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# Numerical simulation of impact noise generated at the railway insulated joint

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## Abstract

This paper presents a full finite element (FE) model of wheel-track interaction to study the wheel-rail impact noise excited by an insulated joint (IJ). The integration is performed in the time domain with an explicit central difference scheme. The vibratory behaviour of the track and wheel model are respectively validated with hammer test and Axle Box Acceleration (ABA) measurement. By making use of the calculated velocities and pressures on the vibrating surfaces, the boundary element method (BEM) based on Helmholtz equation is adopted to transform the vibrations of the wheel-track into acoustic signals. The decay rate of impact noise at different frequency bands during propagation are analysed. The predictions of total impact noise radiation and the noise contributions of different track components are in good agreement with results reported in the literature, while the effective frequency range is successfully extended from 5 kHz to 10 kHz.

## 1 Introduction

Due to the significant geometric and material discontinuity, IJ is considered as one of the weakest part of the track structure and an important excitation source of impact noise. When a train runs over an IJ, wheel-rail impact inevitably happens and consequently the ‘clickety-clack’ impact noise is generated and emitted.

An early comprehensive study on impact noise was published by V er et al. in 1976 [1], before which the studies focused on test and were largely qualitative. V er et al. established an analytical model and defined geometric and dynamic variables which make contributions to impact noise generation by analysing the noise initiated at different types of discontinuities such as rail joints, frogs, switches, and wheel flats. Because of the limited modelling approaches and computing resources at that time, the analytical model was simple and failed to calculate the time history of impact force, let alone the spectral distribution of impact noise. In reviewing the prior work, Remington [2] introduced the models and method of Newton and Clark for contact force calculation [3] into analysis of impact noise to tackle non-linear contact problem, pointing out a new direction for impact noise study. In addition, the geometric discontinuities of the rail and wheel surfaces were replaced with an average roughness spectrum in frequency domain as the excitation inputs for the calculation of impact vibration and noise. Wu and Thompson in [4] employed a time-domain analytical contact model to calculate the impact force between wheel and rail under non-linear contact conditions, and then, employing a linear approximation method, converted the impact force into force spectrum in frequency domain and further into an equivalent roughness spectrum also in frequency domain. On the basis of TWINS [5], the processed roughness spectrum was directly applied as inputs and the impact noise results could be obtained. This hybrid method managed to solve the problem of non-linearity, but due to the simplification of the contact model, the analysing frequency was limited to 5 kHz. A study by Pieringer et al. also showed that without consideration of the changes in contact stiffness due to the realistic geometry at the discontinuities, simplified analytical model failed to reach a sufficiently accurate prediction [6]. On the basis of Wu’s hybrid method, a more complicated numerical finite element (FE) track model was developed in [7] to predict the impact noise track system and excited

by wheel flat, but the simplification of the wheel as a rigid mass still caused deviations especially at high frequency.

Instead of using simplified analytical models of wheel and track, and the assumption of Hertzian or non-Hertzian spring contact, Yang et al. presented a transient finite element wheel-track interaction model to predict the impact noise generated by squat [8]. The wheel, the rail and the sleepers are modelled with finite elements in three dimensions, where necessary and appropriate. Realistic contact geometry, including 3D geometric irregularities in the contact surfaces is considered. The integration is performed in the time domain with an explicit central difference scheme. By making use of the calculated velocities and pressures of the vibrating surfaces, the boundary element method (BEM) based on Helmholtz equation is adopted to transfer the vibration of the railway system into acoustic signal, extending the prediction range of frequency of impact noise to 10 kHz.

By applying an approach similar to that of [8], a wheel-rail impact at an insulated joint (IJ) is modelled in this paper. Compared with the squat excitation model, the structural and geometric discontinuity of the IJ makes the track model developed in this paper more complex. In addition, the IJ excitation model optimised the boundary conditions and mesh schemes of wheel and rail. The inertance frequency response function of the track model and the dynamic vibrating response of the wheel model are respectively validated by hammer test and Axle Box Acceleration (ABA) measurement. The impact noise emission and the contributions of different track components to the total noise are analysed in the end.

