river catchment vary significantly, 99

especially in ENSO (El Nino-Southern Oscillation) years such as in 1997, leading to significant
 variations of flow in the river and downstream region, i.e. the delta [12].

In the middle part of the Mahakam River catchment, there are four tributaries (i.e. Kedang Pahu, 102 Belayan, Kedang Kepala, and Kedang Rantau) and over thirty shallow-water lakes covering a total 103 area of about 400 km². These lakes are connected to the Mahakam River system through small 104 channels (Fig. 1). The water collected over vast regions of the land around these lakes can be stored 105 in the lakes. Obviously, the water from the connected channels can flow into or out of the lakes, 106 depending on the season, e.g. flood or drought periods. For instance, these lakes act as a buffer of 107 the Mahakam River and regulate the water discharge in the lower part of the river through the 108 damping of flood surges [14]. During the dry season, tides can also force a flow into the lakes. 109 Therefore, studies of the flow in the Mahakam river-lake-delta system have to take into account the 110 interconnections between these lakes and the river. 111

Downstream of the Mahakam River, the Mahakam Delta presents a multi-channel network including a large number of active distributaries and tidal channels. The delta is symmetrical with a radius of approximately 50 km, as measured from the delta shore to the delta apex. The width of the channels in the deltaic region ranges from 10 m to 3 km. The delta discharges into the Makassar Strait, whose width varies between 200 and 300 km, with a length of about 600 km. Located between the islands of Borneo and Sulawesi, the Makassar Strait is the main passage for the transfer of water and heat from the Pacific to the Indian Ocean by the Indonesian Throughflow [15,16].

119 Complex coastlines are present in the delta (Fig. 1). Such complex coastlines might have a 120 significant impact on the flow [17]. This means that the effects of complex coastlines have to be 121 taken into account in studies of the flow. In addition, because of the multi-channel network, many 122 bifurcations are also inherently exhibited in the delta. Division of water discharge at these 123 bifurcations should be accurately represented since it affects not only the flow dynamics [2] but also 124 the sediment distribution and morphology in the adjacent channels [18].

125

The Mahakam Delta is a mixed tidal and fluvial delta. The tide in the delta is dominated by

semidiurnal and diurnal regimes, with a predominantly semidiurnal one. The tidal range decreases
from the delta front to upstream Mahakam River and its value varies between 3 and 1 m, depending
on the location and the tidal phase (e.g. neap or spring tides) under consideration.

Partial mixing is reported in the delta, based on the vertical distribution of salinity collected at different locations [14]. The limit of salt intrusion is located around the delta apex [14,19,20]. Temperature data collection at 29 locations in the whole delta [20] shows that the temperature varies from 29.2 to 30.5°C at the surface and from 29.2 to 30.8°C at the bottom. This suggests that there is no large difference of water temperature in the water column and between stations for different tidal conditions.

Large parts of the open waters in the delta are sheltered from wind action by vegetation and thus 135 the influence of the wind will not be taken into account in the calculations presented hereinafter. 136 The effect of wind on the flow in the lakes is also disregarded, mainly because there are not 137 available wind data in this region. In the Makassar Strait, the effect of the wind is limited due to 138 low-level wind speed. In terms of wind-induced surface waves, the average wave height is about 0.3 139 m at a distance of 14 km offshore and the maximum wave height is less than 0.6 m with the largest 140 waves approaching from the southeast [21]. Due to the limited fetch in the narrow strait of the 141 Makassar and low-level wind speed, the mean value of the significant wave height is also less than 142 0.6 m and the wave energy that affects the deltaic processes is very small [14]. Therefore, the 143 effects of wind and waves are assumed to be negligible in this study. 144

145 **3 Model**

146 **3.1 Governing equations**

The two-dimensional depth-averaged shallow-water equations are applied in the Mahakam Delta, lakes, and the Makassar Strait. The elevation η of the water surface above the reference level and the depth-averaged horizontal velocity vector $\mathbf{u} = (u, v)$ are obtained by solving the following equations:

$$\frac{\partial \eta}{\partial t} + \nabla \cdot (H\mathbf{u}) = 0 \tag{1}$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot (\nabla \mathbf{u}) + f \mathbf{k} \times \mathbf{u} + g \nabla \eta = \frac{1}{H} \nabla \cdot \left[H \mathbf{v} (\nabla \mathbf{u}) \right] - \frac{\mathbf{\tau}_{\mathbf{b}}}{\rho H}$$
(2)

where *t* is the time and ∇ is the horizontal del operator; $H = \eta + h$ is the water depth, with *h* being the water depth below the reference level (taken as the mean sea level); $f = 2\omega \sin \phi$ is the Coriolis parameter, ω is the Earth's angular velocity and ϕ is the latitude, **k** is the unit upward vector; g is the gravitational acceleration; ρ is the water density (assumed constant); v is the horizontal eddy viscosity; $\tau_{\mathbf{b}}$ is the bottom shear stress, which is parameterized using the Manning-Strickler formulation:

$$\boldsymbol{\tau}_{\mathbf{b}} = \rho \frac{g n^2 \| \mathbf{u} \|}{H^{1/3}} \mathbf{u}$$
(3)

where *n* is the Manning coefficient, generally depending on the physical properties of the riverbed and the seabed. Basically, the value of *n* is calibrated in order to reproduce the flow as well as possible.

The eddy viscosity v is evaluated using the Smagorinsky formula [22]: 160

$$\mathbf{v} = \left(0.1\Delta\right)^2 \sqrt{2\left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x}\right)^2 + 2\left(\frac{\partial v}{\partial y}\right)^2} \tag{4}$$

where Δ is the local characteristic length scale of the element, i.e. the longest edge of a triangle in the 2D unstructured mesh. The Smagorinsky formula arises from the unresolved turbulence at the subgrid scale and depends on the strain-rate of the velocity field. The energy production and dissipation of the small scales are assumed to be in equilibrium in this formula.

¹⁶⁵ The continuity and momentum equations are integrated over the river cross-section in the ¹⁶⁶ Mahakam River and tributaries, yielding the following one-dimensional equations

$$\frac{\partial A}{\partial t} + \frac{\partial (Au)}{\partial x} = 0 \tag{5}$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + g \frac{\partial \eta}{\partial x} = \frac{1}{A} \frac{\partial}{\partial x} \left(v A \frac{\partial u}{\partial x} \right) - \frac{\tau_{\rm b}}{\rho H}$$
(6)

where A is the cross-sectional area, H = A/b is the effective water depth, and b is the river width.

¹⁶⁸ The bottom shear stress τ_b in the 1D model is computed using Manning's formula as:

$$\tau_{\rm b} = \rho \frac{g n^2 |u|}{H^{1/3}} u. \tag{7}$$

169

$$\mathbf{v} = 0.16u_*H \tag{8}$$

The eddy viscosity is parameterized using the zero-equation turbulent model [23], under the form:

where u_* is the shear velocity, which is calculated as $u_*^2 = c_f u^2$, with c_f being a coefficient obtained from Manning's formula ($c_f = gn^2 H^{-1/3}$).

