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Multiple Andreev reflections and Shapiro steps in a Ge-Si nanowire Josephson junction

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We present a Josephson junction based on a Ge-Si core-shell nanowire with transparent superconducting Al contacts, a building block which could be of considerable interest for investigating Majorana bound states, superconducting qubits, and Andreev (spin) qubits. We demonstrate the dc Josephson effect in the form of a finite supercurrent through the junction and establish the ac Josephson effect by showing up to 23 Shapiro steps. We observe multiple Andreev reflections up to the sixth order, indicating that charges can scatter elastically many times inside our junction and that our interfaces between superconductor and semiconductor are transparent and have low disorder.

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I. INTRODUCTION

Josephson junctions are defined as a weak link between two superconducting reservoirs, which allows a supercurrent to be transported through intrinsically nonsuperconducting materials, as long as the junction is shorter than the coherence length [1,2]. While early Josephson junctions realized a weak link by using thin layers of oxide, microconstrictions, point contacts, or grain boundaries [3–7], access to complex mesoscopic semiconducting materials have led to Josephson junctions in which control over the charge carrier density enables *in situ* tuning of the junction transparency and critical current [8–13].

Devices employing semiconducting nanowires have consequently explored a wide range of applications in a variety of material systems such as SQUIDs (superconducting quantum interference devices) [14–16], π junctions [15,17–19], and Cooper pair splitters [20,21]. Additionally, superconducting trans- and gatemon qubits have been successfully realized using InAs nanowires [22,23] and carbon nanotubes [24], while considering two-dimensional materials, graphene [25] and InAs-InGaAs quantum wells [26] have been used.

Another field where induced superconductivity in mesoscopic junctions is key is the undergoing experimental confirmation of Majorana fermions. This has resulted in a great number of works [27–32], but results have been limited to only a handful of material systems.

In this work we present a Josephson junction with transparent high-quality interfaces based on semiconducting Ge-Si core-shell nanowires. This material system has proven itself in the realm of normal-state quantum dots [33–41], but apart from a limited number of reports [42–45], topics related to induced superconductivity are relatively unexplored.

Apart from the possibility for Ge-Si nanowires to be implemented in trans- or gatemon qubits, holes in this system possess several interesting physical properties which makes them highly suitable for hosting Majorana fermions [46] and Andreev (spin) qubits [47–53]. They are predicted to have strong, tunable spin-orbit coupling [54,55], have a Landé g factor that is tunable with electric field [37], and have potentially zero hyperfine interaction [56]. The realization of a Josephson junction with transparent high-quality interfaces is a crucial step towards all the described applications for this system.

Using superconducting Al contacts on the Ge-Si nanowire, we will present the experimental observation of the dc Josephson effect: a finite switching current I_{SW} through the nanowire Josephson junction. We will also look at multiple Andreev reflections (MAR) [57,58] and analyze the position of the resulting conductance peaks inside the superconducting gap of Al, Δ_{Al} . Additionally, we look at the temperature dependence of MARs and I_{SW} and, finally, we irradiate our junction with microwaves resulting in Shapiro steps, a report on the ac Josephson effect in this system. The observation of both the dc and the ac Josephson effect confirms we have a true Josephson junction.

II. NANOWIRE JOSEPHSON JUNCTION

Figure 1(a) shows a SEM (scanning electron microscopy) image of the device with a channel length of ~ 150 nm, designed for four-terminal measurements. As described in detail in Ref. [59], Ge and/or Si interdiffuses with the Al contacts during thermal annealing. This leaves a semiconducting island of ~ 50 nm, which can be identified by a difference in contrast in the nanowire core on the SEM image. This has been confirmed by a TEM (transmission electron microscopy) study with an EDX (energy-dispersive x-ray) spectrum analysis on the same device (see Ref. [59]).

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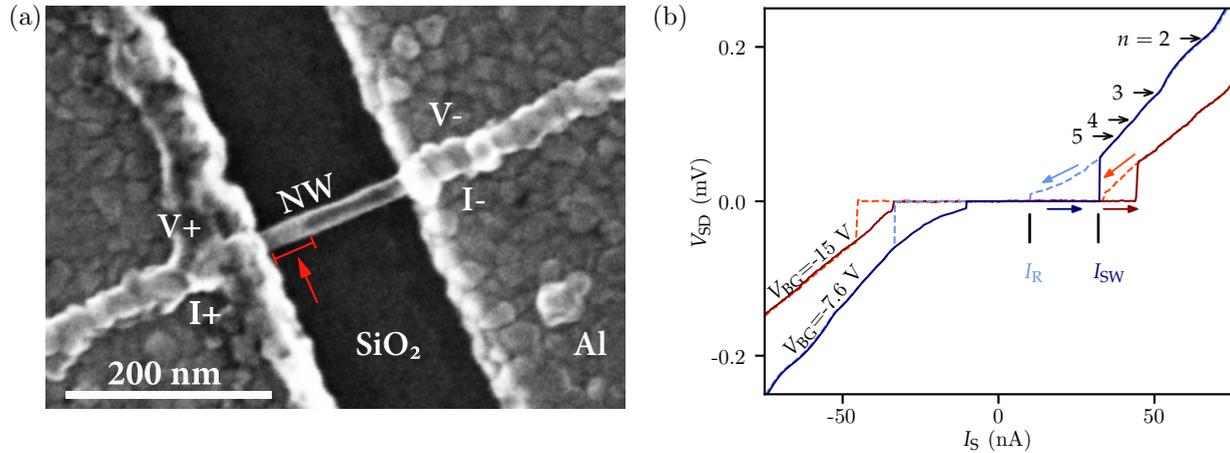


FIG. 1. dc Josephson effect in a Ge-Si nanowire. (a) False-color SEM image of the device under investigation. A nanowire with a 20 nm diameter lies on the SiO_2 covered substrate and is contacted by an Al source and drain. The channel length is ~ 150 nm with a semiconducting island (red arrow) of ~ 50 nm. (b) V_{SD} vs I_S for $V_{BG} = -7.6$ V and $V_{BG} = -15$ V. I_S is swept from left to right (solid) and successively from right to left (dashed) denoted by the colored arrows. I_{SW} and I_R are indicated for $V_{BG} = -7.6$ V. Horizontal black arrows indicate “wiggles” in the curve corresponding to MAR of the n th order.

We plot the sourced current I_S versus the measured voltage between source and drain V_{SD} in Fig. 1(b). Sweeping I_S forward, i. e., from zero to finite bias, we find that the junction switches from the superconducting state to a dissipative state at a switching current of $I_{SW} = 44$ nA at a backgate voltage $V_{BG} = -15$, while $I_{SW} = 32$ nA at $V_{BG} = -7.6$ V. When sweeping backwards, i. e., from finite I_S to zero, the junction returns to its superconducting state at the retrapping current I_R , resulting in hysteretic behavior. For a backgate voltage $V_{BG} = -15$ V, we find $I_R = 34$ nA and a ratio $I_{SW}/I_R = 1.3$, while for $V_{BG} = -7.6$ V, $I_R = 10$ nA and a ratio $I_{SW}/I_R = 3.4$. This indicates that our junction is underdamped [60] and that I_{SW} , as well as the damping, depend on V_{BG} , mainly due to the changing number of subbands participating in transport and their position relative to the Fermi energy of the Al contacts. As described in extensive detail in Ref. [44], the device is tunable from full depletion (with $I_{SW} = 0$) to highly transparent, where $I_{SW} > 40$ nA on which this work is focused.