## 2 FE model

### 2.1 The numerical model

A typical IJ of Dutch railway is selected in the track from Eindhoven to Weert as the modelling objective. The in-situ condition of the IJ and the corresponding time-domain FE wheel-rail interaction model are respectively shown in Fig. 1 and Fig. 2. To reduce the model size, a half-side track and a half wheel set with sprung mass of the car body and the bogie are considered. Since the value of elastic modulus of the insulation layer is much lower than that of the rail, the insulation layer between the two rail ends can be omitted in the model and simplified as a gap. The IJ including fishplates, 4 pairs of bolts and a 6 mm realistic geometrical gap is modelled in the middle of the 10 meter half-side track model. 9 sleeper spans extend from IJ to each end of the track. According to the in-situ condition, the rail is UIC54 with an inclination of 1:40. Non-reflective boundary conditions are applied at rail ends to prevent artificial stress wave reflections generated at the model boundaries. The wheel geometry corresponds to that of a passenger car of the Dutch railway with a radius of 0.46 meter. The symmetric boundary condition is applied at the inner side of wheel axle and the outer end of the axle is free. The wheel, the rail, the fishplates of the IJ and the sleepers are modelled with 8-node solid elements. In order to achieve a high accuracy of the solution with a reasonable model size, non-uniform meshing scheme is used. The mesh size around the initial position of the wheel-rail contact and the insulated joint area is 1 mm. The lumped mass of the car body and bogie are modelled as 8 mass elements, connected to the wheelset by the primary suspension of the vehicle with parallel linear springs and viscous dampers. The two neighbouring timber sleepers beneath the IJ with baseplate fastening system and the concrete sleepers elsewhere with Vossloh fastening system (Fig. 1) are differentiated by material models and spring/damper parameters. Bolts are simplified as 4 pairs of oppositely-oriented force loads, pressing the fishplates on the web of rails. Since the substructure has little influence on the high-frequency dynamic impact studied in this paper, each sleeper only contains 12 solid elements and the ballast is simplified as vertical spring and damper elements with the displacements constrained in lateral and longitudinal directions. The parameters used in the model are listed in table 1. Most of them were taken from [9].



Figure 1: Modelling objective

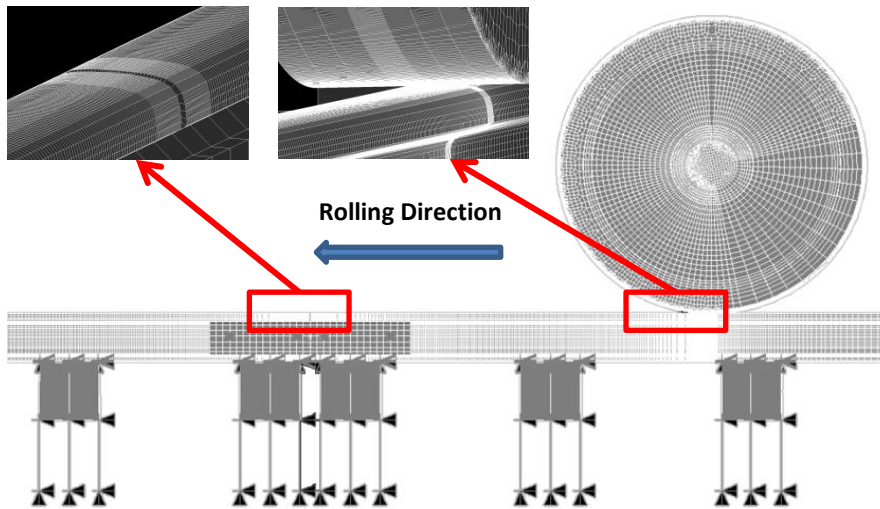


Figure 2: FE Wheel-IJ Interaction Model

parameters		values	parameters		values
Wheel diameter		0.92 m	Wheel, rail material	Young's modulus	210 GPa
Sprung mass		8000 kg		Poisson's ratio	0.3
Sleeper distance		0.6 m		Density	7800 kg/m <sup>3</sup>
Primary suspension	Stiffness	1.15 MN/m		Yield stress	0.5 GPa
	Damping	2500 Ns/m		Tangent modulus	21 GPa
Baseplate fastening	Stiffness	1944 MN/m	Timber sleeper material	Young's modulus	20 GPa
	Damping	67440 Ns/m		Poisson's ratio	0.3
Vossloh fastening	Stiffness	1300 MN/m		Density	1300 kg/m <sup>3</sup>
	Damping	45000 Ns/m	Concrete sleeper material	Young's modulus	38.4 GPa
Ballast	Stiffness	45 MN/m		Poisson's ratio	0.2
	Damping	32000 Ns/m		Density	2520 kg/m <sup>3</sup>