172 **3.2 Wetting and drying algorithm**

In the river-lake-delta system and particular in the deltaic region, several areas can be wet or dry 173 depending on the water elevation and tidal conditions. An accurate representations of these wetting 174 / drying areas is crucial and mandatory in any model aimed at reproducing the flow in such systems. 175 In this paper, we use the wetting and drying algorithm designed by Kärnä et al. [24]. This means 176 that the actual bathymetry (i.e. the water depth h below the reference level) is modified according to 177 a smooth function f(H) as $h_m = h + f(H)$, to ensure a positive water thickness at any time. The 178 smooth function has to satisfy the following properties. Firstly, the modified water depth (i.e. 179 $H_m = h_m + \eta$) is positive at any time and position. Secondly, the difference between the real and 180 modified water depths is negligible when the water depth is significantly positive. Thirdly, the 181 smooth function is continuously differentiable to ensure convergence of Newton iterations when 182 using an implicit time stepping. The following function, which satisfies the properties described 183 above, is used: 184

$$f(H) = \frac{1}{2} \left(\sqrt{H^2 + \xi^2} - H \right)$$
(9)

where ξ is a free parameter controlling the smoothness of the transition between dry and wet situations, with the smaller value of ξ corresponding to the smaller the transition zone [24]. The modified water depth, i.e. $H_m = h_m + \eta$ will be equal to $\xi/2$ when H = 0, revealing that ξ also directly controls the water depth in the dry area. In our calculations, a value $\xi = 0.5$ m is adopted for modifying the bathymetry, in order to maintain the positive water depth.

¹⁹⁰ Using the redefined total water depth, the depth-averaged shallow-water equations (1)-(2) are

¹⁹¹ modified slightly, resulting in the following forms:

$$\frac{\partial \eta}{\partial t} + \frac{\partial h_m}{\partial t} + \nabla \cdot \left(H_m \mathbf{u} \right) = 0 \tag{10}$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot (\nabla \mathbf{u}) + f \mathbf{k} \times \mathbf{u} + g \nabla \eta = \frac{1}{H_m} \nabla \cdot \left[H_m \mathbf{v} (\nabla \mathbf{u}) \right] - \frac{\mathbf{\tau}_{\mathbf{b}}}{\rho H_m}$$
(11)

¹⁹² The appearance of the second term in eq. (10) is due to the redefinition of the bathymetry.

3.3 Finite element implementation

The governing equations (5)-(6) and (10)-(11) are solved by means of an implicit discontinuous 194 Galerkin finite element method (DG-FEM) in the framework of the unstructured-mesh, finite 195 element model SLIM (www.climate.be/slim, [3,24,25]). To avoid a repeated description of the 196 model and its capabilities, only general information about the finite element (FE) implementation of 197 these equation is presented below. The computational domain is discretized into triangle elements 198 and line segments as shown in Fig. 4. The governing equations are multiplied by test functions and 199 then integrated by parts over each element or segment, resulting in element-wise surface and 200 contour integral terms for the spatial operators. The surface term is estimated using a linear shape 201 function. An approximate Riemann solver is used for computing the fluxes at the interfaces between 202 two adjacent elements or segments in order to represent properly the water-wave dynamics in 203 contour terms [25]. A second-order diagonally implicit Runge-Kutta method is used for the 204 temporal derivative operator [24] and a time step of 10 minutes is used in this study. At the 205 interfaces between the 1D and 2D models, the local conservation is guaranteed by compatible one 206 and two dimensional numerical fluxes [3]. 207

3.4 Treatment of channel confluences in the 1D model

To impose suitable conditions at the interface of a confluence point (where waters in two channels flow into a single channel) in the Mahakam River, a special treatment is needed because of the following reasons. Firstly, one computational confluence node is associated with three nodal values and the usual Riemann solver [40] cannot be resorted to compute the numerical fluxes at the interface of a confluence node. Secondly, a confluence node can be handled rather easily in conservative finite difference models, but not in finite element ones [26]. In this study, we

implemented a method inspired by Sherwin et al. [26] for arterial systems. This means that the 215 characteristic variables are used to compute the fluxes at the interface of the confluence point, 216 together with the continuity of mass and momentum. The detailed derivation of these characteristic 217 variables from the governing equations is described below. The governing equations (5) and (6) can 218 be expressed in a vector form as 219

$$\frac{\partial \mathbf{U}}{\partial t} + \mathbf{A} \frac{\partial \mathbf{U}}{\partial x} = \mathbf{S}$$
(12)
where $\mathbf{U} = \begin{pmatrix} A \\ u \end{pmatrix}, \ \mathbf{A} = \begin{pmatrix} u & A \\ g/b & u \end{pmatrix}, \ \mathbf{S} = \begin{pmatrix} 0 \\ \frac{1}{A} \frac{\partial}{\partial x} \left(vA \frac{\partial u}{\partial x} \right) - \frac{\tau_b}{\rho H} \end{pmatrix}.$

The eigenvalues of the eq. (12) can be easily obtained by solving the equation $det(\mathbf{A} - \lambda \mathbf{I}) = 0$. The 221 eigenvalues, λ_1 and λ_2 , are real: 222

$$\lambda_1 = u + \sqrt{\frac{gA}{b}}$$
 and $\lambda_2 = u - \sqrt{\frac{gA}{b}}$. (13)

The characteristic variables W can be determined by using the expression $W=K^{-1}U$, with K being 223 the eigenmatrix whose elements are determined from the eigenvalues: 224

$$\mathbf{K} = \begin{pmatrix} 1 & 1\\ \sqrt{\frac{g}{Ab}} & -\sqrt{\frac{g}{Ab}} \end{pmatrix}.$$
 (14)

Finally, the characteristic variables **W** are obtained: 225

$$\mathbf{W} = \begin{bmatrix} \frac{1}{2} \left(A + u \sqrt{\frac{Ab}{g}} \right) \\ \frac{1}{2} \left(A - u \sqrt{\frac{Ab}{g}} \right) \end{bmatrix}.$$
 (15)

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220

Because the discontinuous Galerkin method is applied at a confluence point, one computational confluence node is associated with 3 nodal values (Fig. 2) and thus six unknowns, i.e. sectional area 227 and velocity of each node. If these six variables $(A_l, u_l, A_{r1}, u_{r1}, A_{r2}, and u_{r2})$ at the interface are 228 known, we can compute the six upwind variables $(A_{ul}, u_{ul}, A_{ur1}, u_{ur1}, A_{ur2}, and u_{ur2})$ by imposing the 229 characteristic variables from eq. (15) and by using the continuity of mass and momentum fluxes at 230 the confluence. The characteristic variables at the interfaces of the confluence point are assumed to 231 remain constant: 232

$$\frac{1}{2}\left(A_{l}+u_{l}\sqrt{\frac{A_{l}b_{l}}{g}}\right)=\frac{1}{2}\left(A_{ul}+u_{ul}\sqrt{\frac{A_{ul}b_{l}}{g}}\right)$$
(16)

$$\frac{1}{2} \left(A_{r1} - u_{r1} \sqrt{\frac{A_{r1}b_{r1}}{g}} \right) = \frac{1}{2} \left(A_{ur1} - u_{ur1} \sqrt{\frac{A_{ur1}b_{r1}}{g}} \right)$$
(17)