III. JUNCTION CHARACTERISTICS

We will now establish whether our nanowire is ballistic or diffusive. In the ballistic case, particles traversing the junction do not scatter, except on the interfaces. In the diffusive case, particles encounter scattering sites inside the junction which leads, for example, to suppression of I_{SW} [61]. For a ballistic nanowire and completely transparent interfaces, one expects the normal-state conductance to appear in multiples of the conductance quantum $G_0 = 2e^2/h$, and the critical current in multiples of the maximum critical current for a single subband $I_{C,MAX} = e\Delta_{Al}/\hbar = 51$ nA [2]. In our case, the finite interface transparency [44] leads to lower observed values of both the conductance G and the switching current I_{SW} , where I_{SW} is suppressed by additional mechanisms such as electromagnetic coupling with the environment [9], premature switching, and heating effects [2,62]. From experiments it is therefore not trivial to conclude whether our nanowire is diffusive or ballistic and we therefore make a quantitative estimation based on calculations.

We start with estimating the elastic scattering length using $l_e = \mu m^* v_F / e$ [63], with μ the hole mobility, m^* the effective hole mass, and v_F the Fermi velocity. We use $\mu \approx 3500$ $\text{cm}^2/\text{V s}$ (determined at 4 K; see [64]) and $m^* \approx 0.5m_e$ for the mixed heavy and light holes [54,65] with m_e the free electron mass. To obtain the Fermi velocity we use the solutions of the Schrödinger equation for a cylindrical potential well and find the expression for the Fermi energy of the n th subband with quantum number l as $E_{n,l} = \hbar^2 \alpha_{n,l}^2 / 2m^* R^2$ [66] with $\alpha_{n,l}$ the l th root of the n th order Bessel function and R the wire radius. For the first subband this gives $E_{1,1} \approx 15$ meV, corresponding to a Fermi velocity $v_F \approx 1 \times 10^5$ m/s and an estimated elastic scattering length of $l_e \approx 100$ nm. Using a gate lever arm $\alpha = 0.02$ and the fact that the nanowire is depleted at $V_{BG} \approx 5$ V [44], we find that in the regime $V_{BG} = [-7.6, -15]$ V we operate at six ($E_{6,1} \approx 256$ meV) to eight ($E_{8,1} \approx 388$ meV) subbands, increasing l_e to ~ 400 nm.

As can be seen in Fig. 1(a), our nanowire channel length is ~ 150 nm, but as discussed before, our semiconducting island is ~ 50 nm. We are therefore far away from the diffusive limit $l_e \ll L$ with a corresponding coherence length of $\xi_{diff} = \sqrt{\hbar D / \pi \Delta_{Al}} \approx 390$ nm with $D = v_F l_e$. We approach the ballistic limit $l_e \gg L$, with a coherence length of $\xi_{ball} = \hbar v_F / \pi \Delta_{Al} \approx 380$ nm [2] independent of l_e . This places the nanowire well within the ballistic limit, as is reaffirmed by the fact that the semiconducting island can be host to a single few-hole quantum dot [44] and that highly tunable normal-state devices can be host to dots of length $l > 400$ nm [38]. By increasing the Al-nanowire interface transparencies, fully ballistic junctions could therefore be realized with lengths up to a few hundred nanometers.

In Ref. [44] we extract an averaged $\langle I_{SW} R_N \rangle = 217 \mu\text{eV} \sim \Delta_{Al}$, close to the theoretical maximum. Since our Ge-Si segment is ballistic, the Thouless energy has only meaning in terms of the time of flight through the junction $\tau = L/v_F \approx 125$ fs, so that $E_{Th,ball} = \hbar/\tau \approx 5.5$ mV $\gg \Delta_{Al}$ for the sixth subband and the induced gap is therefore $\sim \Delta_{Al}$.

Out of the seven devices exhibiting superconducting transport, three devices showed gate tunability and Shapiro steps.

There are strong indications that in the other four devices the Al interdiffusion has progressed throughout the channel (see Ref. [59]), resulting in a completely metallic superconducting device.

IV. MULTIPLE ANDREEV REFLECTIONS

Small wiggles are visible in the V_{SD} versus I_S curve for $V_{BG} = -7.6$ V in Fig. 1(b), which are a signature of MAR. This becomes clearer in the differential conductance $\partial I_S / \partial V_{SD}$ for a range of V_{BG} in Fig. 2(a): the wiggles in V_{SD} translate to conductance peaks seen at values of V_{SD} corresponding to $eV_{SD}(n) = 2\Delta_{Al}/n$ [2], with n an integer denoting the MAR order. $n = 1-5$ are indicated by the green arrows in Fig. 2(a) for positive bias [orders $n = 2-5$ are indicated in Fig. 1(b)]. The strong conductance peak at $V_{SD} = 0$ corresponds to a supercurrent and is a direct consequence of the inversion of the I_S and V_{SD} axes (see Methods), which maps I_S onto the corresponding value of V_{SD} . Since a supercurrent implies $V_{SD} = 0$ for a range of I_S , this results in a strong peak in $\partial I_D / \partial V_{SD}$. The height of the oscillating black regions for $V_{SD} < 0.05$ mV as a function of V_{BG} is a measure for the magnitude of I_R (see Methods), where the oscillations correspond to varying occupation of the subbands of a weak confinement potential in the wire [44].

The MAR conductance peaks can be more clearly distinguished in individual line traces in Fig. 2(b) and we focus on the blue trace at $V_{BG} = -7.6$ V. The finite width of the MAR peaks reflects the distribution of the DOS peak at $eV_{SD} = 2\Delta_{Al}$ and is additionally broadened by phase decoherence and inelastic processes when quasiparticles traverse the channel [2,67]. We extract the peak positions (P.P.) in V_{SD} of the first six orders and plot them versus the inverse MAR order in the inset in Fig. 2(b). We expect the second order MAR peak to be at the position of our superconducting gap, i. e., for $n = 2$, $eV_{SD} = \Delta_{Al}$. For a more accurate estimate of Δ_{Al} we perform a linear fit through zero for the six MAR peak positions and find $\Delta_{Al} = 0.212$ meV, which translates to a critical temperature of our Al $T_{C,Al} = \Delta_{Al}/1.764 k_B T = 1.39 \pm 0.03$ K [2]. This is confirmed by an independent measurement of the T_C of an Al stripline (not shown) and is in good agreement with the critical temperature observed in Fig. 3.

