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1 **CFD and EnKF coupling estimation of LNG leakage and dispersion**

2 **Abstract:** As a kind of clean fuel, increasing quantities of natural gas have been
3 transported as liquefied natural gas (LNG) worldwide. The safety of LNG storage has
4 gained the concerns from the public due to the potential severe consequences that may
5 arise from LNG leakage. In this paper, a three-dimensional model with the combination
6 of computational fluid dynamics (CFD) and the ensemble Kalman filter (EnKF) is
7 proposed to predict LNG vapor dispersion and estimate the strength of the LNG leakage
8 source. The LNG vapor dispersion CFD model is validated by the experimental data
9 with good feasibility, and is further demonstrated with the reasonable modeling of the
10 characteristics of the LNG vapor dispersion in a typical receiving terminal. The
11 effectiveness of the proposed CFD and EnKF coupling model is evaluated and validated
12 by a twin experiment. The results of the twin experiment indicate that the proposed
13 CFD and EnKF coupling model allows the integration of observation data into the CFD
14 simulations to enhance the prediction accuracy of the LNG vapor spatial-temporal
15 distribution and thereby realizing a reasonable estimation of the LNG leakage velocity
16 under complex environments. This study can provide technical supports for safety
17 control, loss prevention and emergency response in case of LNG leakage accidents.

18 **Keywords:** LNG leakage; LNG vapor dispersion; LNG receiving terminal;
19 computational fluid dynamics; ensemble Kalman filter

1 **CFD and EnKF coupling estimation of LNG leakage and dispersion**

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1 **CFD and EnKF coupling estimation of LNG leakage and dispersion**

2 **1. Introduction**

3 The Liquefied Natural Gas (LNG) industry has attracted a lot of attention in the
4 past few decades due to the increasing demand for clean energy all over the world. LNG
5 receiving terminals that are equipped with large cryogenic storage tanks are regarded
6 as an ideal way to satisfy the energy storage and energy supply ([Lee et al., 2012](#); [Li et
7 al., 2012](#)). As a kind of flammable and cryogenic gas, leaked LNG vapor could become
8 a gas cloud rapidly because of the mass heat exchange with the atmospheric
9 environment. There are possibilities of causing catastrophic consequences induced by
10 the LNG tank leakage, such as cryogenic burns, fires, explosions, and so on. When
11 serious LNG leakage accidents occur, the flammable gas cloud that formed by mixing
12 natural gas and air could be driven by the ambient wind for several kilometers, which
13 will pose serious threats to the human health and safety, and the environment.
14 Meanwhile, the leaked LNG vapor will be driven by the negative buoyancy force
15 because of the low temperature of LNG vapor at the initial stage of LNG leakage, which
16 will aggravate the dangerous area ([Pontiggia et al., 2009](#)). As a result, the characteristics
17 of LNG vapor dispersion, the prediction of the LNG vapor distribution and the
18 estimation of the strength of the leakage source after LNG leakage have been a research
19 focus in the past decade, which is of great significance for the loss prevention, safety
20 control and emergency response of LNG leakage accidents.

21 In the early years, there were some studies investigating LNG spill accidents,
22 which mainly focused on the field tests at relatively open terrains ([Burro Series Data](#)
23 [Report,1982](#); [Coyote Series Data Report, 1983](#); [Falcon Series Data Report, 1990](#)).
24 These experiments analyzed the process and characteristics of the LNG spilling on
25 water and spreading with the ambient wind. Meanwhile, some Computational Fluid
26 Dynamics (CFD) models have been developed for LNG spilling and dispersion
27 simulation. Based on Coyote series experiments, Sklavounos et al. presented a
28 comparison between ANSYS CFX and two popular box-models (SLAB and DEGADIS)
29 by using statistical performance measures ([Sklavounos et al., 2006](#)). [Cormier et al.](#)
30 ([Cormier et al., 2009](#)) and [Qi et al. \(Qi et al., 2010\)](#) employed the Brayton Fire Training
31 Field (BFTF) experimental data to validate the ANSYS CFX code. Then, the process
32 of LNG leakage and dispersion at a large pit with the consideration of the effects of
33 dike wall/fence and the sensitivity analysis of several key parameters were investigated
34 as well. The results indicated that the ANSYS CFX could obtain a good performance
35 in the simulation of non-isothermal gas dispersion. What's more, the multi-phase of the
36 LNG leakage process was taken into consideration in the previous studies. [Giannissi et](#)
37 [al. proposed a two-phase jet model, which could realize the simulation of LNG vapor](#)
38 [dispersion and LNG liquid pool spreading simultaneously, and the Falcon series](#)
39 [experiments were selected to validate the proposed two-phase model with good](#)
40 [reliability \(\[Giannissi et al., 2013\]\(#\)\)](#). Additionally, the ANSYS FLUENT with the
41 combination of the Lee model was proposed to simulate the LNG multi-phase

42 transformation process, which well predicted the peak value of LNG vapor compared
43 with the Falcon series experimental data and other numerical models (Luo et al., 2018).
44 However, the above studies mainly focused on the evaluation of the proposed CFD
45 models by simplified experiments data without the consideration of the realistic
46 complex layouts of a real LNG storage site. By contrast, Sun et al. (Sun et al., 2013)
47 studied the LNG spill accident at an LNG station by using ANSYS FLUENT and
48 assessed the risk of an LNG spill accident with the consideration of the influence of
49 dyke walls. Similarly, Guo et al. utilized the Burro series test to evaluate the
50 applicability of the Fluidyn-PANACHE code, and the effects of the atmosphere stability
51 on the LNG vapor dispersion were discussed (Guo et al., 2019). Baalisampanga et al.
52 (Baalisampanga et al., 2019) and Dasgotra et al. (Dasgotra et al., 2018) studied the LNG
53 spilling accident using FLACS considering its cascading consequences, and the results
54 showed that the integrated consequences were more severe.

55 However, there are always some uncertainties about the parameters of the LNG
56 leakage source and dispersion process, which could bring a certain degree of errors to
57 the simulation results. The LNG leakage rate and the ambient wind speeds under
58 complex environments are difficult to estimate, which could result in a large deviation
59 between simulation results and the real situations. Moreover, the estimation of LNG
60 vapor leakage rate is of significance to provide technical supports for emergency
61 response. The estimation of hazardous materials leakage source has been investigated
62 by many studies. The data assimilation (DA) method is proven with good reliability

63 and practicability to estimate the strength of the leakage source and predict the
64 hazardous materials spatio-temporal distribution (Zhang et al., 2014; Xue et al., 2018;
65 Wu et al., 2018; Yuan et al., 2019). As a kind of sequential DA method, the ensemble
66 Kalman filter (EnKF) method is widely used in the prediction of hazardous materials
67 dispersion and with good feasibility to reconstruct hazardous materials release source
68 by integrating observation data into the dispersion models (Zhang et al., 2014; Yuan et
69 al., 2019). These studies demonstrate that the DA method and the ensemble Kalman
70 filter have great potentials in the prediction of LNG vapor dispersion and to realize the
71 estimation of the strength of the LNG vapor leakage source.

72 In this study, a three-dimensional [CFD and EnKF coupling model](#) is proposed to
73 estimate the LNG leakage and predict the LNG dispersion process. An OpenFOAM
74 solver is improved to simulate the LNG vapor dispersion process, and the EnKF method
75 is used to integrate the observation data into the OpenFOAM simulations and realize
76 the estimation of the leakage source at the same time. Firstly, the OpenFOAM solver
77 for simulating LNG vapor dispersion was evaluated and validated by using the Burro 8
78 spill test data. Furthermore, scenario analysis of LNG vapor leakage in an LNG
79 receiving terminal located in the north of China is conducted to investigate the
80 characteristics of LNG vapor dispersion in complex environments. Finally, a twin
81 experiment is done to evaluate and validate the proposed [CFD and EnKF coupling](#)
82 [model](#) through quantitative and qualitative analysis. This study could be helpful to
83 provide technical supports for safety control and emergency response of LNG leakage

84 accidents.