Table 1: The values of parameters in the model

To apply the real geometry to the surface of the rails at the IJ for the impact simulation, the longitudinal-vertical rail profile at the IJ was measured with RAILPROF [10]. Since the RAILPROF measures the longitudinal-vertical rail profile along the centre line of the rail, while the maximum deviation of the vertical irregularity probably occurs off the centre line as shown in Fig. 3, modification is made for a more realistic shape of IJ in the model. Fig. 4 shows the surfaces of the IJ model before and after applying the measured profile.

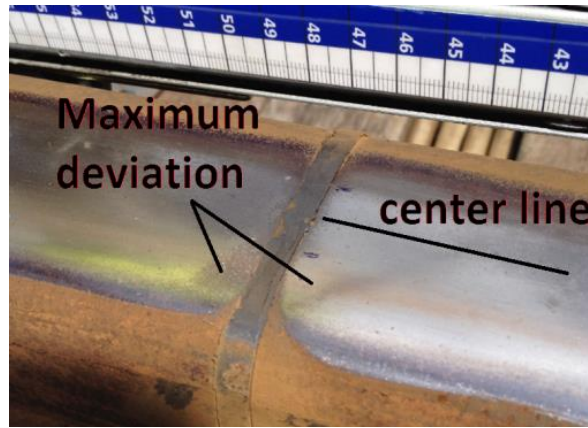


Figure 3: Irregularity at rail surfaces around IJ

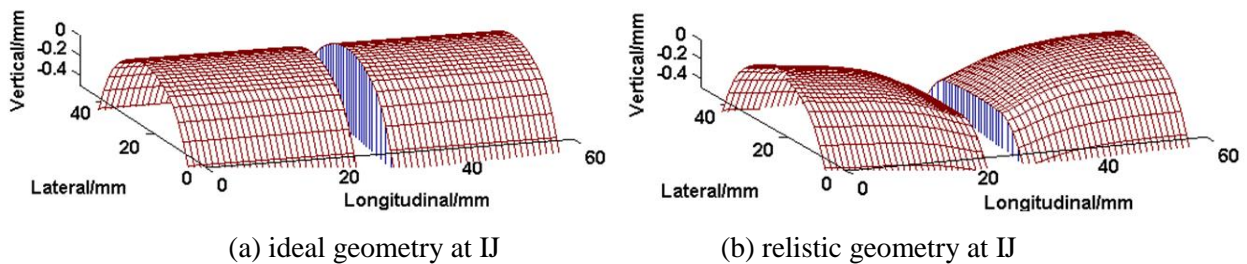


Figure 4: Applying the realistic geometry to IJ (size of irregularity exaggerated)

The integration is performed in the time domain with an explicit central difference scheme. Very small time step ( $4.9e-8$  s) is employed for the model to meet Courant stability condition [11]. This effectively guarantees that high frequency dynamic effect up to 10 kHz is reproduced. In the transient dynamic simulation, a dynamic relaxation is first employed to make the wheel-track system reach an equilibrium state under gravity. The initial position of wheel model is at 1.2 m (2 sleeper spans) away from the IJ (as shown in Fig. 2). The movements of the wheel in both rotation and forward translation are applied as the initial conditions. The wheel is subsequently set to roll along the rail from the initial position toward the IJ. The effects of transient wheel rotation can be included inherently.

## 2.2 Model validation

Due to limitation on track access, the in-situ measurement of rail vibration and noise radiation have not yet been performed. The properties of the track model and the dynamic response of the wheel model are respectively validated with hammer test and Axle Box Acceleration (ABA) measurement.

### 2.2.1 Validation of track Inertance

The vibratory behaviour of the track model is validated with an in-situ hammer test. The hammer test was performed at the selected IJ to obtain the experimental inertance of the track. A Brüel & Kjær 8206

hammer with a hard metal tip was used to generate a narrow band pulse. The input force spectrum determines that the maximum valid frequency of the measured signals cannot be over 5 kHz. The locations of the pulse load and the measurement of the rail vertical acceleration are at the rail head above the sleeper just after the IJ.