In Fig. 2(b) higher-order MAR peaks become increasingly hard to resolve because of the hyperbolic relation of V_{SD} with n . In Fig. 2(c), we therefore convert the x axis from V_{SD} to units of $n = 2\Delta_{Al}/eV_{SD}$, resulting in evenly spaced orders of n , and plot the conductance for positive bias for the same three V_{BG} as in Fig. 2(b). We see that, for $n > 6$, the conductance peaks can no longer be unambiguously assigned and they span multiple n . Possibly, the peak patterns for high-order MAR are a superposition of many overlapping MAR processes.

Comparing the blue curve in Fig. 2(c) with the orange and green curves taken at different V_{BG} , we observe that peak positions for lower order MAR do not perfectly reproduce, for instance, the orange curve does not show a clear peak at $n = 4$. We partly explain this by considering our interface transparencies which act as a weak confinement potential, resulting in highly broadened energy levels in the wire. The relative position of these levels with respect to the Fermi level changes the resonant condition for MAR, resulting in a shift

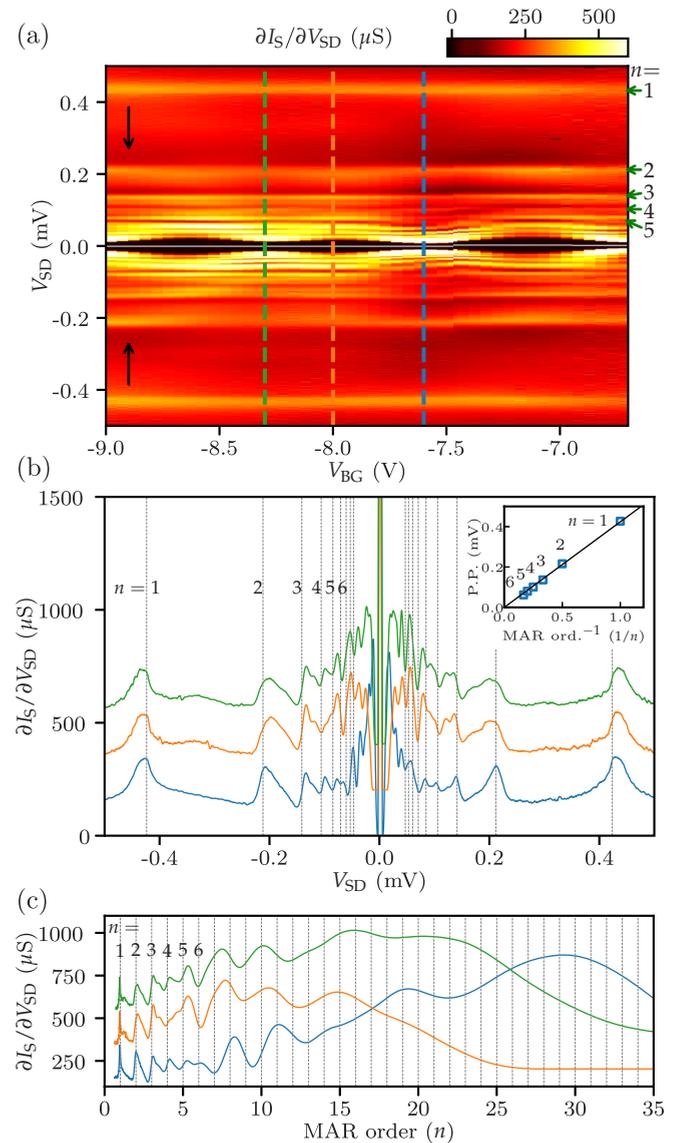


FIG. 2. Multiple Andreev reflections up to the sixth order. (a) Differential conductance $\partial I_S / \partial V_{SD}$ vs V_{SD} and V_{BG} . The black arrows indicate the sweep direction (see Sec. IX B). Horizontal equipotential lines of increased conductance indicated by the green arrows correspond to MAR. Current biased measurement where the I_S and V_{SD} axes were inverted (see Methods) before numerical derivation. Only return current was measured (see black arrows) in a highly hysteretic regime [see blue curve in Fig. 1(b)] to reach the low-voltage regime. (b) Single traces of $\partial I_S / \partial V_{SD}$ vs V_{SD} for three values of V_{BG} . Green, orange, and blue (traces offset by 200 μS) taken at $V_{BG} = -8.3$, -8 , and -7.6 V [see Fig. 2(a), dashed lines]. Vertical gray dashed lines denote expected MAR peak positions calculated by $n = 2\Delta_{Al}/eV_{SD}$ for $n = 1-10$. Inset: MAR peak positions (P.P.) vs inverse MAR order $1/n$ at $V_{BG} = -7.6$ (blue trace) for positive bias. The black line is a linear fit through zero. (c) Same data as (b) plotted vs n , only positive V_{SD} is shown. The vertical dashed gray lines show integers of n which can be matched with the MAR peaks up to $n = 6$.

of the MAR peak positions [68]. Inspecting Fig. 2(a), the high-order MAR peaks ($n > 5$) are indeed modulated, both in intensity and position in V_{SD} , by the changing charge and

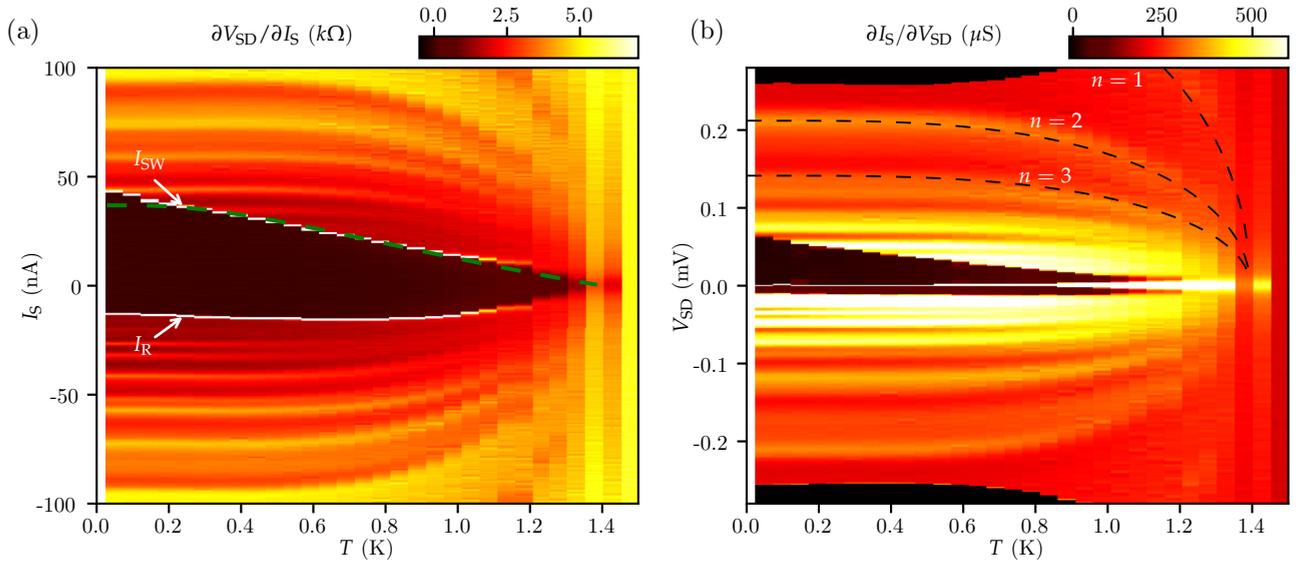


FIG. 3. Temperature dependence of MAR and I_{SW} . (a) Differential resistance $\partial V_{SD}/\partial I_S$ vs I_S and T and (b) differential conductance $\partial I_S/\partial V_{SD}$ vs V_{SD} and T , both for the same data with $V_{BG} = -13.35$ V. I_S and V_{SD} are swept from negative to positive bias. In (a) I_{SW} and I_R are denoted by the white arrows and the green dashed line is a fit based on the Eilenberger equations [70]. Black dashed curves in (b) are fits to Eq. (1).

subband population represented by the black regions at low bias ($V_{SD} < 0.05$ mV).