85 **2. Methodology**

86 **2.1 Governing equations of LNG vapor dispersion**

87 In this study, a three-dimensional compressible Navier-Stokes solver based on
88 OpenFOAM is employed to simulate LNG vapor leakage and dispersion. This solver
89 has been validated with feasibility and effectiveness in the simulation of gravity-driven
90 gas flows (Fiates et al., 2016; Mack and Spruijt, 2013). In this paper, only the mass
91 conservation equation, momentum conservation equation and no-reaction species
92 mass-conservation equation are utilized, because there is no chemical reaction during
93 the LNG vapor leakage and dispersion process. The basic governing equations of LNG
94 vapor dispersion can be expressed as follows:

95 (i) Mass conservation equation

$$96 \quad \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \quad (1)$$

97 (ii) Momentum conservation equation

$$98 \quad \frac{\partial}{\partial t}(\rho \mathbf{v}) + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) = -\nabla p + \nabla \tau + \rho \mathbf{g} + \mathbf{F} \quad (2)$$

99 (iii) Species mass-conservation equation

$$100 \quad \frac{\partial}{\partial t}(\rho Y_i) + \nabla \cdot (\rho \mathbf{v} Y_i) = \nabla \cdot (D_c \nabla (\rho Y_i)) + S_i \quad (3)$$

101 where ρ is the density of the mixed gas, \mathbf{v} is the velocity, p presents the pressure, and
102 τ is the shear stress, which can be calculated according to the law of viscosity. \mathbf{g} and

103 \mathbf{F} present the gravity acceleration and the external forces respectively, and Y_i
 104 represents the volume concentration of different species. D_c represents the diffusion
 105 coefficient reflecting the gas diffusion degree and S_i represents the generalized source
 106 term.

107 2.2 Turbulence Model

108 The typical κ - ε turbulence model is widely applied in the CFD simulation of gas
 109 dispersion due to its stability and accurate prediction (Liu et al., 2018; Siddiqui et al.,
 110 2012). However, the standard κ - ε turbulence model has some shortages in handling
 111 fluid on the curved surface or even more complex flows. Therefore, the SST turbulence
 112 model was employed in this study that is a promising turbulence model in the
 113 simulation of gravity-driven gas flow with the combination of the advantages of the
 114 standard κ - ε model and the k - ω model (Li et al., 2016; Xing et al. 2013). The solved
 115 equations of the SST turbulence model are presented as follows:

$$116 \quad \frac{\partial(\rho k)}{\partial t} + \nabla \cdot (\rho U k) = \nabla \cdot \left[\left(u + \frac{u_t}{\sigma_\omega} \right) \nabla k \right] + P_k - \beta' \rho k \omega \quad (4)$$

$$117 \quad \frac{\partial(\rho \omega)}{\partial t} + \nabla \cdot (\rho U \omega) = \nabla \cdot \left[\left(u + \frac{u_t}{\sigma_\omega} \right) \nabla \omega \right] + \frac{\alpha \omega}{k} P_k - \beta \rho \omega^2 \quad (5)$$

$$118 \quad \mu_t = \frac{\rho k}{\omega} \quad (6)$$

119 In the equations above, β' , α , σ_k , σ_ω , and β are the model constants, which are assigned
 120 as $\beta' = 0.09$, $\alpha = \frac{5}{9}$, $\sigma_k = \sigma_\omega = 2$, $\beta = 0.075$ respectively according to a previous
 121 study (Sklavounos et al., 2006). κ means kinetic viscosity, ω represents the turbulent
 122 frequency, and P_k is the production rate of the turbulence. u_t represents turbulent

123 kinetic that can be calculated by using equation (6).

124 **2.3 Ensemble Kalman Filter**

125 The ensemble Kalman filter (EnKF) is a kind of widely-used data assimilation
126 method, which can deal with the prediction of nonlinear dynamic models. It has some
127 obvious advantages, such as consistent estimation of spatiotemporally varying model
128 covariance, ease of implementation, and estimation of the posterior error (Pu and
129 Hacker, 2009). The EnKF method has been widely used for solving many engineering
130 problems, typically, it has already been successfully applied in the hydrological model
131 prediction (Pu and Hacker, 2009; Valdes-Abellan et al., 2018), forecasting of smoke
132 movement during tunnel fires (Ji et al., 2018), prediction of the indoor environment
133 (Lin and Wang, 2013) and gas release and dispersion in an underground tunnel (Wu et
134 al., 2018; Yuan et al., 2019). Meanwhile, the [CFD and EnKF coupling model](#) is also an
135 alternative way to provide supports for the emergency of the nuclear accident (Zhang
136 et al., 2015a; Zhang et al., 2015b).

137 In this study, the basic formulas of EnKF are described as follows:

$$138 \quad y^f(t_i) = D \left(y^f(t_{i-1}) \right) \quad (7)$$

$$139 \quad y^a(t_i) = y^f(t_i) + E \left(r(t_i) - L \left(y^f(t_i) \right) \right) \quad (8)$$

140 Where y denotes the state vector, t_i and t_{i-1} represent the time step, $y^f(t_i)$ is the
141 predicted value at time t_i , $y^a(t_i)$ is the analytical value at time t_i , D and L mean the
142 nonlinear dynamic system model and the observation model respectively. r means the

143 observation vector and E denotes the ensemble Kalman gain.

144 EnKF describes the nonlinearity of the dynamic system by using a set of state

145 estimations. The state matrix is generated as follows:

$$146 \quad Y = \frac{1}{\sqrt{M-1}} (y_1, y_2, \dots, y_M) \quad (9)$$

$$147 \quad Y' = \frac{1}{\sqrt{M-1}} (y_1 - \bar{y}, y_2 - \bar{y}, \dots, y_M - \bar{y}) \quad (10)$$

$$148 \quad Q_e = Y'Y'^T \quad (11)$$

149 Where Y represents the state matrix, M is the ensemble size. Q_e denotes the ensemble

150 covariance matrix, which is generated by the state ensemble. The ensemble Kalman

151 gain and the prediction of the observation vector are calculated as follows:

$$152 \quad r^f = L(y^f) \quad (12)$$

$$153 \quad E = Q_e^f L^T (LQ_e^f L^T + Z_e)^{-1} \quad (13)$$

154 Where r^f means the prediction of the observation vector, and Z_e denotes the

155 observation ensemble covariance matrix, which can be given as follows:

$$156 \quad R = (r_o + \varepsilon_1 \dots r_o + \varepsilon_n \dots r_o + \varepsilon_M) \quad (14)$$

$$157 \quad R' = (\varepsilon_1 \dots \varepsilon_n \dots \varepsilon_M) \quad (15)$$

$$158 \quad Z_e = R'R'^T \quad (16)$$

159 Where ε_n is the pseudo-random perturbation. R indicates an ensemble of observation,

160 which can be obtained by adding ε_n to the observation data r_o . Z_e represents the

161 covariance matrix of R' .

162 2.4 State vector and update of source term

163 In this paper, the state vector consists of the LNG vapor concentrations and the
164 leakage velocities:

$$165 \quad y = (c_1 \dots c_i \dots c_n \quad l_1 \dots l_j \dots l_m)^T \in R^{n+m} \quad (17)$$

166 Where y denotes the state vector, c means the concentration of the LNG vapor and l
167 means the LNG vapor leakage velocity at the leak hole. The subscript n and m represent
168 the number of LNG vapor concentrations and the number of data assimilation time steps
169 respectively.

$$170 \quad l_j^b = \sum_{i=1}^N l_{j-1}^a(i) / M \quad (18)$$

$$171 \quad l_j^f(i) = l_j^b + \delta l_j^b(i), \quad i = 1, 2, \dots, M \quad (19)$$

172 Where l_{j-1}^a means the latest updated leakage velocity ensemble, i and M represent the
173 ensemble member and ensemble size respectively. The ensemble l_1^f is the first-guess
174 leakage velocity, which can be initialed by the users. l_j^f represents a prior gas leakage
175 velocity for the j -th data assimilation, which are automatically calculated according to
176 the formulas (19). The added noise $\delta l_j^b(i)$ is generated as follows:

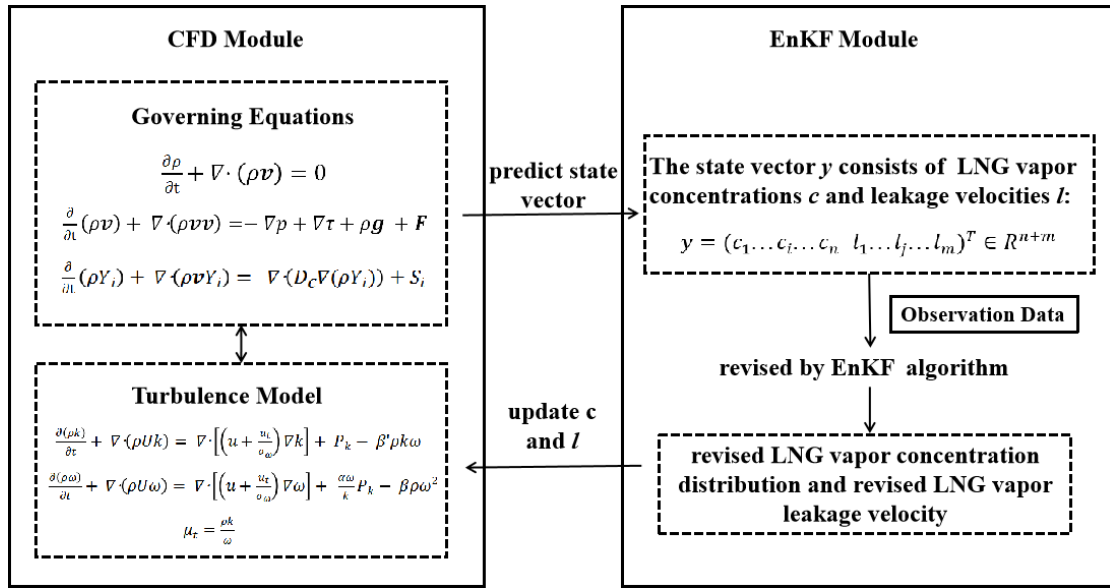
$$177 \quad \delta l_j^b(i) = \alpha \delta l_{j-1}^a(i) + \sqrt{1 - \alpha^2} c_j(i) \sigma_{j-1}^a, \quad i = 1, 2, \dots, M \quad (20)$$

178 Where $\delta l_{j-1}^a(i)$ denotes the deviation between the i -th analysis leakage velocity
179 and the ensemble mean σ_{j-1}^a represents the standard deviation, which is calculated by

180 l_{j-1}^a . $c_j(i)$ is random numbers, which following the Gaussian distribution $N(0,1)$. The
 181 parameter α (range from 0 to 1) controls the degree to which the influence of the prior
 182 state will be retained, which can be set as 0.99 in this paper.

183 2.5 CFD and EnKF coupling model for leakage source estimation and dispersion 184 prediction

185 With the combination of LNG vapor dispersion model and EnKF algorithm, the
 186 CFD and EnKF coupling model for LNG vapor leakage source estimation and
 187 dispersion prediction are developed by the procedure shown in Fig. 1.



188
 189 Fig. 1 Framework of the CFD and EnKF coupling model for LNG vapor leakage
 190 source estimation and dispersion prediction

191 The CFD and EnKF coupling model for leakage source estimation and dispersion
 192 prediction consists of the CFD module and the EnKF module. The CFD module is
 193 operated to simulate the LNG vapor dispersion process through the calculations of

194 governing equations and turbulence model. Meanwhile, the state vector of the EnKF
195 module, which consists of LNG vapor concentrations and the leakage velocities in the
196 leak hole can be predicted by the CFD module calculation. When the observation data
197 is available, the state vector can be revised by the EnKF algorithm and the updates of
198 the LNG vapor concentrations and the LNG vapor leakage velocities can be realized.
199 Finally, the revised LNG vapor concentration distribution and the revised LNG vapor
200 leakage velocity will be utilized into the CFD module for the next calculation of LNG
201 vapor dispersion and a data assimilation step is finished.

202 **3. Results and discussion**

203 This section is organized as follows: Firstly, as a coupling model consisting of the
204 CFD model and the EnKF algorithm, the feasibility of the CFD and EnKF coupling
205 model can only be guaranteed after the validation of the CFD model. Therefore, the
206 OpenFOAM-based CFD model was evaluated by experimental data firstly and then a
207 case study was investigated as well to analyze the basic characteristics of the LNG
208 vapor dispersion. Finally, the effectiveness of the proposed CFD and EnKF coupling
209 model was demonstrated by a twin experiment.

210 **3.1 Evaluation and validation of OpenFOAM code**

211 As a kind of open-source CFD computing platform, OpenFOAM gained
212 popularity in engineering system and scientific research. However, it has not been
213 validated in a specific scenario associated with an LNG spill and vapor dispersion.

214 Moreover, the validation of the OpenFOAM code in the simulation of LNG vapor
215 leakage and dispersion is of significance to the development of the [CFD and EnKF](#)
216 [coupling model](#) LNG vapor leakage and dispersion prediction model, and it is also
217 beneficial to provide an alternative tool for the investigation of LNG leakage and
218 dispersion by numerical simulations. In this paper, the experimental data, the results of
219 ANSYS FLUENT code and the results of the OpenFOAM code will be compared to
220 validate the applicability of the OpenFOAM simulations.

221 3.1.1 Numerical configurations

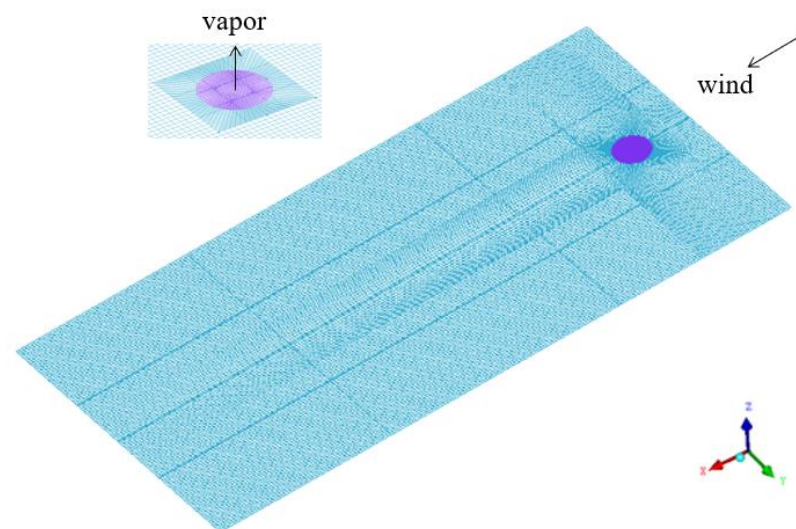
222 The Burro 8 spill test performed by the Lawrence Livermore National Laboratory
223 (LLNL) at the Naval Weapons Center was considered appropriate enough to investigate
224 the behaviors and the characteristics of the LNG vapor dispersion due to its stable
225 atmospheric conditions ([Sun et al., 2013](#)). In the Burro 8 test, the LNG vapor spread
226 from a pond with a diameter of 58 m into the atmosphere environment. There were 25
227 gas sensor sites arranged downwind from the center of pond. 20 wind-filed station were
228 placed in both upwind and downwind to capture the wind velocity and the wind
229 directions. The experimental setup and the meteorological data involved in the Burro 8
230 experiment are listed in **Table.1**.

231 Table 1 Experimental setup and meteorological data involved in the Burro 8
232 experiment

Parameters	values
Spill volume (m ³)	28.4

Spill duration (s)	107
Spill rate (m ³ /min)	16
Wind speed (m/s)	1.8
Ambient Temperature (°C)	33.1
Relative humidity	4.5 %
Atmospheric stability class	E
Monin-Obukhov length (m)	16.5

233 The computational domain used in the OpenFoam simulation was
 234 1000_m×500_m×50_m. ANSYS ICEM was employed to create and discretize the
 235 computational domain. The hexahedral cells with refined mesh close to the pond and
 236 ground were used and the mesh in the computational domain can be seen in **Fig.2**.



237

238

Fig.2 Mesh in the computational domain

239

240

241

According to the previous studies (Luo et al., 2018; Zhang et al., 2015), the boundary condition of velocity in the wind inlet was prescribed as uneven velocity inlet, which was calculated as follows:

242
$$U(z) = u_0 \times \left(\frac{z}{z_0}\right)^\lambda \quad (21)$$

243 where $U(z)$ is the wind velocity at the specific height z , and u_0 is the reference velocity
244 at the reference height z_0 . In the Burro 8 test, u_0 was set as 1.8 m/s and z_0 was 2 m. λ is
245 a dimensionless parameter determined by the atmospheric stability and the surface
246 roughness, which was set as 0.12 in this study. This uneven velocity inlet was added
247 into the OpenFOAM simulation by the codeFixedValue function in the OpenFOAM
248 platform.