Receptance of the track model was calculated by employing a harmonic analysis. The wheel was removed from the model during the harmonic analysis. Under the harmonic excitation forces with constant amplitude but varying frequencies from 10 Hz to 5 kHz at a step of 10Hz, the nodal displacements of the FE track model can be obtained. Since the experimental response was obtained in terms of acceleration, equation (1) is adopted to convert the calculated track receptance into simulation inertance for comparison.

$$H_{af}(f) = (2\pi f)^2 * H_{xf}(f) \quad (1)$$

Where  $H_{af}(f)$  and  $H_{xf}(f)$  are respectively inertance and receptance frequency response functions of the track structure with the argument of frequency  $f$ . After the conversion, the calculated inertance of the track is compared in Fig. 5 with the experimental inertance from the hammer test. It can be seen that, in the frequency range higher than 500 Hz, the tendency and resonant behaviour of numerical inertance are basically in accordance with the experimental inertance; while below 500 Hz, some sleeper-related low frequency modes cannot be reproduced by the model, which could result from the simplification of sleeper and ballast model. Since the main research objective of this paper is the high frequency impact noise, whose dominant frequency range is over 1 kHz, this deviation at the lower end of the frequency range can be tolerated for the dynamic and acoustic calculation.

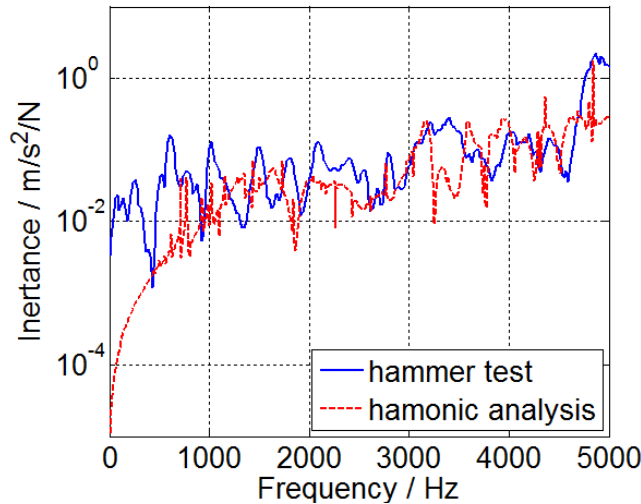


Figure 5: Comparison of inertance of track at IJ

### 2.2.2 Axle Box Acceleration (ABA)

The calculated vibration acceleration of the wheel are validated by measured axle box accelerations (ABA) [12]. ABA measurements were carried out twice at the selected IJ in September 2011 and march 2014, respectively. The rail was ground just before the second measurement. During the two measurements, the traveling speed of measuring train was kept around 100km/h when passing over the IJ area, the same with the wheel rolling speed applied in the transient analysis. The vertical vibrations of both leading and trailing axles were measured each time.

In order to see the tendencies and differences of the simulated and measured vibration results clearly, their 2 kHz low-pass filtered time history signals are plotted in Fig. 6 (a). As shown in the figure, the simulation result has a good agreement with the measured results in the time domain. The positions of the peaks and dips, as well as the attenuation trends of simulated and measured signals show basically the same pace with each other. The differences can be attributed to the differences between the parameters used for the



model and the actual values in the track. In the frequency domain, the comparison of one third octave band spectra in Fig. 6 (b) indicates that the calculated wheel acceleration is largely in agreement with the measured results in the whole analysed frequency range. Specifically, the simulation signal in the low frequency range is closer to the results from measurement 2. It is found that although the three peaks at centre frequency bands of 1250 Hz, 2500 Hz and 4000Hz also exist in the vibration signals of measurement 2, their values are significantly reduced compared with the results of measurement 1 and the simulation signal. This is probably because the short wave irregularities of track which can excite high frequency wheel vibration was decreased by grinding. Another explanation can be that the high frequency vibration contents in this range were damped to certain extent by the bearings between wheel and axle, while the lower frequency components could be conserved during the vibrating energy transfer from wheel to axle box.