$$\frac{1}{2} \left(A_{r2} - u_{r2} \sqrt{\frac{A_{r2}b_{r2}}{g}} \right) = \frac{1}{2} \left(A_{ur2} - u_{ur2} \sqrt{\frac{A_{ur2}b_{r2}}{g}} \right)$$
(18)

$$A_{ul}u_{ul} = A_{ur1}u_{ur1} + A_{ur2}u_{ur2}$$
(19)

$$\frac{1}{2}u_{ul}^2 + g\eta_{ul} = \frac{1}{2}u_{ur1}^2 + g\eta_{ur1}$$
(20)

$$\frac{1}{2}u_{ul}^2 + g\eta_{ul} = \frac{1}{2}u_{ur2}^2 + g\eta_{ur2}$$
(21)

where η_{ui} and b_i are respectively the elevations and widths corresponding to the river cross-section areas A_i , with i=l, r1, r2. The non-linear system of six algebraic equations (16)-(21) is solved by means of the Newton-Raphson method. The fluxes at the interfaces are directly calculated from the characteristic variables.

It is worth realizing that a confluence point in the Mahakam River can become a bifurcation point (where water in a single channel is divided into two channels) due to the variations of the water discharge and tides. In that case, the numerical fluxes at the interfaces of the bifurcation point are computed using the computational procedure introduced above.

241 **4 Model setup**

242 4.1 Computational domain

The domain of interest in this study is limited to the region of tidal influence of the Mahakam river-lake-delta system (Fig. 1). This domain comprises 300 km of the Mahakam River and four tributaries, the three largest lakes (i.e. Lake Jempang, Lake Melingtang, and Lake Semayang) located about 150 km upstream of the delta, the Mahakam Delta, and the Makassar Strait. The four tributaries (i.e. Kedang Pahu, Belayan, Kedang Kepala, and Kedang Rantau) located in the middle part of the Mahakam River are included because they greatly contribute to the river flow. Also, among over thirty shallow-water lakes in the middle river catchment, the three largest lakes mentioned above are taken into account in the computational domain since, again, these lakes act as
a buffer of the river and regulate the water discharge in the lower part of the river. Finally, the
multi-channel network in the delta is included in detail in the computational domain for taking into
account several physical processes in the calculations.

4.2 Bathymetry

Data sets from various sources are available to represent the bathymetry of the studied system. The 255 bathymetric data obtained from fieldwork campaigns with a single-beam echosounder during a 256 period between 2008 and 2009 [27] are employed for the delta, the three lakes, and the river. The 257 depth of the deltaic channels ranges from 5 to 15 m (see Fig. 3) while the water depth is of the order 258 of 5 m in the three lakes. The water depth in the river varies greatly, and can reach up to 45 m in 259 some meanders. In the Mahakam River and the four tributaries, the bathymetric data are used to 260 interpolate river cross-sections. The global bathymetric GEBCO database (www.gebco.net) is used 261 in the Makassar Strait and for the adjacent continental shelf. 262

4.3 Grid of the computational domain

The grid of the computational domain consists of a 2D sub-domain covering the three lakes, the 264 whole delta, and the Makassar Strait and a 1D sub-domain representing the Mahakam River and 265 four tributaries. The 2D sub-domain is discretized by means of an unstructured triangular grid 266 whose resolution varies greatly in space while the river network within the 1D sub-domain has a 267 resolution of about 100 m between cross-sections (Fig. 4). The 2D sub-domain allows for a very 268 detailed representation of the delta. The resolution in the deltaic channels is such that there are at 269 least two triangles (or elements) over the width of each tidal channel in the delta. The element (or 270 mesh) size varies from 5 m in the narrowest branches of the delta to around 10 km in the deepest 271 part of the Makassar Strait. The grid shown in Fig. 4 comprises 60,819 triangular elements and 272 3,700 line segments. This grid is generated using the open-source mesh generation software GMSH 273 (www.geuz.org/gmsh, [28,29]). 274

275

The current unstructured grid allows for an accurate representation of the very complex

shorelines. The refinement criteria of the grid takes into account (i) the speed of the external gravity wave (\sqrt{gh}) [3,30,31] and (ii) the distance to the delta apex and coastlines in order to cluster grid nodes in regions where small scale processes are likely to take place.

It must be emphasized that in comparison with the computational grids used in previous studies 279 [2,27,32] of the Mahakam Delta, the present computational grid is the first attemp to include most 280 of the meandering and tidal branches as well as the creeks in the delta together with the main deltaic 281 channels. The use of a model with such refinement of the computational grid is an important 282 achievement because a wide range of temporal and spatial scales of several physical processes (e.g. 283 tides, river flow) interacting with each other in the narrow and meandering tidal branches can be 284 included in the calculations. For instance, Mandang and Yanagi [32] studied the dynamics of tide 285 and tidal currents in the delta using a three-dimensional finite difference model, ECOMSED, with a 286 structured grid that had a resolution of 200 meters. Such a horizontal grid resolution is unlikely to 287 be suitable to represent the complex shorelines as well as the many small tidal channels existing in 288 the delta. This is the reason why only the main deltaic channels are included in their study. An 289 unstructured mesh comprising only the main deltaic channels is also used in the study of de Brye et 290 al. [2], who quantified the division of water discharge through the main channels of the delta. Then, 291 Sassi et al. [27] used exactly the same mesh to study the tidal impact on the division of water 292 discharge at the delta apex (DAN and DAS) and first (FBN and FBS, in Fig. 4) bifurcations. 293

4.4 Boundary and initial conditions

As shown in Fig. 4, the downstream boundaries of the system are located at the entrance and the outlet of the Makassar Strait. The upstream boundaries are imposed at the city of Melak in the Mahakam River, where the tidal influence on the flow is negligible, and at the upstream end of the four tributaries (see Fig. 4b). The measured daily water discharge is imposed at the upstream boundary of the Mahakam River and the calculated daily water discharge from a rainfall-runoff model is prescribed at the upstream boundaries of the four tributaries. The tidal components (elevation and velocity harmonics) from the global ocean tidal model TPXO7.1 [33] are imposed at the downstream boundaries. This global ocean tidal model allows for combining rationally both dynamic information from hydrodynamic equations and direct observation data from tide gauges and satellite altimetry [33]. In addition, this model also provides the best fits, in the least-squares sense, of the Laplace tidal equations and along-track averaged data from Topex/Poseidon and Jason satellites data [3,33].

Along the impermeable boundaries of coastlines, lakes, and the multi-channel network in the delta, the tangential stress is estimated using the following formulation:

$$v \frac{\partial u_t}{\partial n} = \alpha u_t \tag{22}$$

where α is the slip coefficient, $\partial u_t / \partial n$ is the normal derivative of the tangential velocity u_t . The constant coefficient α lies between zero and infinity, corresponding to free slip and no-slip conditions, respectively [34]. A finite value of α corresponds to a partial slip condition. In the current calculations, the adopted value $\alpha = 10^{-3}$ m/s [2] is applied, to allow for taking into account the effect of the transversal and tangential momentum flux along the impermeable boundaries.