249 Due to the rapid evaporation phenomenon when LNG is spilt on a water pond area,
250 the leakage velocity of the LNG vapor can be calculated by the formula as follows:

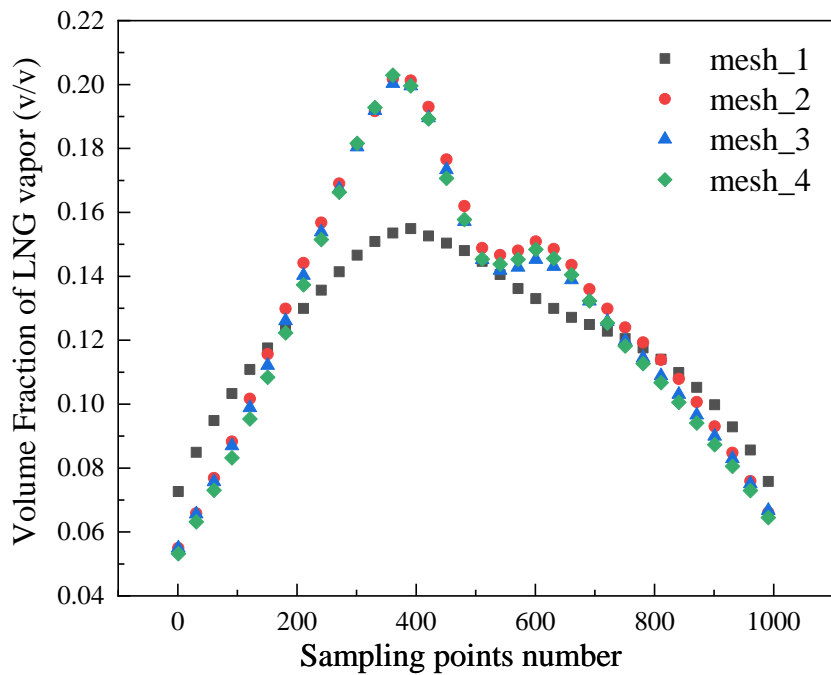
251
$$U_g = (\rho U)_{liq} / \rho_g, \quad (22)$$

252 Where U_g is the vapor leakage velocity in the computational domain, ρ_{liq} and ρ_g are
253 the LNG density (424.1 kg/m³) and the vapor density (1.76 kg/m³) at 111 K respectively.
254 U_{liq} represents LNG spill velocity, which can be calculated by the spill rate and the
255 pond diameter.

256 The outflow boundary at 900 m downwind from the origin was set as pressure
257 outlet, the top and the two sides of the computational domain were assumed far away
258 from the vapor leakage area, which were set as symmetry boundary conditions. The
259 ground was set as the wall with no-slip condition. Additionally, all the boundary
260 conditions applied in the ANSYS FLUENT simulation were set according to the
261 boundary conditions used in the OpenFOAM simulation.

262 3.1.2 Comparison and analysis

263 In order to obtain the mesh-independent simulation results, the mesh independence
264 analysis was investigated by using four different meshes with grid numbers of 400
265 thousand, 550 thousand, 700 thousand and 850 thousand. Some sampling points
266 obtained from a sampling line were selected to perform this mesh sensitivity analysis.
267 The results of the calculated volume fraction of the LNG vapor at the sampling points
268 by using four different meshes are shown in **Fig.3**. With the comparison between the
269 results calculated by a different mesh, the average relative error and max error between
270 mesh_1 and mesh_2 are 0.12 and 0.31 respectively. However, the average relative error
271 and max error between mesh_2 and mesh_3 are 0.023 and 0.045 while 0.018 and 0.042
272 for mesh_3 and mesh_4. Therefore, mesh_2 was selected for the following simulation
273 with both good accuracy and less computation load.



274

275

Fig.3 LNG vapor volume fraction at sampling line

276

Fig.4 presents the horizontal concentration distribution of the LNG vapor at the

277

height of 1 m after LNG spilling. It shows the LNG vapor contours of 1%, 2%, 5%,

278

10%, 15%, 25%, and 35% volume fraction. The results show that a gravity-driven gas

279

cloud moved downwind as time goes by under the stable atmosphere stability in the

280

Burro 8 test. Furthermore, the shapes of the gas cloud obtained from the field test have

281

less symmetry about the center-line of the computational domain compared with the

282

simulation results. The reason for this may be that there was a non-uniform wind speed

283

in different directions existing in the field test, which was ignored in the CFD

284

simulations. However, the lateral and downwind range of the vapor dispersion of the

285

OpenFOAM code results was in a good agreement with the field test and the ANSYS

286

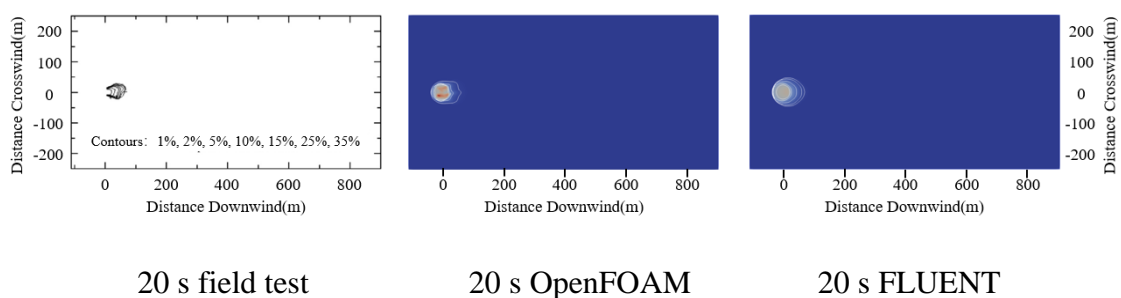
FLUENT simulation, which demonstrates that the OpenFOAM code well reproduced

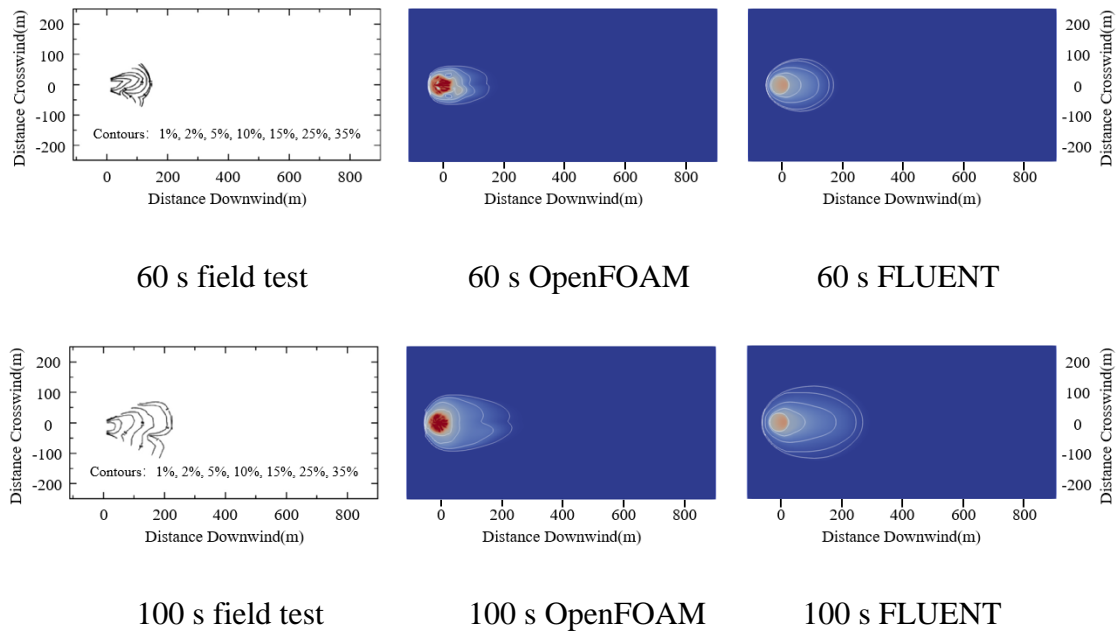
287

the distribution of the LNG vapor dispersion and can be used as an alternative tool for

288

LNG vapor dispersion with good reliability.