We conclude from Fig. 2 that the resolvability of MAR up to $n = 6$ means that quasiparticles can elastically scatter at least six times on the interfaces, each time traversing the nanowire channel. This requires very low inelastic scattering probabilities and a high (though finite) interface transparency [69].

V. TEMPERATURE DEPENDENCE OF I_{SW} AND MAR

We will now investigate the temperature dependence of the switching current and the multiple Andreev reflections. In Fig. 3(a) we plot the differential resistance $\partial V_{SD}/\partial I_S$ versus I_S as a function of temperature T . The black region $\partial V_{SD}/\partial I_S = 0$ indicates superconductivity and we can see the decrease of I_{SW} for increasing T until I_{SW} disappears at $T \approx 1.4$ K, in agreement with $T_{C,Al} = 1.39$ K calculated from Δ_{Al} . The slight increase of $|I_R|$ between $T = 0$ and 0.7 K could be due to changes in the thermal conductivity of the devices' surroundings, leading to better thermalization at higher temperatures.

For ballistic supercurrent through a superconductor-normal metal–superconductor Josephson junction, the critical current was modeled by Galaktionov and Zaikin [70] based on the Eilenberger equations. Note that this model neglects the spin-orbit interaction, but arbitrary barrier transparencies can be included and an average is provided over multiple modes. We have used this model to fit our $I_c(T)$ data. As input parameters we used the critical temperature of 1.4 K, a Fermi velocity of 1×10^5 m/s, and an electrode separation of 50 nm. These parameters completely determine the shape of the $I_c(T)$ and provide a zero-temperature estimate for the average critical current of 6 nA per mode. For the experimentally measured I_c , this would correspond to about seven modes in the junction, consistent with our estimate of

the number of modes based on the normal transport data. We furthermore obtain an average transparency of $\sim 50\%$, lower than the previously obtained transparency of $\sim 80\%$ [44] using the BTK model [71], averaged over a large gate voltage. This difference could be explained by the fact that $I_{SW}(T)$ was only determined at a single value of V_{BG} and that I_{SW} is likely to be suppressed with respect to the actual critical current of the junction. The resulting model $I_c(T)$ has been plotted in Fig. 4(a), together with the experimental data.

The MAR signatures visible outside the superconducting region scale with Δ_{Al} and therefore gradually decrease and converge to $V_{SD} = 0$ for $T \rightarrow T_{C,Al}$. Figure 3(b) shows the same data set as Fig. 3(a) converted to a voltage-biased plot (see Methods) and since for MAR order $n = 2$, $V_{SD} = \Delta_{Al}$, we have a direct measure of $\Delta_{Al}(T)$. We use the BCS interpolation formula [72,73]:

$$\Delta(T) = \frac{2\Delta_{Al,0}}{n} \tanh\left(1.74\sqrt{\frac{\Delta_{Al,0}}{1.76k_B T} - 1}\right), \quad (1)$$

where we replaced the prefactor $\Delta_{Al,0}$ with $2\Delta_{Al,0}/n$, where $\Delta_{Al,0} = 0.212$ μeV is the superconducting gap of Al at $T \approx 0$ as determined in Fig. 2(b). We plot this curve in Fig. 3(b) and find excellent agreement for the $n = 2$ MAR peak and a good fit for $n = 3$. The value of $\Delta_{Al,0}$ corresponds to the observed $T_{C,Al} \approx 1.4$ K, while Δ_{Al} follows the BCS curve as a function of T , i.e., the MAR are indeed an excellent measure for the superconducting gap of the Al contacts.

VI. SHAPIRO STEPS

We now look at the ac Josephson effect by irradiating our junction with a $\lambda/4$ antenna located ~ 5 mm above the chip with frequencies ranging from 0.8 to 4.4 GHz. Figure 4(a) shows V_{SD} versus I_S for three different frequencies at finite microwave amplitudes V_{rms} , revealing Shapiro steps in the