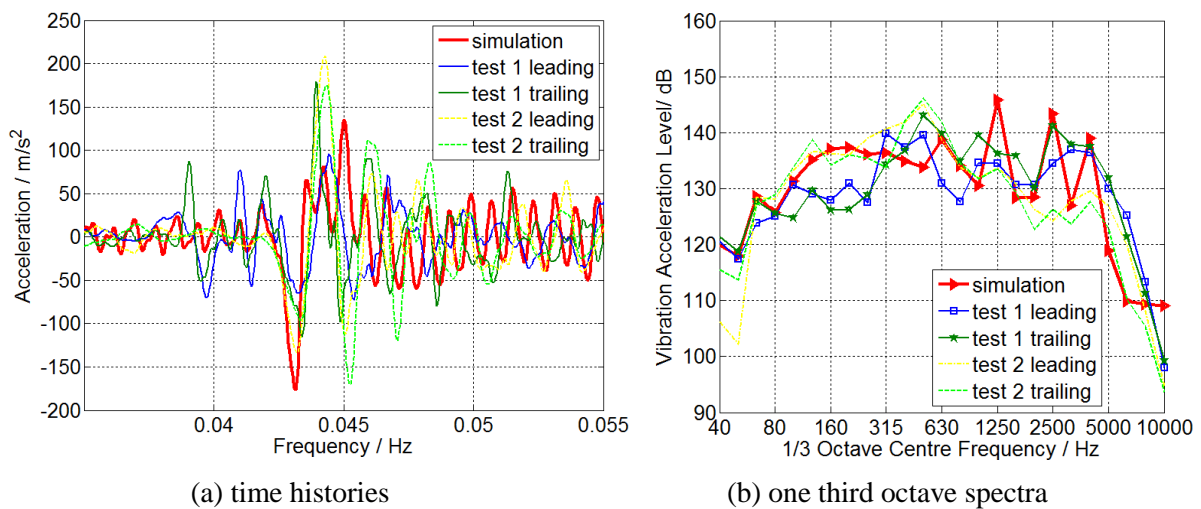


Figure 6: Comparison of simulated wheel vibration and measured ABA

The wavelet power spectrum (WPS) indicates the energy distribution of a signal regarding both frequency components and space distribution in a frequency range concerned. The WPS of the simulated wheel vibration and the measured ABA are compared in the same scale in Fig. 7. To emphasis the main energy parts and make the comparison clearly, only the frequency range below 5 kHz is plotted. It can be noticed that in both the simulation and the measurement results, the energy concentrations take place just at the IJ position and the dominant frequency focuses on about 500 Hz. For each measurement, the WPS at the leading axle looks very similar to that at the trailing axle, but difference exists between the two measurements. There exist obviously some high frequency contents in the WPS of measurement 1, performed before rail grinding. Although less prominent than the dominant frequency contents, subtle energy concentrations are noticeable at high frequency range around the IJ position in the WPS of simulation and measurement 1, which indicates that the high frequency contents of wheel impact vibration over IJ can reach up to 5 kHz or even higher. Since the same scale is applied for each WPS, the energy value can be reflected by the area of energy concentration spot. By comparing the energy magnitudes of WPS in one measurement, it can be found that the energy value of impact vibration from the trailing axle is higher than that from the leading axle. The reason of this phenomenon will be further studied in future; While comparing the energy value from two different measurements, it seems that although rail grinding was performed just before the measurement 2, the impact energy in the frequency range below 1 kHz is still significant higher than that from measurement 1, which could be probably due to the deterioration of substructures.