289 Fig.4 LNG vapor contours at olume fraction of 1%, 2%, 5%, 10%, 15%, 25%, and
 290 35%

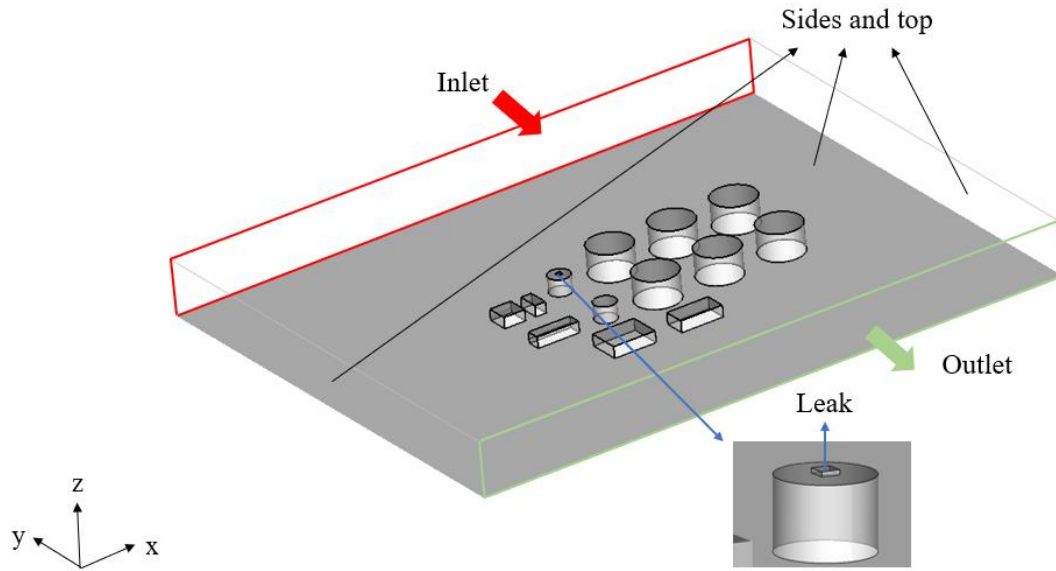
291 3.2 LNG vapor dispersion in receiving terminal

292 Different from the experimental data investigated above, the LNG vapor
 293 dispersion process in the LNG receiving terminal will be influenced by complex
 294 obstacle layouts, ambient ventilation conditions, buoyancy forces and so on. In order to
 295 investigate the LNG vapor cloud dispersion in receiving terminal at ports, a typical
 296 LNG receiving terminal located in the north of China was selected as simulation
 297 scenario in this section.

298 3.2.1 Numerical configurations of LNG port model

299 In this section, the computational domain has a dimension of
 300 1120_m×880_m×100_m, and the leakage hole is placed at the center of the
 301 computational domain. The layout and the boundary conditions of the investigated

302 LNG receiving terminal model are shown in **Fig.5**. Meanwhile, the detailed parameters
 303 of the LNG receiving terminal model are presented in **Table.2**.



304

305 Fig.5 The layout and boundary conditions of the investigated LNG receiving
 306 terminal at ports

307 Table 2 Configurations of the investigated LNG receiving terminal model

Parameter	value
Width (m)	220
Height (m)	50
Length (m)	280
Average flow speed in inlet (m/s)	8
Leakage area (m ²)	64
Leakage velocity of LNG (m/s)	15
Location of leakage source (m)	(500 m, 20 m, 32 m)
Environment temperature (K)	298
Density of LNG at the leak hole (kg/m ³)	1.76

308 The computational domain above was created and discretized by using ANSYS
309 ICEM. Three meshes with different grids (20 thousand, 40 thousand, and 60 thousand)
310 were used for primary simulations and comparisons. It showed that there was a small
311 average relative error that was 0.048 between the results of mesh_2 with 40 thousand
312 grids and mesh_3 with 60 thousand grids. However, the errors between the results of
313 mesh_2 and mesh_1 with 20 thousand grids can not be ignored, being 0.20. Therefore,
314 mesh_2 was selected for the following simulations with better accuracy and computing
315 speed. Moreover, a wind field under steady-state was calculated and initialed in the
316 simulation of LNG vapor leakage and dispersion in the LNG receiving terminal in order
317 to ensure a more realistic leakage scenario.

318 The boundary conditions applied in the simulation are shown as follows:

319 (i) Inlet: A power law correlation velocity was utilized in the air inlet boundary,
320 which was calculated by formula (21). And the z_0 and u_0 were set as 3 m/s and 2 m
321 respectively according to the meteorological records of northern China. Additionally,
322 the λ was set as 0.4 with consideration of the layout of the complex buildings.

323 (ii) Leak: The leakage velocity of the LNG vapor was set as 15 m/s under the
324 assumption that the LNG was easy to evaporate and accumulate in the higher part of
325 the storage tank. The temperature of the leaked LNG vapor at the leak hole was set as
326 111 K.

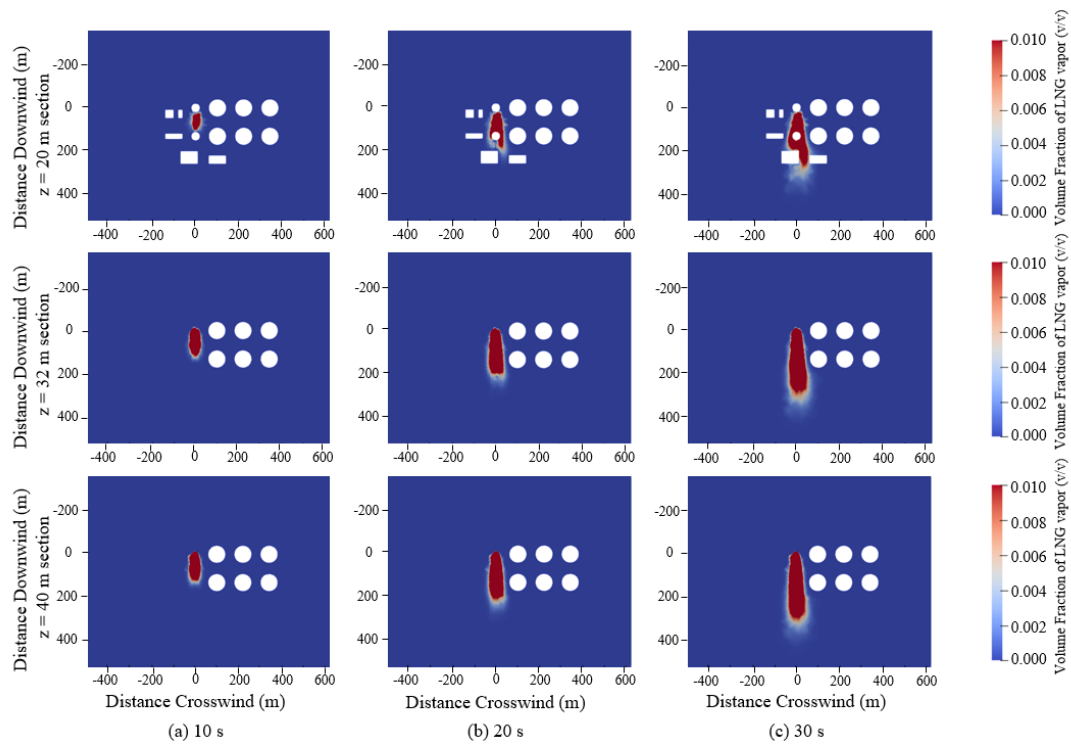
327 (iii) Outlets: The fully developed condition was employed in the outlets as outflow
328 conditions.

329 (iv) Sides and top: Two sides and the top of the computational domain were
330 defined as symmetry conditions.

331 (v) Walls: All the walls and blocks in the investigated model were set as no-slip
332 wall conditions.

333 **3.2.2 LNG vapor dispersion analysis**

334 The simulation of LNG vapor leakage and dispersion in the LNG receiving
335 terminal at ports was presented to investigate the characteristics of the LNG cloud
336 dispersion. Due to the high molecular weight, the low temperature, and the presence of
337 the aerosols, some released materials usually have the density that is heavier than the
338 ambient gas and will be driven by the gravity (Pontiggia et al., 2009). The LNG vapor
339 usually leaked and dispersed as dense gas at the initial stage before the temperature rose
340 because of the cryogenic storage condition. However, with the exchange of heat
341 between leaked LNG vapor and the surrounding atmospheric environment, the leaked
342 LNG vapor will be heated and behave like light gas gradually. Therefore, the leakage
343 and dispersion process of the LNG vapor is complex, especially in the environment
344 with some obstacles, which increases the complexity of the airflow. In this section, the
345 horizontal and vertical distributions of the LNG vapor are presented in **Fig.6** and **Fig.7**.