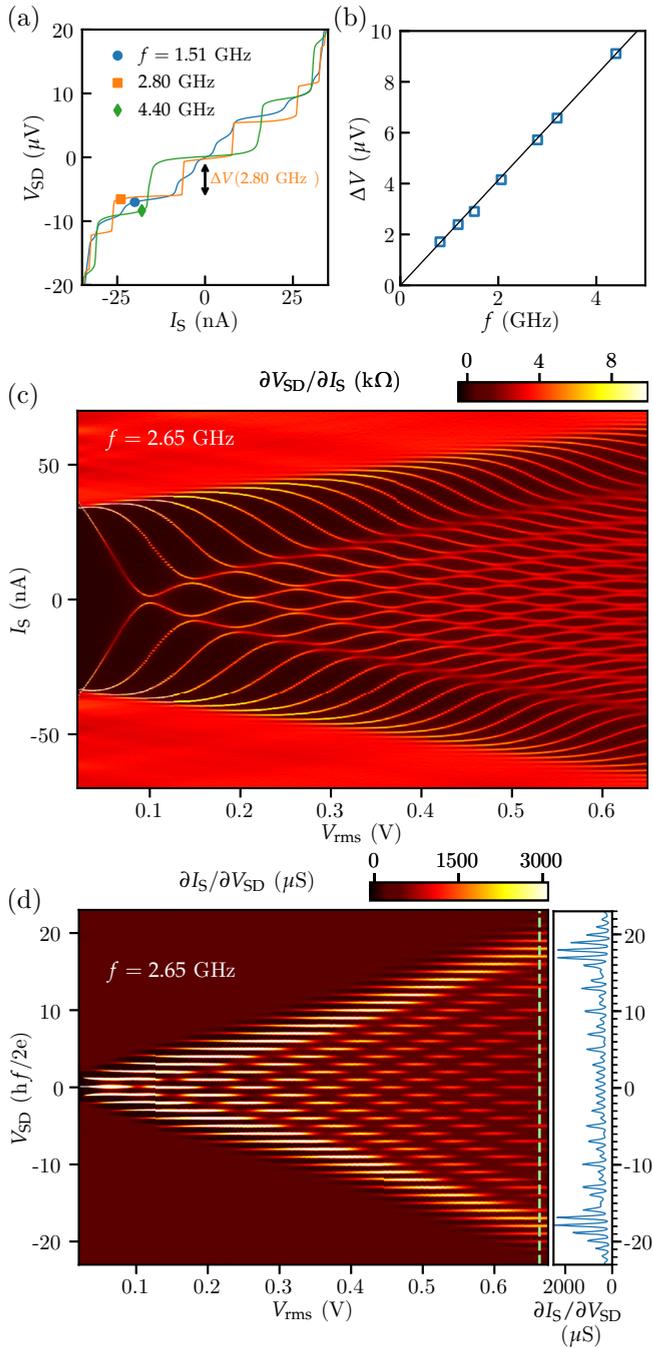


FIG. 4. ac Josephson effect, up to 23 Shapiro steps. (a) V_{SD} vs I_S for frequencies $f = 1.51, 2.80,$ and 4.40 GHz at respective amplitudes $V_{rms} = 0.11, 0.13,$ and 0.13 V. V_{rms} values are ac amplitudes applied before filtering. $f = 2.8$ GHz results in a step height of $\Delta V = 5.8 \mu\text{V}$ (black arrow). (b) Step height ΔV vs microwave frequency f extracted from data (blue boxes). The black line is a plot of $\Delta V = hf/2e$. (c) Differential resistance $\partial V_{SD}/\partial I_S$ vs I_S and microwave rms voltage V_{rms} applied at a frequency of 2.65 GHz at $V_{BG} = -15$ V [red curve in Fig. 1(b)]. (d) Left: $\partial I_S/\partial V_{SD}$ vs V_{SD} and V_{rms} , same measurement data as (c) with I_S and V_{SD} axes reversed before numerical derivation (see Methods). V_{SD} shown in units of $hf/2e$. Right: line cut at $V_{rms} = 0.66$ V showing 23 peaks.

current-voltage relation. Shapiro steps [74] are a direct manifestation of the ac Josephson effect, where phase locking

occurs between the quasiparticles in the junction and the applied microwaves. Starting from the ac Josephson relation $V = \frac{\hbar}{2e} \frac{d\phi}{dt}$, quasiparticles can acquire a phase of $\phi = 2\pi m$ per period of the applied microwave frequency f with m an integer denoting the Shapiro step number. We can thus write $\frac{d\phi}{dt} = 2\pi mf$, translating to a total dc voltage $V_{SD} = m\Delta V = mhf/2e$ [2], where m is determined by I_S and microwave amplitude V_{rms} . The extracted step height for various frequencies in Fig. 4(b) shows good agreement. We attribute the qualitative variation in the rounding of the steps as a function of frequency to spectral broadening of the microwaves, in turn caused by the microwave antenna properties and the coupling to the Faraday cage in which the sample resides.

We now fix the applied frequency at 2.65 GHz and plot $\partial V_{SD}/\partial I_S$ versus I_S and V_{rms} at $V_{BG} = -15$ V in Fig. 4(c). When increasing V_{rms} , clearly visible lines of differential resistance enter the bias window, each corresponding to a stepwise increase of V_{SD} by $m\Delta V = \text{const}$ on the plateaus enclosed by the steps. As in most experimental setups, our microwave source and antenna have a much higher impedance than our superconducting Josephson junction [2,75] and it therefore acts as an ac current source. Therefore, the width of the current plateaus cannot be described by simple Bessel functions, but can only be numerically approximated [2,75,76].

To gain insight in the number of Shapiro steps and their corresponding plateau heights in Fig. 4(c), we show a V_{SD} biased plot in units of $\Delta V = hf/2e$ of the same measurement data in Fig. 4(d). The plateaus of constant V_{SD} in Fig. 4(c) are now visible as peaks in differential conductance $\partial I_S/\partial V_{SD}$. Looking at the line cut on the right we see that up to 23 steps are visible, all aligned with values of $m\Delta V = mhf/2e$. This clear demonstration of the ac Josephson effect in Fig. 4, together with dc effects such as MAR and finite I_{SW} , proofs that our junction is indeed a well behaved Josephson junction.

VII. SHAPIRO STEPS VERSUS V_{BG}

Previously, V_{BG} was fixed at -15 V, corresponding to a region with a high I_{SW} and low hysteresis, i.e., close to critical damping corresponding to a Stewart-McCumber parameter β_C close to 1 [2]. In Fig. 5(a) we show a current-sourced backgate dependence of Shapiro steps at fixed microwave frequency and power. The junction is generally hysteretic for regions with lower I_{SW} , observed in this figure at regions where the Shapiro steps are moving closer together on the I_S axis. This corresponds to a higher normal state resistance R_N which increases β_C and results in an underdamped junction. Since measurement data were acquired in both directions while sweeping I_S back and forth (after stepping V_{BG} with 25 mV after each sweep), hysteresis appears as a white speckle pattern caused by the data acquisition alternating directions in I_S (see for instance between $V_{BG} = -10$ and -8 V). The observed oscillations of I_{SW} (and indirectly R_N) as a function of V_{BG} are again the result of the varying population of subbands.

Figure 5(b) shows the voltage-biased backgate dependence of the same measurement data as Fig. 5(a), where plateaus in current are translated to peaks in $\partial I_S/\partial V_{SD}$ by inverting the I_S and V_{SD} axis and normalizing V_{SD} to ΔV . We identify five Shapiro steps which partially disappear in regions with increased R_N when the junction is hysteretic. For this specific