The initial velocity in the computational domain is set equal to zero and an arbitrary value of 0.5 m is used for the initial water elevation, except in the lakes where a measured value of water elevation is imposed in the calibration step and a calculated value is used in the validation step. A spin up period of one neap-spring tidal cycle (about 15 days) is applied before the beginning of the period of interest. Regime conditions can be reached quickly after a few days and thus the effects of the initial conditions can be eliminated completely.

Calculations were performed using the high-performance computing facilities of the Université catholique de Louvain (<u>www.uclouvain.be/cism</u>). We used 24 processors in parallel for calculations and it takes about 1.5 days to simulate a period of 1 month using the refined computational grid shown in Fig. 4.

5 Calibration and validation results

325 5.1 Observations and simulation periods

In situ measurements including water elevation, flow velocity, and water discharge at various 326 stations are available for estimating approximate values of the Manning coefficient in the system. 327 Observations of water elevation at five stations (i.e. JWL, Pela Mahakam, Delta Apex, Delta North, 328 Delta South, see Fig. 1) from May to August 2008 are used for calibration purposes (Section 5.3) 329 while the long-term observations of water elevation (at Pela Mahakam, Muara Karman, Delta Apex, 330 Delta North, and Delta South), flow velocity and water discharge (at Samarinda, DAN, DAS, FBN, 331 and FBS) between October 2008 and June 2009 are employed for the validation of the model 332 (Section 5.4). The water discharge at the upstream boundary in the Mahakam River varies between 333 1,200 and 2,300 m³/s during the calibration period while it ranges from 870 to 2,800 m³/s in the 334 validation period. 335

5.2 Error estimates

Three different types of error, i.e. the root mean square (RMS) error, mean absolute error (MAE), and the Nash-Sutcliffe efficiency (NSE) are used to assess the quality of the simulations. The RMS error, MAE, and NSE are computed as follows:

RMS error =
$$\sqrt{\frac{1}{N} \sum_{j=1}^{N} \left(X_{data,j} - X_{model,j} \right)^2}$$
 (23)

$$MAE = \frac{1}{N} \sum_{j=1}^{N} \left| X_{data,j} - X_{model,j} \right|$$
(24)

NSE =
$$1 - \frac{\sum_{j=1}^{N} (X_{model,j} - X_{data,j})^2}{\sum_{j=1}^{N} (X_{data,j} - X_{data,m})^2}$$
 (25)

where $X_{data,j}$ and $X_{model,j}$ are respectively the observations and model results of the quantity of interest, at the point number *j* in a time-series, $X_{data,m}$ is the mean value of observed quantity of interest, and *N* is the total number points in the considered time-series.

The RMS error is the most commonly used in practical applications. However, as shown in eq.

(23) for the RMS error, the differences between observed and computed values are calculated as square values (inside the square). Thus, the importance of larger values in time-series may be overestimated whereas lower values are neglected [35]. This is the reason why the MAE is additionally used. The RMS error and MAE are valuable indicators because they provide the error in the units of the quantity of interest, which is helpful in the analysis of the results. The NSE coefficient, that determines the relative magnitude of the residual variance (or noise) compared to the observations variance, is used to provide extensive information of comparisons.

The Pearson's correlation coefficient (r) is also applied for assessing the trend between computed results and observed data. The coefficient r is calculated as:

$$r = \frac{\sum_{j=1}^{N} (X_{data,j} - X_{data,m}) (X_{model,j} - X_{model,m})}{\sqrt{\sum_{j=1}^{N} (X_{data,j} - X_{data,m})^2} \sqrt{\sum_{j=1}^{N} (X_{model,j} - X_{model,m})^2}},$$
(26)

where $X_{model, m}$ is the mean value of computed results.

5.3 Calibration results

To calibrate the Manning coefficient, the computational domain of the Mahakam river-lake-delta 355 system is provisionally divided into three regions, i.e. Mahakam River and tributaries, lakes, and 356 delta and Makassar Strait. Different simulations are performed by using a constant Manning 357 coefficient in each flow region. The Manning coefficient in the lakes changes from $0.023 \text{ s/m}^{1/3}$ to 358 $0.045 \text{ s/m}^{1/3}$ while its value lies between 0.0175 s/m^{1/3} and 0.0325 s/m^{1/3} in the river and tributaries. 359 In the remaining flow region, the Manning coefficient ranges from 0.019 s/m^{1/3} to 0.035 s/m^{1/3}. 360 Three values in each of the abovementioned ranges are selected for calibration purposes, resulting 361 in twenty seven simulations (Table 1). According to the RMS errors of water elevation at five 362 stations, the optimal value of the roughness coefficient is obtained in simulation a.14 (Table 1), with 363 a value of 0.0275 s/m^{1/3}, 0.0305 s/m^{1/3}, and 0.023 s/m^{1/3} for the river and tributaries, lakes, and delta 364 and Makassar Strait, respectively. A slight improvement is obtained with an additional simulation 365 where the Manning coefficient is taken as in simulation a.14 in the river and the lakes (i.e. 0.0275 366

and 0.0305), and then in the delta its value decreases linearly with the distance from the 1D / 2D connecting location (Fig. 4b) to the delta front, from 0.0275 s/m^{1/3} to 0.023 s/m^{1/3}. Finally, the Manning coefficients corresponding to this additional simulation are considered as the optimal values. The computed water elevation obtained from this optimal distribution of the Manning coefficient is shown in Fig. 5 and Fig. 6 while the RMS error, MAE, NSE, and *r* coefficient at five stations are listed in Table 2.

Fig. 5 shows comparisons between observed and computed water elevations at JWL and Pela Mahakam stations. The model reproduces very well the observed water elevation at these stations. The RMS error of water elevation is only 6 cm at Pela Mahakam and 13 cm at JWL station during the comparable period. The MAE is less than 10 cm and the NSE coefficient is greater than 0.93, indicating that the model reproduces very well the observations. The correlation coefficient *r* is close to unity, revealing that both computed and observed water elevations show similar behaviors or variation trends during the calibration period.

In Lake Jempang, both simulations and observations show clearly that the tidal signal is of a 380 marginal importance (Fig. 5a). These results suggest that the tide propagates up to a location located 381 downstream of the lakes or around the Pela Mahakam. A discrepancy in the water elevation of 382 about 20 cm occurs on 2008-06-16 at JWL station in the lake. This difference between observations 383 and simulated water elevation can be explained by the lateral flow into the lake that is not taken into 384 account in our simulations. At station Pela Mahakam, which is located closer to the delta, the tidal 385 signal is felt more clearly than in the Lake Jempang (Fig. 5b). However, the fluctuation of the water 386 elevation due to the tide at this station is still relatively small. 387

Fig. 6 shows the computed water elevation and the observations at Delta Apex, Delta South, and Delta North. A very good agreement between computed and observed water elevations is obtained at all three stations in the delta. The largest value of RMS errors at these stations is less than 13 cm in the two months period that is available for calibration. This error is only about 6.5% of the observed tidal range (i.e. about 2.0 m) at these stations. The MAE is more or less 5 cm while both NSE and r coefficients are very close to unity.