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Fig.6 Horizontal concentration distribution of LNG vapor at Z=20 m, Z=32 m and Z=40 m sections

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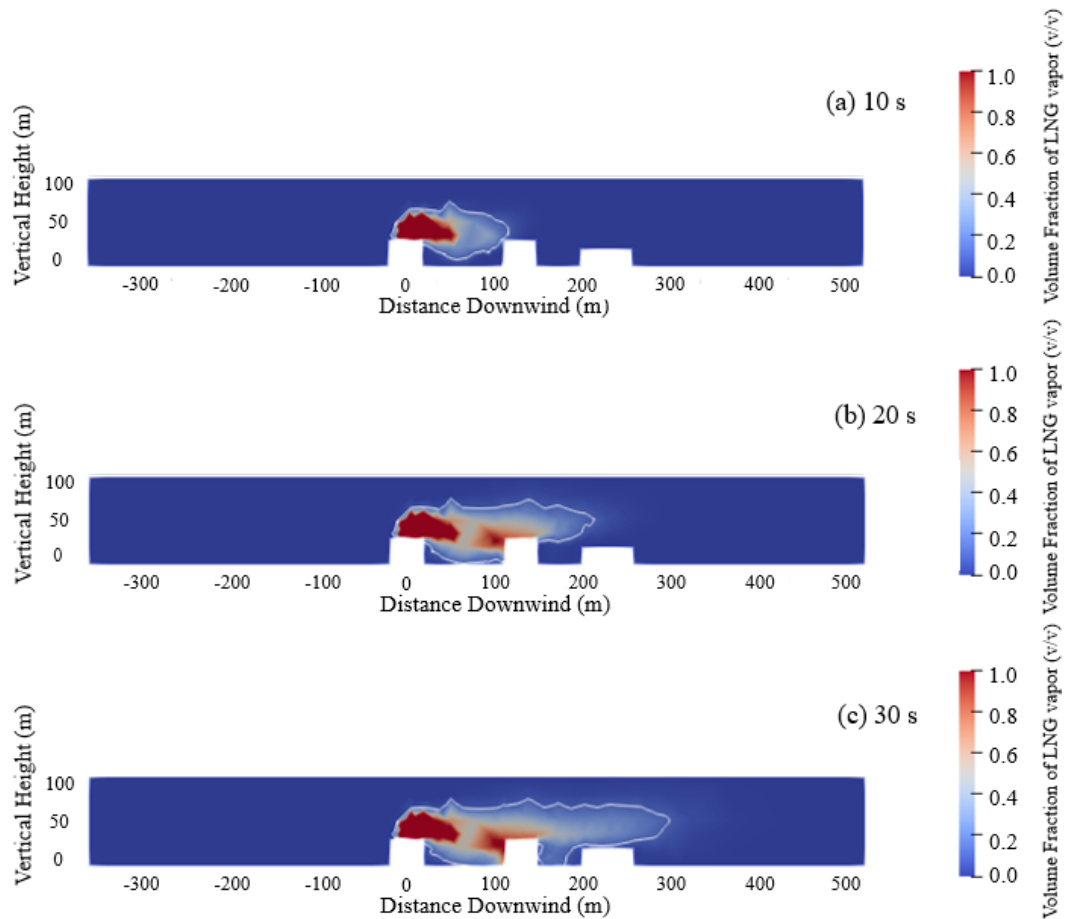
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Fig.6 compares the horizontal concentration distributions of the LNG vapor at different horizontal section heights (Z=20 m, Z=32 m and Z=40 m) at 10 s, 20 s and 30s. The range of the leaked LNG vapor in the Z=20 m section was smaller than the Z=32 m and Z=40 m sections due to the delay of the LNG vapor dispersion, lower ambient wind speed and the complex obstacles. Since the effects of the obstacles could lead to a low wind velocity at the leeward side of the storage tank, there was an obvious low concentration region at 150 m downwind in the Z=20 m section at 20 s and 30 s. Whereas, the LNG vapor cloud in the Z=32 m and Z=40 m sections had similar range areas because the there was no obstacle that could influence the process of vapor cloud dispersion in the direction of wind flow. Moreover, the vapor cloud range of the z=40

359 m section was slightly greater than $z=32$ m section, and it was probably because the
360 applied pow law correlation inlet made a relatively higher wind velocity in the $z = 40$
361 m section.



362
363 Fig.7 Vertical concentration distribution of LNG vapor at X=500 m section

364 The concentration distributions of the LNG vapor in vertical section were
365 presented in the **Fig.7**. At the initial stage of LNG vapor leakage, the vapor cloud
366 dispersion was mainly dominated by the leakage velocity and the wind speed near the
367 leakage source, and then the cryogenic dense vapor cloud affected by the gravity had
368 the tendency to sink as shown in panel (a). After spreading out of leakage source area,

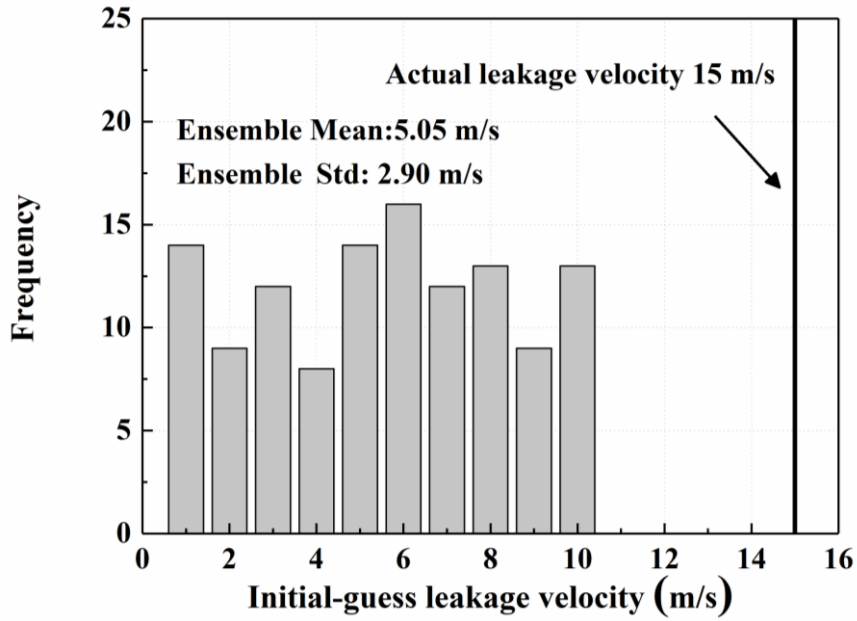
369 the buoyant force and the obstacles would have more influence on the vapor cloud
370 dispersion gradually. A conspicuous dipped trajectory of vapor cloud could be seen
371 between the first two tanks and a certain amount of LNG vapor sank into the cavity area
372 in panel (b) and panel (c). A relatively high concentration of LNG vapor could be seen
373 near the top of the second tank at 100 m downwind in panel (b) and panel (c). That was
374 because there were vortexes in the cavity area between the two tanks caused by the
375 LNG receiving terminal layout, and the similar phenomenon of vapor cloud dispersion
376 could be seen in the street canyons (Liu et al., 2018). The LNG vapor cloud continued
377 to spread to around 300 m downwind without obvious sinking trend, it was probably
378 because the density of the LNG vapor decreased gradually with the heat transfer
379 between LNG vapor cloud and the atmospheric environment. Therefore, the vapor
380 cloud dispersion process became momentum-dominated after 300 m downwind in
381 panel (c).

382 **3.3 CFD and EnKF coupling estimation of LNG leakage and dispersion**

383 In this paper, the twin experiment was used to validate the proposed CFD and
384 EnKF coupling prediction model for LNG vapor leakage and dispersion. Twin
385 experiment was widely used in the evaluation of data assimilation models (Bengtsson
386 et al., 1981, Ngodock and Carrier, 2013). There is always a control group in the twin
387 experiment, in which the numerical simulations with controlled initial parameters can
388 be used and the simulation of section 3.2 was employed as the control group in this
389 paper.