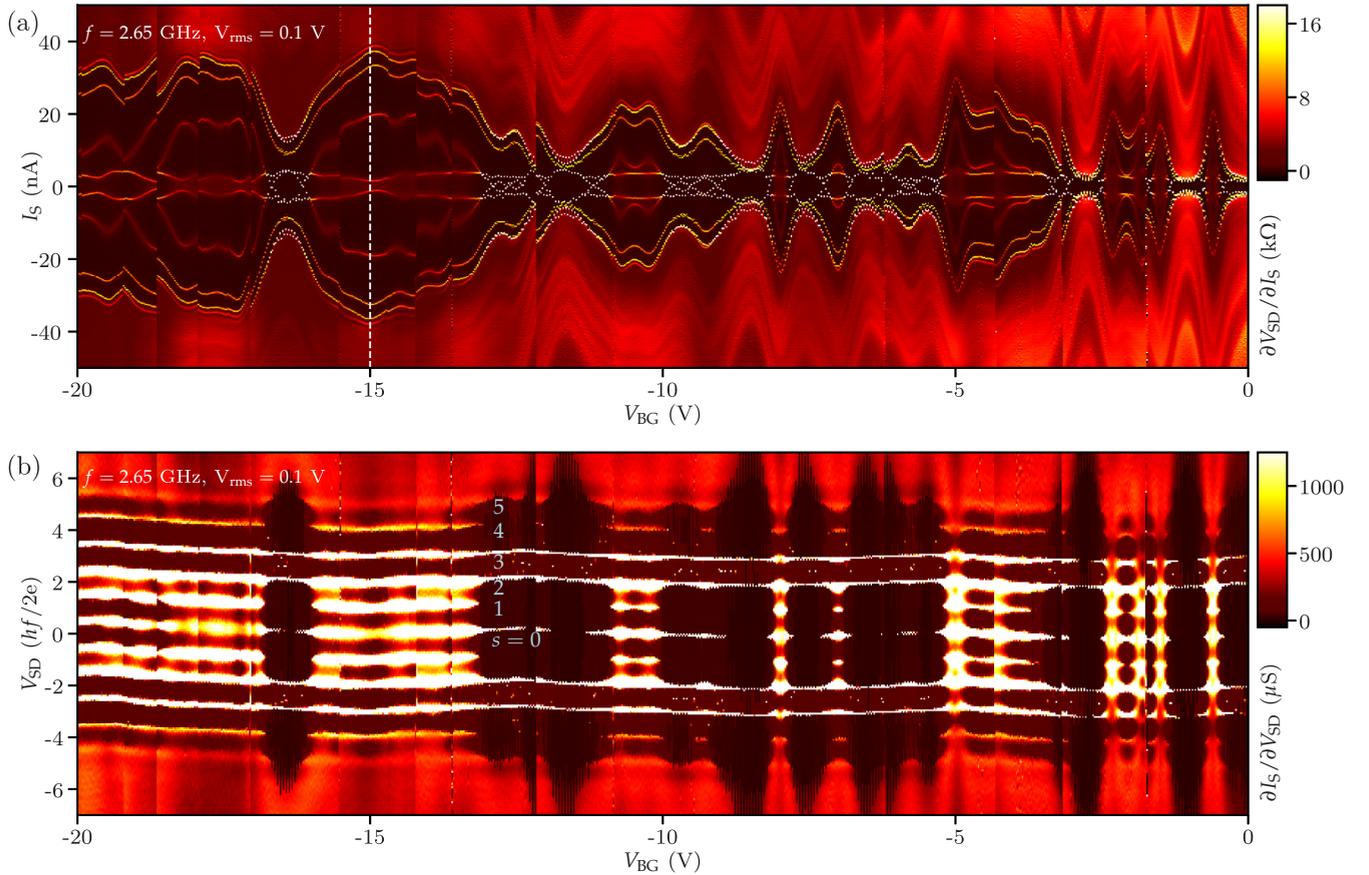


FIG. 5. Shapiro steps vs backgate voltage. (a) Differential resistance $\partial V_{\text{SD}} / \partial I_S$ vs I_S and V_{BG} at fixed microwave frequency $f = 2.65$ GHz and $V_{\text{rms}} = 0.1$ V. The direction in which I_S is swept is reversed after each step of $V_{\text{BG,step}} = 25$ mV. The white dashed line denotes $V_{\text{BG}} = -15$ V used in Fig. 4. (b) Differential conductance $\partial I_S / \partial V_{\text{SD}}$ vs V_{SD} (units of $hf/2e$) vs V_{BG} . Same data set as (a) where I_S and V_{SD} axes were inverted (see section Methods). We identify up to five Shapiro steps, i. e., current plateaus $s = 0-5$. The “wavy” pattern, i. e., the gradual shift of the lines in V_{SD} as a function of V_{BG} , is caused by small variations in the leakage current at different V_{BG} .

V_{rms} , steps zero, 1, and 4 disappear in the hysteretic regions, loosely corresponding to the smaller current plateau widths. Since the plateau widths vary (Bessel-like) with V_{rms} [see Fig. 4(c)], which steps are missing therefore changes as a function of V_{rms} (not shown here). At $V_{\text{BG}} = -15$ V, all steps are visible, which is the reason this specific voltage was used in Fig. 4.

VIII. CONCLUSION

We have realized a Josephson junction where the high interface transparency between the superconducting leads and the nanowire results in multiple Andreev reflections up to the sixth order. We additionally show up to 23 Shapiro steps, clearly demonstrating the ac Josephson effect in this system. We estimate the total contact transparency to be between 50% and 80% based on the temperature dependence and previously obtained results. We furthermore estimate the nanowire segment to be in the ballistic limit and improving the contact interfaces could therefore result in fully ballistic junctions.

Ge-Si nanowire-based Josephson junctions possess all ingredients necessary for obtaining Majorana fermions and in parallel experiments we have found very hard induced

superconducting gaps [59]. We therefore propose a followup experiment with a device design suitable for probing the zero-energy Majorana bound states in the nanowire [28]. Additionally, other applications, such as superconducting qubits and Andreev (spin) qubits, can now actively be pursued in this system.

IX. METHODS

A. Postprocessing of measurement data

All measurements in this work are performed using a three-probe measurement. A series resistance of 3.46 k Ω was subtracted from all measurement data. In Figs. 2, 3(b), 4(d), and 5(b), the data sets are obtained using a current source driving I_S with V_{SD} measurement after which a software routine is used to invert the source and measurement axis. To obtain equidistant points on the new V_{SD} source axis, the points are recalculated by interpolation in I_S on a grid with predetermined V_{SD} step size. The resolution of V_{SD} is chosen high enough so that no features in the original measurement of V_{SD} are lost. In Figs. 4(c) and 4(d) a similar grid interpolation procedure was used to convert the x axis from units of dBm to V.

B. MAR data set acquisition

In the open regime MAR peaks can only be seen when the junction is in the dissipative current state and, since higher-order ($n > 6$) MAR reside close to zero bias, they can be obscured by the superconducting “blind spot” of the junction. We use the bistable current-voltage relation (hysteresis) of our underdamped Josephson junction in Fig. 2(a), where we choose a region of V_{BG} with a low I_R . In order to measure the current-voltage relation of the junction way below I_{SW} , the low I_R is exploited by sweeping from finite $|I_S|$ to zero in both bias directions. We note that I_R is still finite which is reflected in the small black oscillating blind spot region around $|V_{SD}| = 0$, although a much larger range of V_{SD} can now be probed. The visibility of MAR also depends on G_N :

a higher G_N results in a lower voltage drop over the same I_S , thus effectively enhancing measurement resolution of the equipotential MAR peaks. This is especially important for higher order MAR (>4), since its hyperbolic relation with V_{SD} means that the corresponding peaks become very closely spaced.