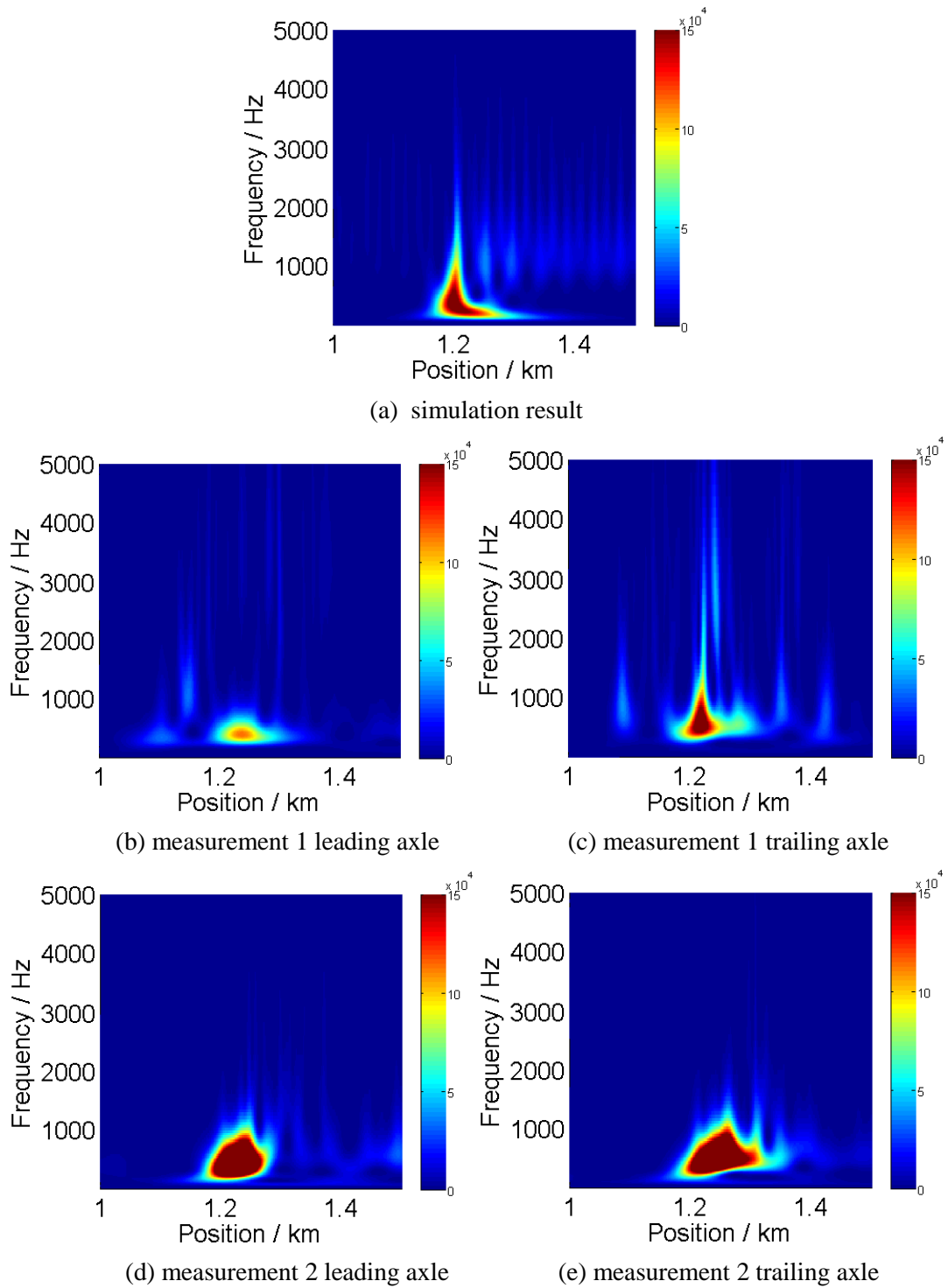


Figure 7: WPS of simulated wheel vibration and measured ABA

### 3 Impact noise reproduction

#### 3.1 Boundary element method for noise radiation

After the validation of FE model, the Boundary Element method [13] is employed to transform the vibration of the wheel and rail into acoustic radiation. In this case, a boundary surface enclosing a volume (rail or wheel) is surrounded by an ideal and homogeneous fluid medium (air). In the frequency domain,



the acoustic wave propagation in an ideal fluid is governed by Helmholtz equation, which can be discretized into a linear equation system by meshing the vibration surface of rail and wheel. Because of the non-linear character of impact problem, the transient vibration response of track structural is computed in the time domain. Through the Fast Fourier Transform, velocities on the surface of the structure are converted into a frequency response, which can be further taken as boundary conditions for the BEM. This frequency-domain method allows the calculation of sound pressure at any observation point of the acoustic domain.

### 3.2 Noise propagation and contribution

Relying on the FE Model and the noise calculation method described above, the impact noise emission of the modelled wheel-rail system were obtained. The distribution of receivers employed to collect the acoustic signals generated by the track system is shown in Fig. 8. Taking in-situ measurement scenario into consideration, the far-field receivers are placed at the same height as the wheel axle (0.6 m) to reduce the ground reflection influence and perpendicular to the wheel web plane with distances of 1.5 m, 3 m and 6 m respectively. The near-field receiver is located at 0.03m (an approximation to 0 m) from the fishplate.