390 3.3.1 Configurations of the CFD and EnKF coupling model

391 In the CFD and EnKF coupling model, the observation sampling time step was set
392 as 0.5 s, which means the observation data from the control group will be utilized for
393 data assimilation every 0.5 s. We set up 100 observation sites in the control group
394 simulation to obtain observation data of the LNG vapor concentration. The ensemble
395 size in the CFD and EnKF coupling model was set as 120 and the inflation factor
396 (Anderson, 2007) was set as 1.0 in this paper. Additionally, two parameters with
397 uncertainties were taken into account in the proposed model: the initial-guess leakage
398 velocity and the airflow velocity in the computational domain. We set the initial-guess
399 leakage velocity as an ensemble following uniform distribution from 0 m/s to 10 m/s,
400 whereas the actual leakage velocity was 15 m/s, which is shown in Fig. 8. The u
401 ensemble calculated in the CFD and EnKF coupling model was presumed to follow a
402 normal distribution of $N(1, 0.1)$. We selected 100 observation sites in three sections of
403 the computational domain, 9 observation sites in the Z=20 m section, 70 observation
404 sites in the Z=32 m section and 21 observation sites in the X=500 m section respectively.
405 The layouts of the observation sites are shown in Fig. 9. The detailed configurations of
406 the CFD and EnKF coupling model are shown in Table 3.

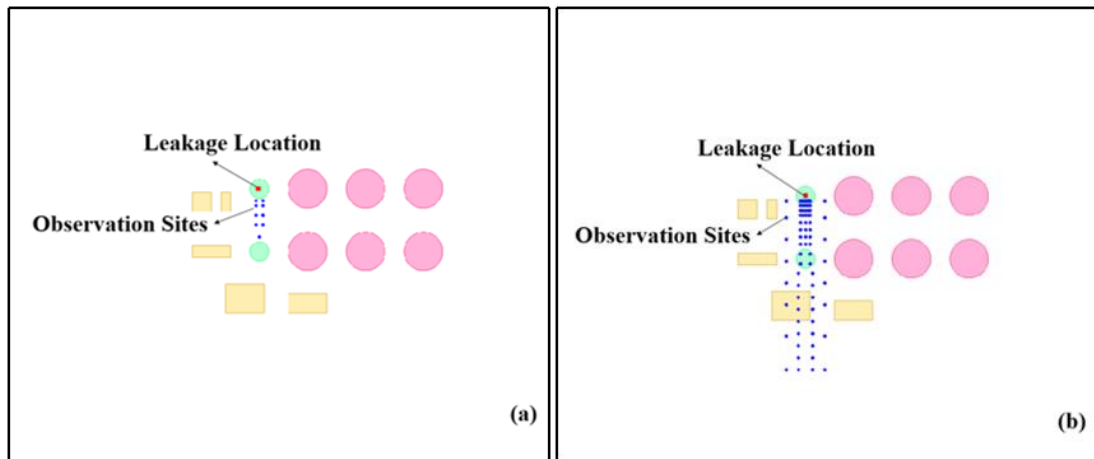


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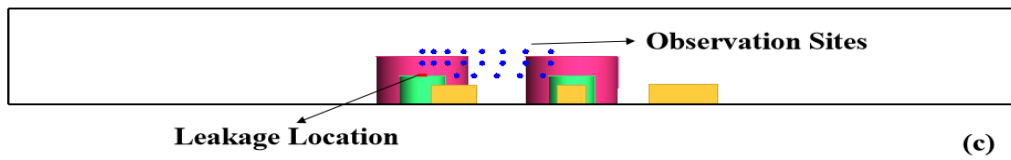
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Fig. 8. The initial-guess leakage velocity ensemble used in the [CFD and EnKF coupling model](#)



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Fig. 9. The layouts of the observation sites in three sections of the computational domain: (a) Z=20 m section, (b) Z=32 m section and (c) X=500 section

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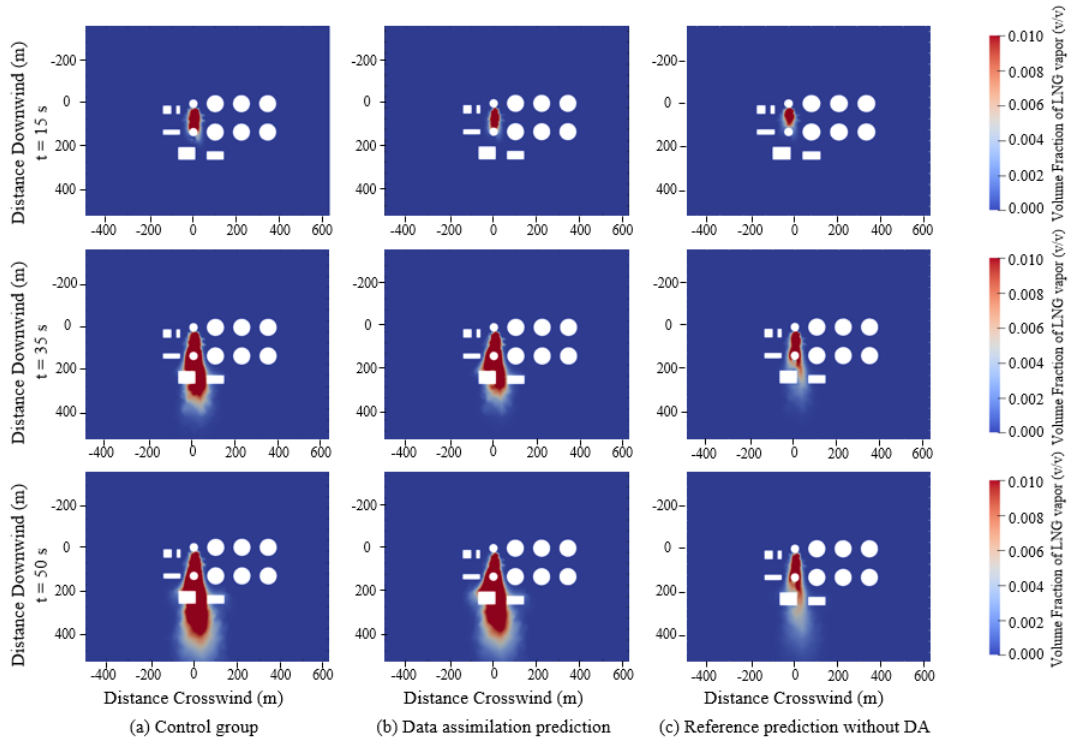
Table 3 Configurations of the [CFD and EnKF coupling model](#)

Parameter	Setup value
-----------	-------------

Ensemble number	120
Ensemble inflation	1.0
Number of measurement sites	100
Observation time interval (s)	0.5
Perturbation of velocity ensemble	$N(1, 0.1)$
Number of observation time steps	100

415 **3.3.2 Predictions of the CFD and EnKF coupling model**

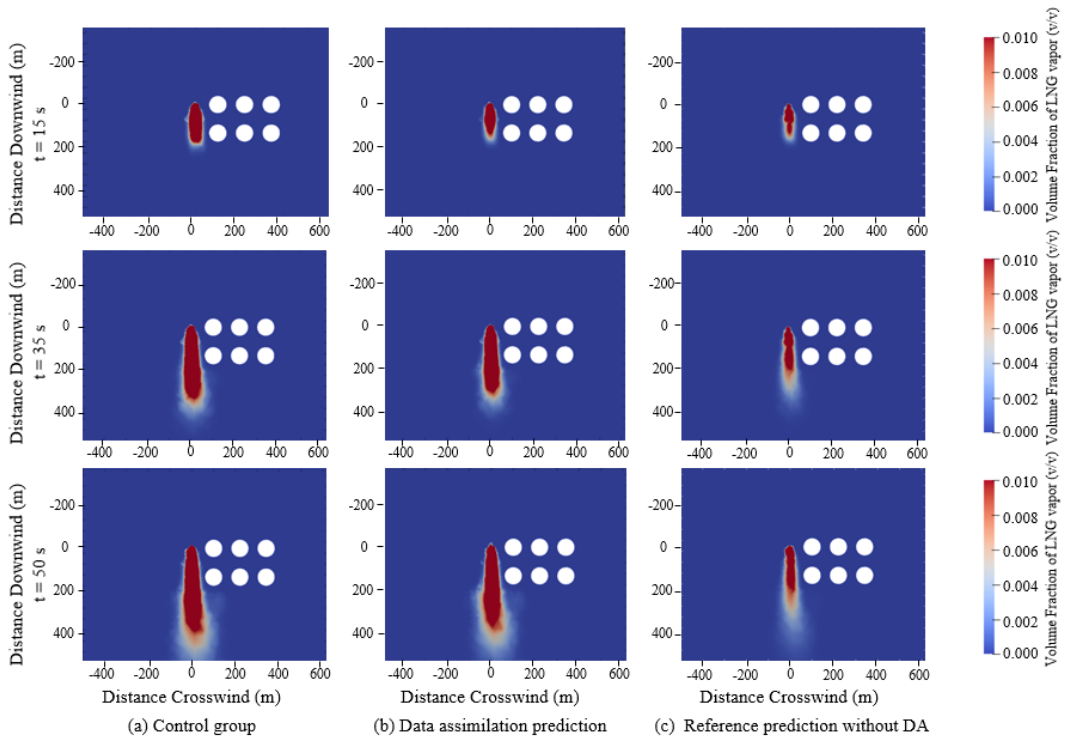
416 **Fig.10** to **Fig.12** illustrate the comparisons between the horizontal concentration
417 distributions of the LNG vapor cloud at three different sections calculated by the control
418 group, data assimilation group and a reference group without data assimilation (the
419 leakage velocity in the this group was set as 5 m/s for reference). Moreover, we
420 investigated the effectiveness of the proposed model by using three horizontal sections
421 with different numbers of observation sites, 9 observation sites in the Z=20 m section,
422 30 observation sites in the Z=32 m section and 0 observation sites in the Z=40 m section.