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- [1] B. D. Josephson, *Phys. Lett.* **1**, 251 (1962).
 [2] M. Tinkham, *Introduction to Superconductivity: Second Edition* (Dover Publications Inc., Mineola, New York, 2004).
 [3] S. Shapiro, *Phys. Rev. Lett.* **11**, 80 (1963).
 [4] C. C. Grimes and S. Shapiro, *Phys. Rev.* **169**, 397 (1968).
 [5] K. K. Likharev, *Rev. Mod. Phys.* **51**, 101 (1979).
 [6] C. W. J. Beenakker, *Phys. Rev. B* **46**, 12841 (1992).
 [7] P. A. Rosenthal and E. N. Grossman, *IEEE Trans. Microwave Theory Tech.* **42**, 707 (1994).
 [8] I. V. Krive, S. I. Kulinich, R. I. Shekhter, and M. Jonson, *Low Temp. Phys.* **30**, 554 (2004).
 [9] P. Jarillo-Herrero, J. A. van Dam, and L. P. Kouwenhoven, *Nature (London)* **439**, 953 (2006).
 [10] G. Katsaros, P. Spathis, M. Stoffel, F. Fournel, M. Mongillo, V. Bouchiat, F. Lefloch, A. Rastelli, O. G. Schmidt, and S. De Franceschi, *Nat. Nanotechnol.* **5**, 458 (2010).
 [11] N. Mizuno, B. Nielsen, and X. Du, *Nat. Commun.* **4**, 2716 (2013).
 [12] J. C. E. Saldaña, R. Žitko, J. P. Cleuziou, E. J. H. Lee, V. Zannier, D. Ercolani, L. Sorba, R. Aguado, and S. De Franceschi, *Sci. Adv.* **5**, eaav1235 (2019).
 [13] N. W. Hendrickx, D. P. Franke, A. Sammak, M. Kouwenhoven, D. Sabbagh, L. Yeoh, R. Li, M. L. V. Tagliaferri, M. Virgilio, G. Capellini, G. Scappucci, and M. Veldhorst, *Nat. Commun.* **9**, 2835 (2018).
 [14] H.-S. Kim, B.-K. Kim, Y. Yang, X. Peng, S.-G. Lee, D. Yu, and Y.-J. Doh, *Appl. Phys. Express* **9**, 023102 (2016).
 [15] J. Cleuziou, W. Wernsdorfer, V. Bouchiat, T. Ondarçuhu, and M. Monthieux, *Nat. Nanotechnol.* **1**, 53 (2006).
 [16] F. Vigneau, R. Mizokuchi, D. C. Zanuz, X. Huang, S. Tan, R. Maurand, S. Frolov, A. Sammak, G. Scappucci, F. Lefloch, and S. De Franceschi, *Nano Lett.* **19**, 1023 (2019).
 [17] J. A. van Dam, Y. V. Nazarov, E. P. A. M. Bakkers, S. De Franceschi, and L. P. Kouwenhoven, *Nature (London)* **442**, 667 (2006).
 [18] H. I. Jørgensen, T. Novotný, K. Grove-Rasmussen, K. Flensberg, and P. E. Lindelof, *Nano Lett.* **7**, 2441 (2007).
 [19] R. Delagrangé, R. Weil, A. Kasumov, M. Ferrier, H. Bouchiat, and R. Deblock, *Physica B: Condens. Matter* **536**, 211 (2018).
 [20] L. Hofstetter, S. Csonka, J. Nygård, and C. Schönenberger, *Nature (London)* **461**, 960 (2009).
 [21] Z. B. Tan, D. Cox, T. Nieminen, P. Lähteenmäki, D. Golubev, G. B. Lesovik, and P. J. Hakonen, *Phys. Rev. Lett.* **114**, 096602 (2015).
 [22] G. de Lange, B. van Heck, A. Bruno, D. J. van Woerkom, A. Geresdi, S. R. Plissard, E. P. A. M. Bakkers, A. R. Akhmerov, and L. DiCarlo, *Phys. Rev. Lett.* **115**, 127002 (2015).
 [23] T. W. Larsen, K. D. Petersson, F. Kuemmeth, T. S. Jespersen, P. Krogstrup, J. Nygård, and C. M. Marcus, *Phys. Rev. Lett.* **115**, 127001 (2015).
 [24] M. Mergenthaler, A. Nersisyan, A. Patterson, M. Esposito, A. Baumgartner, C. Schönenberger, G. A. D. Briggs, E. A. Laird, and P. J. Leek, *arXiv:1904.10132*.
 [25] J. G. Kroll, W. Uilhoorn, K. L. van der Eenden, D. de Jong, K. Watanabe, T. Taniguchi, S. Goswami, M. C. Cassidy, and L. P. Kouwenhoven, *Nat. Commun.* **9**, 4615 (2018).
 [26] L. Casparis, M. R. Connolly, M. Kjaergaard, N. J. Pearson, A. Kringhøj, T. W. Larsen, F. Kuemmeth, T. Wang, C. Thomas, S. Gronin, G. C. Gardner, M. J. Manfra, C. M. Marcus, and K. D. Petersson, *Nat. Nanotechnol.* **13**, 915 (2018).
 [27] A. Y. Kitaev, *Phys.-Usp.* **44**, 131 (2001).
 [28] V. Mourik, K. Zuo, S. M. Frolov, S. R. Plissard, E. P. A. M. Bakkers, and L. P. Kouwenhoven, *Science* **336**, 1003 (2012).
 [29] M. T. Deng, S. Vaitiekėnas, E. B. Hansen, J. Danon, M. Leijnse, K. Flensberg, J. Nygård, P. Krogstrup, and C. M. Marcus, *Science* **354**, 1557 (2016).
 [30] R. Aguado, *Riv. Nuovo Cimento* **40**, 523 (2017).
 [31] R. M. Lutchyn, E. P. A. M. Bakkers, L. P. Kouwenhoven, P. Krogstrup, C. M. Marcus, and Y. Oreg, *Nat. Rev. Mater.* **3**, 52 (2018).
 [32] Ö. Gül, H. Zhang, J. D. S. Bommer, M. W. A. de Moor, D. Car, S. R. Plissard, E. P. A. M. Bakkers, A. Geresdi, K. Watanabe, T. Taniguchi, and L. P. Kouwenhoven, *Nat. Nanotechnol.* **13**, 192 (2018).
 [33] Y. Hu, H. O. H. Churchill, D. J. Reilly, J. Xiang, C. M. Lieber, and C. M. Marcus, *Nat. Nanotechnol.* **2**, 622 (2007).
 [34] Y. Hu, F. Kuemmeth, C. M. Lieber, and C. M. Marcus, *Nat. Nanotechnol.* **7**, 47 (2012).
 [35] A. P. Higginbotham, F. Kuemmeth, M. P. Hanson, A. C. Gossard, and C. M. Marcus, *Phys. Rev. Lett.* **112**, 026801 (2014).
 [36] A. P. Higginbotham, T. W. Larsen, J. Yao, H. Yan, C. M. Lieber, C. M. Marcus, and F. Kuemmeth, *Nano Lett.* **14**, 3582 (2014).