An overestimation of low water elevation is observed at Delta Apex station. The use of approximate river discharges at the upstream tributaries, which are estimated from a rainfall-runoff model, could be the main reason for the error, as these estimates are less accurate for low flows. Another reason may be the use of a constant value of the bottom friction in the Mahakam River upstream of the station.

399 **5.4 Validation results**

Using the optimal values of the Manning coefficient obtained in the calibration step, a simulation for a 9 months period (from October 2008 to June 2009) is performed to validate the model and the parameters. The calculation errors and the detailed comparisons between computed results and observed data are presented for water elevation, flow velocity, and water discharge at various stations along the system under study.

405 5.4.1 Water elevation

As shown in Fig. 7a, the model reproduces very well the observed water elevation at Pela Mahakam station during the period from 2008-11-11 to 2008-11-19. The RMS error is only about 4 cm while the MAE is 3 cm (Table 3). The NSE and r coefficients are respectively 0.97 and 0.98 (Table 3), revealing that the model reproduces very well the observed values. These results suggest that appropriate values of the Manning coefficient were obtained for the upstream Mahakam River and tributaries and lakes.

In addition, there is only a minor tidal signal at Pela Mahakam station as shown in the calibration step. This result shows again that the tide propagates up to the Pela Mahakam location in the Mahakam River.

At Muara Karman station, which is located in the region downstream of the three tributaries (River Belayan, Kelang Kepala, and Kedang Rantau) and the lakes, the model reproduces rather well the observed water elevation (Fig. 7b). The RMS error, MAE, NSE, and *r* coefficient are equal to 10 cm, 7 cm, 0.89, and 0.95, respectively, for a two weeks period from 2008-11-04 to 2008-11-19. However, an overestimation and underestimation of the computed water elevation is
observed at this station. Again, this difference can be explained by the inaccuracy of the water
discharge imposed at the upstream boundaries in the tributaries.

As is the case for the calibration results, the model predicts very well the observed water elevation at three stations, namely Delta Apex, Delta South, and Delta North as shown in Fig. 8. The RMS error of water elevation is less than 12 cm at these stations. The MAE is about 9 cm while the NSE and r coefficients are about 0.95 (Table 3), indicating that the model correctly simulates the observed water elevation. However, an overestimation of the computed water elevation is observed in the low tidal situations.

428 **5.4.2** *Flow velocity*

Fig. 9 illustrates the comparisons of the simulation results for the flow velocity and the measurement data in a long-term simulation period from 2009-02-20 to 2009-06-10 at Samarinda station. The model reproduces reasonably well the observed flow velocity in different neap-spring tidal cycles during the long-term simulation. The RMS error of flow velocity is 0.087 m/s, i.e. about 13% of the average value of the measured velocity while MAE of velocity is 0.07 m/s (Table 4). The *r* coefficient is 0.95 and the NSE coefficient is 0.89 (Table 4). These results show that the model successfully reproduces the flow velocity in the Mahakam River.

Fig. 10 shows the comparisons between computed and observed flow velocity at DAN, DAS, 436 FBN, and FBS stations. The observed flow velocity in different spring and neap tides in the period 437 from 2008-12-26 to 2009-01-05 are represented reasonably well by the model in general. As shown 438 in Table 4, the RMS errors of flow velocity at DAN and DAS are 0.053 and 0.081 m/s, respectively. 439 At FBN and FBS stations, these errors are 0.104 and 0.09 m/s (<20% of the average value of the 440 measured velocity). A value of 0.042 and 0.063 m/s is obtained for the MAE at DAN and DAS, 441 respectively, while the MAE respectively equals to 0.095 and 0.065 m/s at FBN and FBS. The NSE 442 coefficient at all four stations is greater than 0.76 while the r coefficient is higher than 0.85. 443

At the low flow velocity situations (see Fig. 10), an overestimation of the calculated flow

velocity in the spring tides is obtained while an underestimation of the calculated velocity in the neap tides is achieved at DAS, FBN, and FBS stations. The difficulty in obtaining good reproduction of flow velocity at these stations is due to the complex flow around the bifurcations, which is highly variable, and probably also to the constant Manning coefficient in our simulations that does not represent well all the head-loss processes occurring around bifurcations.

450 **5.4.3** *Water discharge*

The predicted and observed water discharges in a long-term simulation period from 2009-02-20 to 2009-06-10 at Samarinda station are shown in Fig. 11. The model reproduces reasonably well the observed water discharge in different neap-spring tidal cycles during the long-term simulation. The RMS error for the water discharge is 530 m³/s (about 11% of the average value of the measured water discharge) while the value of MAE of water discharge is 420 m³/s (Table 5). In addition, as for the flow velocity, the *r* coefficient is 0.95 and the NSE coefficient is 0.86 for water discharge. These results confirm again that the model successfully reproduces the flow in the Mahakam River.

The comparisons between computed and observed water discharges at four stations, namely 458 DAN, DAS, FBN, and FBS are shown in Fig. 12. The results show that the simulations generally 459 agree well with the observed water discharges measured in different spring and neap tides in the 460 period from 2008-12-26 to 2009-01-05. The RMS errors of water discharge at DAN and DAS 461 (Table 5) are 340 and 760 m³/s, respectively and are equal to about 8% and 12% of the observed 462 magnitude of water discharges at these stations. At FBN and FBS stations (Table 5), these errors are 463 17% (410 m³/s) and 13% (720 m³/s) of the measured water discharge. A value of 270 and 610 m³/s 464 is obtained for the MAE at DAN and DAS, respectively, while the MAE respectively equals to 370 465 and 540 m³/s at FBN and FBS. The NSE coefficient at these stations is more or less 0.80 while the r 466 coefficient is about 0.85 (Table 5). 467

Water discharges vary significantly in the northern and southern channel sections, depending on the tidal conditions. Due to wider channel sections in the southern channels, a larger amount of water discharges into the southern channels (DAS and FBS) in comparison with the northern

channels (DAN and FBN). As shown in Fig. 12b and Fig. 12d for the channel sections in the 471 southern channels, the model predicts very well the observations at large discharges. At low 472 discharges (corresponding to high water situations), the model overestimates the water discharge 473 observations at the high water of spring tide on 2008-12-26 at DAS and on 2008-12-27 at FBS. The 474 computed water discharge underestimates the observations at the high water of neap tide on 475 2009-01-04 at DAS and on 2009-01-03 at FBS. These discrepancies may be due to the use of a 476 constant value of the Manning coefficient and the inability of the model to take into account lateral 477 secondary circulation flows caused by local channel curvature. A vertical wall is assumed at 478 impermeable coastlines. This assumption may result in inaccuracy of the wetted channel section 479 area corresponding to high waters in calculations and, hence, can be another reason for the 480 discrepancies in the water discharge. 481

482 **6 Discussion**

6.1 Water division at bifurcations in the delta

The delta presents many bifurcations (Fig. 1) that can affect the division of water discharge in the 484 downstream channels. Fig. 13 shows the variation in water discharge division over the downstream 485 channels of the delta apex (DAN and DAS) and first (FBN and FBS) bifurcations at different tidal 486 conditions, e.g. neap or spring tide. The model represents very well the observed division of water 487 discharge at both bifurcations, with an improvement compared to the numerical simulations 488 reported by Sassi et al. [27], in which (i) the water discharge division over the downstream channels 489 is only biased towards the northern channels, (ii) the simulated water discharge division at delta 490 apex bifurcation during spring tide is too asymmetrical, and (iii) the simulations of the water 491 discharge division lead to values smaller than those measured in situ. This improvement may be due 492 to the use, in the present study, of different values of the Manning coefficient in the upstream region 493 of the delta and in the delta itselt. 494

Fig. 14 shows the specific water discharge (q = Q / b) at different cross-sections in the northern and southern channels downstream of the delta apex and first bifurcations in the delta (Fig. 4b). Both computed results and observations show that the specific water discharge is directed towards the northern channel at the delta apex bifurcation (Fig. 14a). This trend in specific water discharge division may result from the differences in local flow, e.g. tidal motion in northern and southern branch channels.