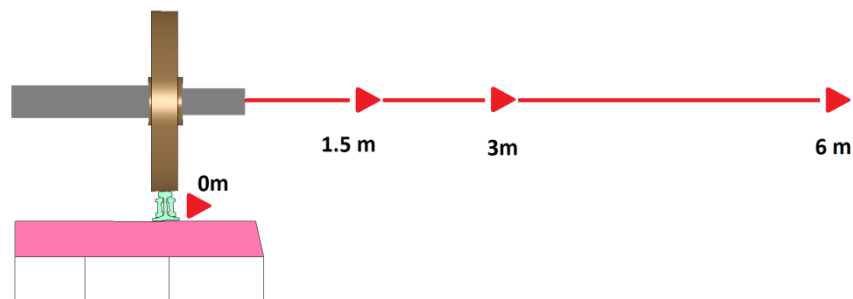


Figure 8: Placement of sound receivers

On the basis of the BEM, the vibrating rail, wheel and sleepers can be regarded as the sources of acoustic emission. One third octave spectra of the total impact noise and the noise emission contributed by the rail at each observation point are shown in Fig. 9 (a) and Fig. 9 (b) respectively. In the spectra of the total impact noise, it shows four main frequency bands at around 600 Hz, 2 kHz, 3 kHz and 6 kHz. Among them, the peaks of spectra at centre frequency of 630 Hz and 3 kHz are more predominant. From the gap widths between spectra collected by different observation point, the decay rate of noise in the analysing frequency range during propagation from near-field observation point to far-field ones can be determined. Fig. 9 (a) shows that the predicted impact noise in the frequency range between 800 Hz and 3 kHz decays less significantly than in the other frequency ranges, which also implies that the impact noise in the frequency range of 800 Hz- 3 kHz is more likely to be transmitted as the noise pollution and required an extra attention and prevention. The peak of one third octave spectrum at 6.3 kHz disappears when the propagation distance is over 3m, which indicates that the near-field observation point is necessary when the high-frequency content of impact noise is required to be captured in the test. For the noise contributed by the rail, the common dominant frequencies of both near-field signal and far-field signals are around 2 kHz and 3 kHz. The one-third octave curves of sound collected by 0 m observation point also presents a peak at 6.3 kHz, which dies away during propagation. Since previous studies on impact noise never extended the analysing frequency range to more than 5 kHz, measurements are required for validation of these results.