- [37] M. Brauns, J. Ridderbos, A. Li, E. P. A. M. Bakkers, and F. A. Zwanenburg, *Phys. Rev. B* **93**, 121408(R) (2016).
- [38] M. Brauns, J. Ridderbos, A. Li, W. G. van der Wiel, E. P. A. M. Bakkers, and F. A. Zwanenburg, *Appl. Phys. Lett.* **109**, 143113 (2016).
- [39] M. Brauns, J. Ridderbos, A. Li, E. P. A. M. Bakkers, W. G. van der Wiel, and F. A. Zwanenburg, *Phys. Rev. B* **94**, 041411(R) (2016).
- [40] A. Zarassi, Z. Su, J. Danon, J. Schwenderling, M. Hocevar, B. M. Nguyen, J. Yoo, S. A. Dayeh, and S. M. Frolov, *Phys. Rev. B* **95**, 155416 (2017).
- [41] F. N. M. Froning, M. K. Rehmann, J. Ridderbos, M. Brauns, F. A. Zwanenburg, A. Li, E. P. A. M. Bakkers, D. M. Zumbühl, and F. R. Braakman, *Appl. Phys. Lett.* **113**, 073102 (2018).
- [42] J. Xiang, W. Lu, Y. Hu, Y. Wu, H. Yan, and C. M. Lieber, *Nature (London)* **441**, 489 (2006).
- [43] Z. Su, A. Zarassi, B.-M. Nguyen, J. Yoo, S. A. Dayeh, and S. M. Frolov, [arXiv:1610.03010](https://arxiv.org/abs/1610.03010).
- [44] J. Ridderbos, M. Brauns, J. Shen, F. K. de Vries, A. Li, E. P. A. M. Bakkers, A. Brinkman, and F. A. Zwanenburg, *Adv. Mater.* **30**, 1802257 (2018).
- [45] F. K. de Vries, J. Shen, R. J. Skolasinski, M. P. Nowak, D. Varjas, L. Wang, M. Wimmer, J. Ridderbos, F. A. Zwanenburg, A. Li, S. Koelling, M. A. Verheijen, E. P. A. M. Bakkers, and L. P. Kouwenhoven, *Nano Lett.* **18**, 6483 (2018).
- [46] F. Maier, J. Klinovaja, and D. Loss, *Phys. Rev. B* **90**, 195421 (2014).
- [47] N. M. Chtchelkatchev and Y. V. Nazarov, *Phys. Rev. Lett.* **90**, 226806 (2003).
- [48] A. Zazunov, V. S. Shumeiko, E. N. Bratus', J. Lantz, and G. Wendin, *Phys. Rev. Lett.* **90**, 087003 (2003).
- [49] C. Padurariu and Y. V. Nazarov, *Phys. Rev. B* **81**, 144519 (2010).
- [50] C. Janvier, L. Tosi, L. Bretheau, Ç. Ö. Girit, M. Stern, P. Bertet, P. Joyez, D. Vion, D. Esteve, M. F. Goffman, H. Pothier, and C. Urbina, *Science* **349**, 1199 (2015).
- [51] D. J. van Woerkom, A. Proutski, B. van Heck, D. Bouman, J. I. Väyrynen, L. I. Glazman, P. Krogstrup, J. Nygård, L. P. Kouwenhoven, and A. Geresdi, *Nat. Phys.* **13**, 876 (2017).
- [52] M. Hays, G. de Lange, K. Serniak, D. J. van Woerkom, D. Bouman, P. Krogstrup, J. Nygård, A. Geresdi, and M. H. Devoret, *Phys. Rev. Lett.* **121**, 047001 (2018).
- [53] L. Tosi, C. Metzger, M. F. Goffman, C. Urbina, H. Pothier, S. Park, A. L. Yeyati, J. Nygård, and P. Krogstrup, *Phys. Rev. X* **9**, 011010 (2019).
- [54] C. Kloeffel, M. Trif, and D. Loss, *Phys. Rev. B* **84**, 195314 (2011).
- [55] A. P. Higginbotham, F. Kuemmeth, T. W. Larsen, M. Fitzpatrick, J. Yao, H. Yan, C. M. Lieber, and C. M. Marcus, *Phys. Rev. Lett.* **112**, 216806 (2014).
- [56] K. M. Itoh, J. Kato, M. Uemura, A. K. Kaliteevskii, O. N. Godisov, G. G. Devyatych, A. D. Bulanov, A. V. Gusev, I. D. Kovalev, P. G. Sennikov, H.-J. Pohl, N. V. Abrosimov, and H. Riemann, *Jpn. J. Appl. Phys.* **42**, 6248 (2003).
- [57] M. Kuhlmann, U. Zimmermann, D. Dikin, S. Abens, K. Keck, and V. M. Dmitriev, *Z. Phys. B* **96**, 13 (1994).
- [58] K. Flensberg and J. B. Hansen, *Phys. Rev. B* **40**, 8693 (1989).
- [59] J. Ridderbos, M. Brauns, J. Shen, F. K. de Vries, A. Li, S. Kölling, M. A. Verheijen, A. Brinkman, W. G. van der Wiel, E. P. A. M. Bakkers, and F. A. Zwanenburg, [arXiv:1907.05510](https://arxiv.org/abs/1907.05510).
- [60] W. C. Stewart, *Appl. Phys. Lett.* **12**, 277 (1968).
- [61] X. Du, I. Skachko, and E. Y. Andrei, *Phys. Rev. B* **77**, 184507 (2008).
- [62] J. Xiang, A. Vidan, M. Tinkham, R. M. Westervelt, and C. M. Lieber, *Nat. Nanotechnol.* **1**, 208 (2006).
- [63] J. H. Davies, *The Physics of Low-dimensional Semiconductors* (Cambridge University Press, New York, 1998).
- [64] S. Conesa-Boj, A. Li, S. Koelling, M. Brauns, J. Ridderbos, T. T. Nguyen, M. A. Verheijen, P. M. Koenraad, F. A. Zwanenburg, and E. P. A. M. Bakkers, *Nano Lett.* **17**, 2259 (2017).
- [65] F. Maier, T. Meng, and D. Loss, *Phys. Rev. B* **90**, 155437 (2014).
- [66] D. J. Griffiths, *Introduction to Quantum Mechanics* (Cambridge University Press, Cambridge, UK, 1996).
- [67] H. A. Nilsson, P. Samuelsson, P. Caroff, and H. Q. Xu, *Nano Lett.* **12**, 228 (2012).
- [68] M. R. Buitelaar, W. Belzig, T. Nussbaumer, B. Babić, C. Bruder, and C. Schönenberger, *Phys. Rev. Lett.* **91**, 057005 (2003).
- [69] K. Flensberg, J. B. Hansen, and M. Octavio, *Phys. Rev. B* **38**, 8707 (1988).
- [70] A. V. Galaktionov and A. D. Zaikin, *Phys. Rev. B* **65**, 184507 (2002).
- [71] G. E. Blonder, M. Tinkham, and T. M. Klapwijk, *Phys. Rev. B* **25**, 4515 (1982).
- [72] K. Senapati, M. G. Blamire, and Z. H. Barber, *Nat. Mater.* **10**, 849 (2011).
- [73] K. Kajimura and H. Hayakawa, *Advances in Superconductivity III: Proceedings of the 3rd International Symposium on Superconductivity (ISS '90), 1990, Sendai* (Springer, Japan, 2012), p. 1320.
- [74] S. Shapiro, A. R. Janus, and S. Holly, *Rev. Mod. Phys.* **36**, 223 (1964).
- [75] R. Gross and A. Marx, *Applied Superconductivity* (Springer, New York, 2005), Vol. 1, p. 480.
- [76] P. Russer, *J. Appl. Phys.* **43**, 2008 (1972).