Results for the first bifurcation (FBN and FBS) are shown in Fig. 14b. For low discharges, a 501 similar trend as in Fig. 14a is observed, i.e. the specific water discharge is directed towards the 502 northern channel. However, for high discharges (corresponding to low tides), the specific water 503 discharge is generally directed towards the southern channel (FBS), presenting an opposite trend in 504 comparison with the delta apex bifurcation. There is a local depositional area (sand bar) in the 505 middle channel downstream of DAS (Fig. 4b) that extends over few kilometers before the first 506 bifurcation. Due to this sand bar, the water flow is divided into two parts, with the dominant water 507 directed towards the northern channel (FBN). This is the reason why the specific water discharge is 508 directed towards the northern branch at low discharges. At high flow discharges, an opposite trend 509 of specific water discharge is obtained. Indeed, the effects of the sand bar become negligible, as for 510 higher water levels the channel in the southern branch is much deeper and wider than the northern 511 branch. 512

513 6.2 Effects of the lakes

In order to investigate the influence of the three largest lakes, one simulation including these lakes 514 and one simulation excluding these lakes are performed for a low flow period from June to 515 November 2009. The optimal values of the Manning coefficient in Section 5 are used in both 516 simulations. The computational grid shown in Fig. 4 is also used, with the particular grid of the 517 three lakes being removed for the later simulation. Fig. 15 shows the computed water elevation 518 from these simulations at three stations, namely Pela Mahakam, Muara Karman, and Samarinda 519 (see Fig. 1). The discrepancy in the water elevation with and without including the lakes is about 35 520 cm (i.e. 28% of the water elevation magnitude that is obtained in the case without the lakes) at Pela 521 Mahakam, 25 cm (i.e. 18% of the water elevation magnitude) at Muara Karman, and 10 cm (i.e. 6% 522

of the water elevation magnitude) at Samarinda station, revealing that the influence of the lakes on the water elevation in the Mahakam River decreases in the downstream direction as expected. At Delta Apex, Delta North, and Delta South stations, this difference (not shown) is less than 5 cm. These results suggest that the effect of the lakes is not negligible and, hence, is worth investigating in detail. This will be done in the next stage of the research.

The computed water discharges at Pela Mahakam, Muara Karman, and Samarinda when 528 including and excluding the lakes into the computational domain are shown in Fig. 16. If the three 529 lakes are added in the computational domain, the magnitude of water discharge will be increased by 530 340 m^3 /s (i.e. 11% of the mean annual river discharge of the Mahakam River), 400 m^3 /s (i.e. 13% of 531 the mean annual river discharge of the Mahakam River), and 500 m^3/s (i.e. 17% of the mean annual 532 river discharge of the Mahakam River) at the Pela Mahakam, Muara Karman, and Samarinda 533 station, respectively, for situations of water flowing in seaward direction. Conversely, when water 534 flows in the direction from the sea to the river corresponding to the negative water discharge in Fig. 535 16, a water discharge of about 800 m³/s (i.e. 27% of the mean annual river discharge of the 536 Mahakam River) will flow in these three lakes, as shown in Fig. 16a. These results suggest that the 537 model is able to reproduce the interconnection between the lakes and the river. 538

6.3 Effects of the computational grid

To investigate the effects of grid resolution on the computed results, a simulation on a coarser grid 540 (denoted by mesh A) and a simulation on a finer grid (denoted by mesh C) are also performed. The 541 total numbers of triangular elements in the 2D sub-domain is 49,175 for mesh A and 80,222 for 542 mesh C and both meshes have 3,700 line segments in the 1D sub-domain. The procedure for 543 generating mesh A and mesh C is exactly the same as those using for creating the computational 544 grid shown in Fig. 4 (denoted by mesh B). The boundary conditions and the optimal values of the 545 Manning coefficient (n = 0.0275 s/m^{1/3} in the river and tributaries, n = 0.0305 s/m^{1/3} in the three 546 lakes, n = 0.023 s/m^{1/3} in the Makassar Strait, and n = 0.023-0.0275 s/m^{1/3} in the delta) presented in 547 the previous section are used in both additional simulations. The statistical evaluation of the 548

different type of errors when using mesh A and mesh C is summarized in Table 6 while, again, these errors when using mesh B are listed in Table 2. It can be observed that slight differences are observed when using different meshes, but the overall statistical evaluation of the different type of errors at all five water elevation stations appears to be similar when using different meshes. This is because the resolution of each computational grid is still defined by physical processes, i.e. the local mesh size is defined to be proportional to the square root of the bathymetry and the refinement of each grid also still depends on the distance to the delta apex and coastlines.

6.4 Reasons for the discrepancies and future work

A constant value of the bottom friction was assumed for the tributaries and along the Mahakam 557 River, in order to render the calibration as simple as possible. The use of such constant values may 558 not be suitable when considering the roughness coefficient of the tributaries and the river in reality. 559 In addition, the effects of secondary flows can be significant in the meandering channels of the delta 560 as well as in the Mahakam River itself [36]. These secondary flows are not taken into account in the 561 calculations, which could explain some of the differences between simulations and observations at 562 some stations. Moreover, the uncertainty in the determination of the water discharge at the upstream 563 boundaries of the tributaries in the model, caused by using a rainfall-runoff model, can be another 564 reason for the observed discrepancy. Furthermore, the absence of baroclinic effects, which cannot 565 be taken into account in the present depth- and section-averaged model, may be an additional reason 566 for the discrepancy between observations and simulations. Finally, regarding the comparisons 567 between computed and observed flow velocity as well as water discharges at four channel sections 568 located downstream of the delta apex and first bifurcations, the difference between them can be 569 explained by several factors, e.g. a bend upstream of bifurcations, the width-depth ratio of the 570 upstream channel, local bank irregularities, differences of roughness [37]. 571

In each flow region such as Mahakam River and tributaries or lakes, variation of the Manning coefficient corresponding to the change of the local water depth was not considered in this study. Previous studies [38,39] suggested that the Manning coefficient can be changed with the variation of the water depth. Regarding the Mahakam River, the water depth can vary considerably, depending on the location. Further investigation of the Manning coefficient as a function of the local water depth will be considered in the future modelling effort for exploring the spatial variation of the Manning coefficient in each region of the studied system.