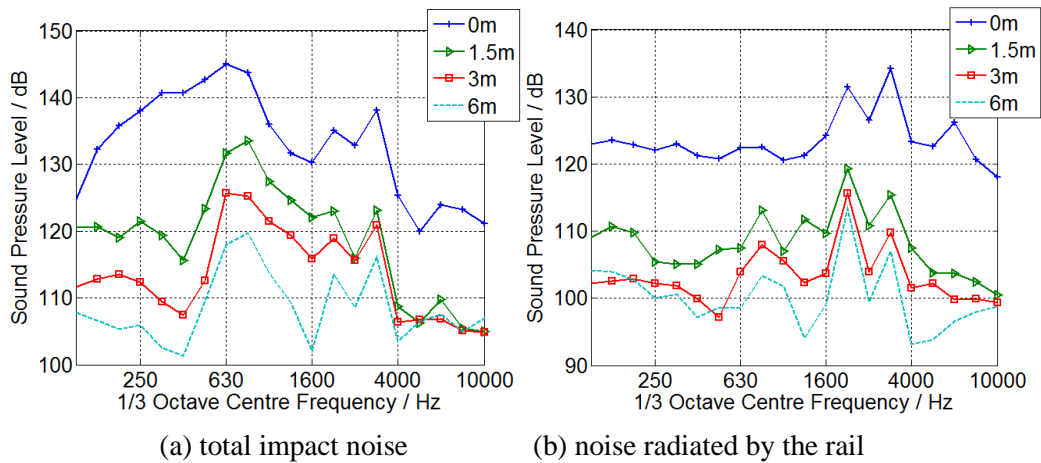


Figure 9: One-third octave of impact noise

A good agreement can be found in Fig. 10 when comparing the results calculated in this paper with the experimental and prediction results in literature [14], which also works on impact noise generation over IJ. In Fig. 10 (a), two obvious peaks of one third octave spectrum at around 600 Hz and 3 kHz correspond well with the testing and calculation results in the literature, while the analysed frequency in this paper is extended to 10 kHz. The impact noise shown in Fig. 10 (a) was calculated at the observation point of 1.5 m, while the testing noise shown in Fig. 10 (b) was measured at a distance of 1.3 m from rail (2 m from track centre). Since the traveling speed of testing train in the literature was only 35 km/h, much slower than the simulation speed of 100 km/h used in this paper, the sound pressure levels (SPL) of impact noise have significant difference. Another difference from the literature results is the impact noise contribution of sleepers. The noise radiated by sleepers was predicted to devote more in the frequency range below 1kHz in the literature than that predicted in this paper. One possibility could be that the mesh size of sleeper model in this paper was not sufficiently small for noise calculation by BEM.

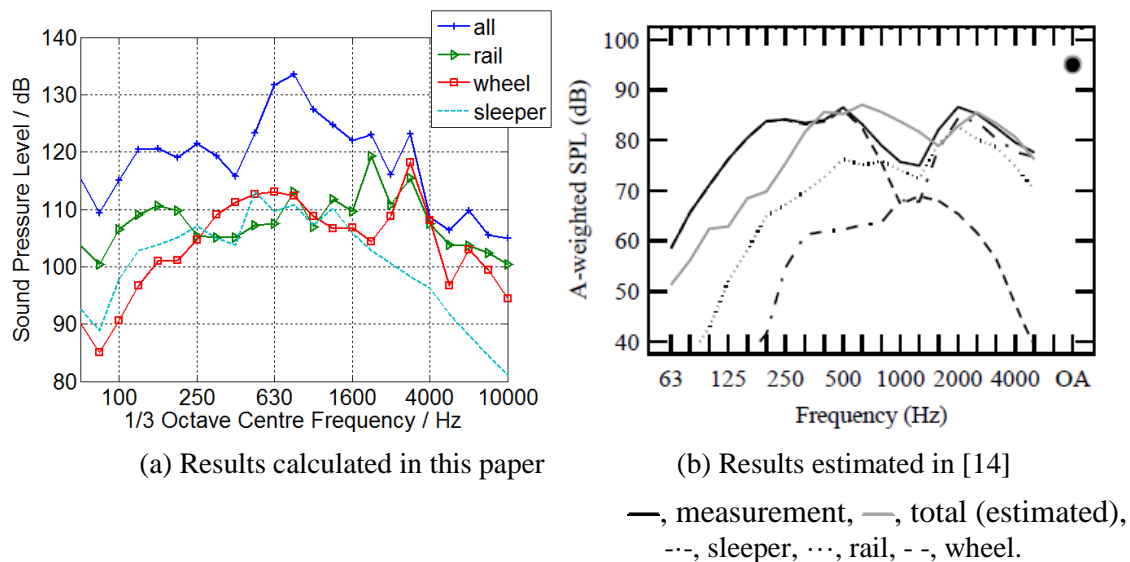


Figure 10: Noise contribution

## 4 Conclusion and Future work

A full finite element wheel-track interaction model is developed in this paper to study the wheel-rail impact noise excited by an insulated joint. The properties of the track model and the vibration response of the wheel model are respectively validated with hammer test and measurement of axle box acceleration.

The good agreements of the results qualify the model for simulating the noise generated by wheel-rail impact at IJ. The BEM based on Helmholtz equation is employed to transform the structural vibrations of the wheel-track simulated by the FE model into acoustic signals. By analysing the acoustic signals collected at observation points located at different distance from IJ, the decay rate of impact noise at different frequency bands during propagation can be determined. The predictions of total impact noise radiation and the noise contributions of different track components are in good agreement with results reported in the literature, while the effective frequency range is successfully extended from 5 kHz to 10 kHz.

The explicit integration finite element method has been proved to be a promising method for simulating the generation of impact noise. For a precise validation, the experimental vibro-acoustic behaviour of the wheel-track structure during train pass-by needs to be measured in the future. In order to obtain accurate solution in the transient dynamic calculation and high-frequency sound calculation, the elements in the model need to be with relatively small sizes, which consequently leads to high computing costs by BEM. A more efficient sound calculation method should be developed in the future. In addition, a sleeper is currently modelled with only 8 solid elements. Thus, the noise radiation of sleepers cannot be accurately reproduced. As another main sound emission source, a detailed sleeper model should be established in future work.

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