Previous study [12] on flooding in the middle Mahakam River catchment shows that bank 579 overtopping can occur during a flood situation in floodplain regions located around the Melintang 580 Lake. During flood periods, these regions are flooded and water flows through these regions to the 581 lake. In the connecting channels between the lakes and the Mahakam River, flow overtopping can 582 also happen in flood situations. Due to the effects of flow overtopping, the channel banks can be 583 eroded, resulting in an increase of the channel width. However, in the framework of the present 584 numerical model, the increase of channel width caused by flow overtopping has not been 585 considered yet and a vertical wall is assumed to be used in such situations, preventing the 586 inundation of the floodplain. Treatments of overtopping flow and simulations in a long-term period 587 of several years are foreseen in the future to further quantify the balance of water inputs to and 588 outputs from the lakes. 589

590 7 Summary and conclusion

The Mahakam river-lake-delta system presents a continuous riverine and marine environment 591 including various interconnected regions, i.e. a river and its tributaries, lakes, a delta, and the 592 adjacent coastal ocean, with complicated processes of the flow. In this study, the unstructured-mesh, 593 finite element model SLIM was applied to this river-lake-delta system, using a coupled 1D / 2D 594 version of the model, (i) to allow for reproducing the flow from the upstream to the open sea and (ii) 595 to have better understanding of the flow processes occurring at different temporal and spatial scales 596 in the system. The complex geometry, especially in the deltaic region, was represented in detail in 597 the computational domain in order to take into account several physical processes in the 598 calculations. 599

600

The appropriate values of the Manning coefficient in each part of the system, i.e. Mahakam

River and tributaries, lakes, delta, and Makassar Strait were calibrated. The model was then 601 validated to confirm the appropriate values of the Manning coefficient. A good agreement was 602 achieved between the computed results and observations for the water elevation at six stations, and 603 for the velocity and water discharge at the other five stations. The RMS error and MAE were only 604 about 10 cm at all water elevation stations while the maximum value of these errors for water 605 discharge was of the order of 12% of the observed values. The RMS error and MAE of velocity 606 were smaller than 20% of the observed velocity. The NSE coefficient was 0.95 at six water 607 elevation stations and its value was about 0.80 at the stations of velocity and water discharge. The 608 Pearson's correlation coefficient between computed results and field data was very close to unity at 609 all stations. The coupled 1D / 2D model of the unstructured-mesh, finite element model SLIM 610 successfully reproduced the observations of the flow in the Mahakam river-lake-delta system. 611

Using the computations, firstly, in terms of division of water at the bifurcations, the model 612 reproduced reasonably well the observations at the delta apex and at the first bifurcations in the 613 delta. Secondly, the effects of three lakes on the flow in the lower part of the Mahakam River were 614 also quantified, showing that these lakes contribute about 20% of the mean annual river discharge 615 of the Mahakam River in the considered low flow period. Thirdly, the region of the lakes, which is 616 located about 150 km upstream of the Mahakam Delta, was found as the limit of the tidal 617 propagation in the Mahakam river-lake-delta system. Finally, the grid resolution was preliminarily 618 explored, revealing that the overall evaluation of the errors at five water elevation stations appears 619 to be similar when using three different meshes, because the resolution of each mesh is still defined 620 by the same physical processes. 621

The results obtained in the present study are believed to be useful for studying transport processes of various constituents (e.g. sediment, salinity) in the system as well as water renewal timescales in the deltaic regions in the future. In addition, the coupled 1D / 2D model of the unstructured-mesh, finite element model SLIM uses a computational grid that allows for an accurate representation of complex topographies and an increase in spatial resolution in areas of interest, which makes the model to be very suitable and computationally efficient for simulating the flow in other river-lake-delta systems like the one associated with the Mahakam River. Fine mesh can be used in the domain of interest instead of in the whole computational domain, and thus, this can reduce the computational time due to a decrease of the number of elements. Moreover, different spatial scales of the flow processes from the river to the coastal ocean and deep margin can be also simulated.

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Tables

| uc | Manning coefficient | | | RMS error of water elevation (cm) | | | | |
|-----------|---------------------|--------------------------|---------------------------------|-----------------------------------|-----------------|----------------|----------------|---------------|
| Simulatio | lakes | river and tributaries | delta and Makassar Strait | JWL | Pela Mahakam | Delta North | Delta South | Delta Apex |
| a.01 | | | 0.019 | 28.1 | 20.5 | 8.4 | 7.6 | 14.6 |
| a.02 | | 0.0175 | 0.023 | 27.3 | 19.3 | 8.3 | 7.4 | 15.1 |
| a.03 | | | 0.035 | 24.8 | 16.2 | 8.8 | 8.1 | 23.6 |
| a.04 | | | 0.019 | 13.5 | 6.0 | 8.4 | 7.6 | 15.2 |
| a.05 | 0.023 | 0.0275 | 0.023 | 13.2 | 5.7 | 8.3 | 7.4 | 13.9 |
| a.06 | | | 0.035 | 12.6 | 5.3 | 8.8 | 8.1 | 21.5 |
| a.07 | | | 0.019 | 14.1 | 8.5 | 8.4 | 7.6 | 16.2 |
| a.08 | | 0.0325 | 0.023 | 14.2 | 8.9 | 8.3 | 7.4 | 13.9 |
| a.09 | | | 0.035 | 14.8 | 10.2 | 8.8 | 8.1 | 20.3 |
| a.10 | | | 0.019 | 28.1 | 20.6 | 8.4 | 7.6 | 14.6 |
| a.11 | | 0.0175 | 0.023 | 27.2 | 19.4 | 8.3 | 7.4 | 15.1 |
| a.12 | | | 0.035 | 24.7 | 16.3 | 8.8 | 8.1 | 23.6 |
| a.13 | | | 0.019 | 13.5 | 6.0 | 8.4 | 7.6 | 15.2 |
| a.14 | 0.0305 | 0.0275 | 0.023 | 13.2 | 5.7 | 8.3 | 7.4 | 12.8 |
| a.15 | | | 0.035 | 13.7 | 5.9 | 9.2 | 8.3 | 21.4 |
| a.16 | | | 0.019 | 14.1 | 8.5 | 8.4 | 7.6 | 16.2 |
| a.17 | | 0.0325 | 0.023 | 14.3 | 8.9 | 8.3 | 7.4 | 13.9 |
| a.18 | | | 0.035 | 14.8 | 10.1 | 8.8 | 8.1 | 20.3 |
| a.19 | | | 0.019 | 27.9 | 20.9 | 8.5 | 7.7 | 14.7 |
| a.20 | | 0.0175 | 0.023 | 27.1 | 19.7 | 8.3 | 7.4 | 15.2 |
| a.21 | | | 0.035 | 24.6 | 16.4 | 8.8 | 8.1 | 23.6 |
| a.22 | | | 0.019 | 13.5 | 6.1 | 8.4 | 7.6 | 15.2 |
| a.23 | 0.045 | 0.0275 | 0.023 | 13.3 | 5.8 | 8.3 | 7.4 | 12.9 |
| a.24 | | | 0.035 | 12.7 | 5.4 | 8.8 | 8.1 | 21.5 |
| a.25 | | | 0.019 | 14.2 | 8.5 | 8.4 | 7.6 | 16.2 |
| a.26 | | 0.0325 | 0.023 | 14.4 | 8.8 | 8.3 | 7.4 | 13.9 |
| a.27 | | | 0.035 | 15.0 | 10.1 | 8.8 | 8.1 | 20.3 |

Table 1 RMS error of water elevation at five measurement stations for the calibration phase

| Station | Water elevation | | | | | | |
|--------------|-----------------|----------|------|------|--|--|--|
| Station | RMS error (cm) | MAE (cm) | NSE | r | | | |
| JWL | 13.1 | 10.4 | 0.93 | 0.96 | | | |
| Pela Mahakam | 5.6 | 4.6 | 0.96 | 0.98 | | | |
| Delta North | 8.3 | 6.7 | 0.98 | 0.99 | | | |
| Delta South | 7.4 | 6.0 | 0.98 | 0.99 | | | |
| Delta Apex | 10.2 | 8.0 | 0.93 | 0.97 | | | |

Table 2 RMS error, MAE, NSE, and r at water elevation stations for the calibration phase

Table 3 RMS error, MAE, NSE, and r at water elevation stations for the validation phase

| | Water elevation | | | | | | |
|--------------|-------------------|----------|------|------|--|--|--|
| Station | RMS error (cm) | MAE (cm) | NSE | r | | | |
| Pela Mahakam | 3.9 | 3.3 | 0.97 | 0.98 | | | |
| Muara Karman | 10 | 7.1 | 0.89 | 0.95 | | | |
| Delta North | 10.9 | 8.8 | 0.96 | 0.98 | | | |
| Delta South | 10.4 | 8.4 | 0.96 | 0.98 | | | |
| Delta Apex | 11.7 | 9.3 | 0.92 | 0.96 | | | |

Table 4 RMS error, MAE, NSE, and r at flow velocity stations for the validation phase

| Station | Flow velocity | | | | | | |
|-----------|-----------------|-----------|------|------|--|--|--|
| Station | RMS error (m/s) | MAE (m/s) | NSE | r | | | |
| Samarinda | 0.087 | 0.069 | 0.89 | 0.95 | | | |
| DAN | 0.053 | 0.042 | 0.88 | 0.94 | | | |
| DAS | 0.081 | 0.063 | 0.79 | 0.85 | | | |
| FBN | 0.104 | 0.095 | 0.76 | 0.90 | | | |
| FBS | 0.090 | 0.065 | 0.77 | 0.88 | | | |

| | Station | Water discharge | | | | | |
|--|-----------|---------------------|---------------|------|------|--|--|
| | Station | RMS error (m^3/s) | MAE (m^3/s) | NSE | r | | |
| | Samarinda | 530 | 420 | 0.86 | 0.95 | | |
| | DAN | 340 | 270 | 0.85 | 0.92 | | |
| | DAS | 760 | 610 | 0.71 | 0.83 | | |
| | FBN | 410 | 370 | 0.75 | 0.87 | | |
| | FBS | 720 | 540 | 0.79 | 0.89 | | |

Table 5 RMS error, MAE, NSE, and r at water discharge stations for the validation phase

Table 6 Statistical evaluation of the different type of errors at water elevation stations when using different meshes

| Mesh | Mesh A | | | Mesh C | | | | |
|--------------|--------------|------|------|--------|--------------|------|------|------|
| Station | RMS error | MAE | NSE | r | RMS error | MAE | NSE | r |
| JWL | 13.2 | 10.7 | 0.93 | 0.97 | 12.7 | 10.5 | 0.93 | 0.97 |
| Pela Mahakam | 5.6 | 4.7 | 0.96 | 0.98 | 5.6 | 4.7 | 0.96 | 0.98 |
| Delta North | 8.2 | 6.7 | 0.98 | 0.99 | 8.0 | 6.6 | 0.98 | 0.99 |
| Delta South | 7.4 | 6.0 | 0.98 | 0.99 | 7.3 | 5.8 | 0.98 | 0.99 |
| Delta Apex | 10.3 | 8.3 | 0.93 | 0.97 | 9.8 | 8.0 | 0.93 | 0.97 |

Figures



Fig. 1 Map of the tropical Mahakam river-lake-delta system, Indonesia: *blue dots* indicate the water elevation stations while *red square* denotes the flow velocity and water discharge station.



Fig. 2: Schematic diagram of line segments and nodes at a confluence point, where the space coordinate x increases in the flow direction.



Fig. 3: Bathymetry in the Mahakam Delta.



Fig. 4 Computational grid of the Mahakam river-lake-delta system: (a) mesh of the whole computational domain, with 60,819 triangles and 3,700 line segments and (b) zoom on the delta and upstream part of the computational domain: *blue dash-lines* indicate the interfaces between the 1D and 2D grids, *black dots* denote upstream boundaries locations, and *red squares* represent the flow velocity and water discharge stations.



Fig. 5 Observed and computed water elevation at: (a) JWL and (b) Pela Mahakam stations (Fig. 1) during the calibration period.



Fig. 6 Observed and computed water elevation at: (a) Delta North, (b) Delta South, and (c) Delta Apex stations (Fig. 1) during the calibration period.



Fig. 7 Observed and computed water elevation at: (a) Pela Mahakam and (b) Muara Karman stations (Fig. 1) during the validation period.



Fig. 8 Observed and computed water elevation at: (a) Delta North, (b) Delta South, and (c) Delta Apex stations (Fig. 1) during the validation period.



Fig. 9 Observed data and computed results of flow velocity at Samarinda station, where positive velocity coincides with seaward direction.



Fig. 10 Computed and measured flow velocity at: (a) DAN, (b) DAS, (c) FBN, and (d) FBS stations (Fig. 4) during the validation period. In each panel, observations in the left site were performed in spring tides while observations in the right site were performed in neap tides.



Fig. 11 Observed data and computed results of water discharge at Samarinda station, where positive water discharge coincides with seaward direction.



Fig. 12 Computed and measured water discharges at: (a) DAN, (b) DAS, (c) FBN, and (d) FBS stations (Fig. 4) during the validation period. In each panel, observations in the left hand site were performed in spring tides while observations in the right hand site were performed in neap tides.



Fig. 13 Discharge difference between southern and northern channels obtained with the simulations and with observations. Each dot is calculated from the water discharge in the northern channel section (denoted by Q_{North}) and the water discharge in the southern channel section (denoted by Q_{South}). The quantity ($Q_{south} - Q_{north}$) in the vertical axis of the figure is calculated from the observation data while the one in the horizontal axis is computed from the numerical simulations.



Fig. 14 Specific water discharge in the northern and southern channels at: (a) delta apex and (b) first bifurcations in the delta.



Fig. 15 Water elevation at: (a) Pela Mahakam, (b) Muara Karman, and (c) Samarinda, in the cases with and without the lakes.



Fig. 16 Water discharge at: (a) Pela Mahakam, (b) Muara Karman, and (c) Samarinda, in the cases with and without the lakes. The positive water discharge coincides with the seaward direction.