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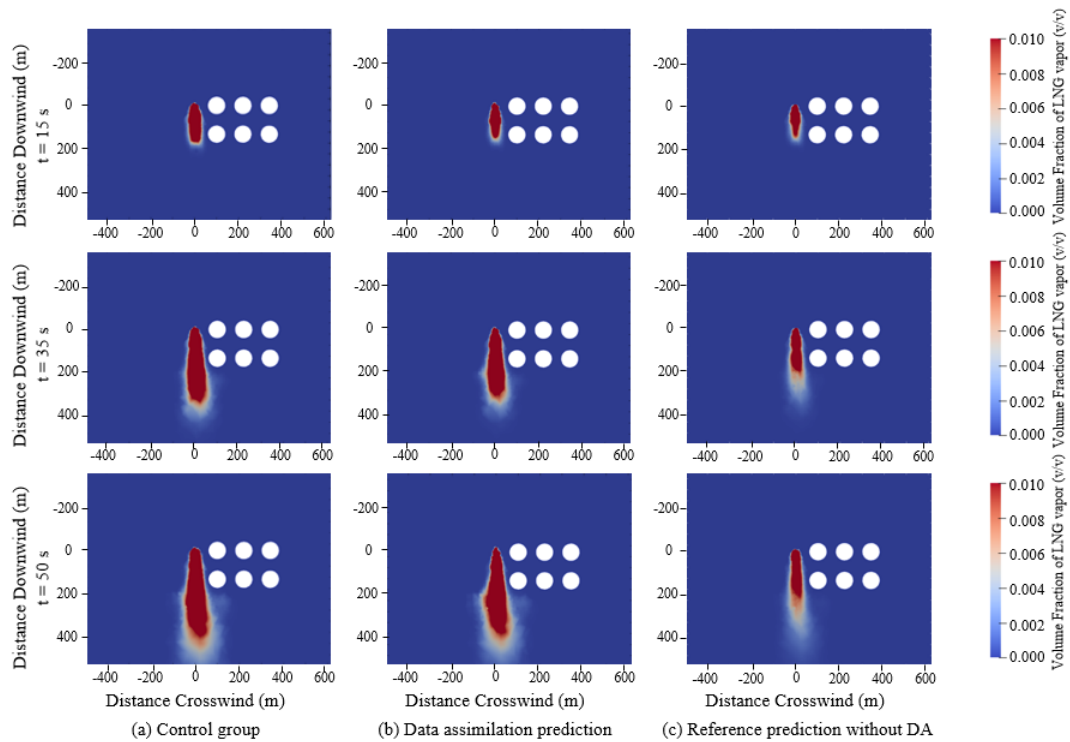
Fig.10 Horizontal concentration distribution of LNG vapor at Z=20 m section



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Fig.11 Horizontal concentration distribution of LNG vapor at Z=32 m section



427

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Fig.12 Horizontal concentration distribution of LNG vapor at Z=40 m section

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The concentration distributions of LNG vapor at three different horizontal sections

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calculated by three different simulation groups can be seen in **Fig.10** to **Fig.12**. At the

431

initial stage of vapor leakage and dispersion, there was no obvious difference of LNG

432

vapor distribution range area between the data assimilation prediction and the reference

433

prediction without DA due to the fact that the leakage velocity used in the two groups

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was similar. The LNG vapor distributions in three sections of the control group were

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slightly larger than the two predictions at 15 s because the underestimation of the

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leakage velocity in two prediction groups led to the underestimation of the LNG vapor

437

distribution area. The correlation coefficients between the data assimilation prediction

438

and the reference prediction without DA and the control group distribution at the

439

observation sites are respectively 0.93 and 0.75 at 15 s. As time goes on, the difference

440 of LNG vapor distribution between the control group and the reference prediction
441 without DA increased gradually because of the difference existing in the vapor leakage
442 velocity. However, the data assimilation group obtained the LNG vapor distribution
443 predictions with good similarities compared with the actual LNG vapor distribution in
444 the control group at 35 s and 50 s, in which the correlation coefficients between the data
445 assimilation prediction and the control group at the observation sites are 0.98 and 0.96
446 respectively. Meanwhile, the correlation coefficient between the reference prediction
447 without DA and the control group at the observation sites is only 0.48 in the end. That
448 was because the observation data were used to correct the errors in the data assimilation
449 prediction gradually and finally achieve the prediction of LNG vapor distribution with
450 relatively high accuracy by the [CFD and EnKF coupling model](#). Additionally, the LNG
451 vapor distribution predictions in the three sections calculated by the [CFD and EnKF](#)
452 [coupling model](#) were all comparable to the actual distributions in the control group,
453 which means that the [CFD and EnKF coupling model](#) could realize the correction of
454 the LNG vapor distribution in the whole computational domain even in the section
455 without observation site.

456 **Fig.13** presents the vertical concentration distribution of the LNG vapor cloud at
457 X=500 m section calculated by the control group, the data assimilation group and the
458 reference prediction group. The effectiveness of the proposed [CFD and EnKF coupling](#)
459 [model](#) in the prediction of the LNG vapor vertical distribution could also be witnessed
460 in **Fig.13**. After several data assimilation periods, the prediction of the LNG vapor

461 vertical distribution became more comparable to the actual distribution in the control
462 group by using the [CFD and EnKF coupling model](#). The correlation coefficients
463 between the data assimilation prediction and the control group at the observation sites
464 in the X=500 m section are 0.99 at 35 s and 0.98 at 50 s, which means the observation
465 data in the X=500 m section was utilized by the [CFD and EnKF coupling model](#)
466 effectively. Whereas, the reference prediction without data assimilation was quite
467 different from the actual distribution during the whole calculation period and with the
468 correlation coefficient of -0.06 in the end.

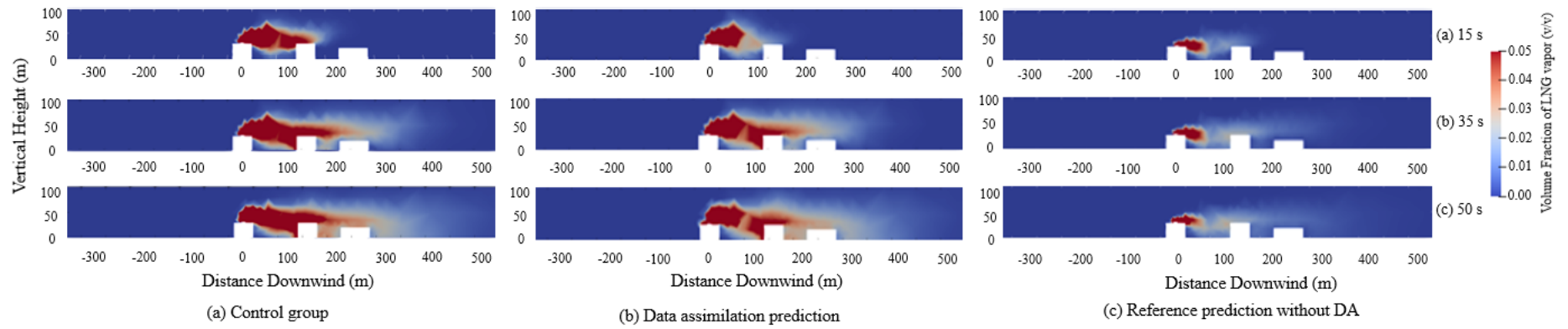


Fig.13 Vertical concentration distribution of LNG vapor at X=500 m section

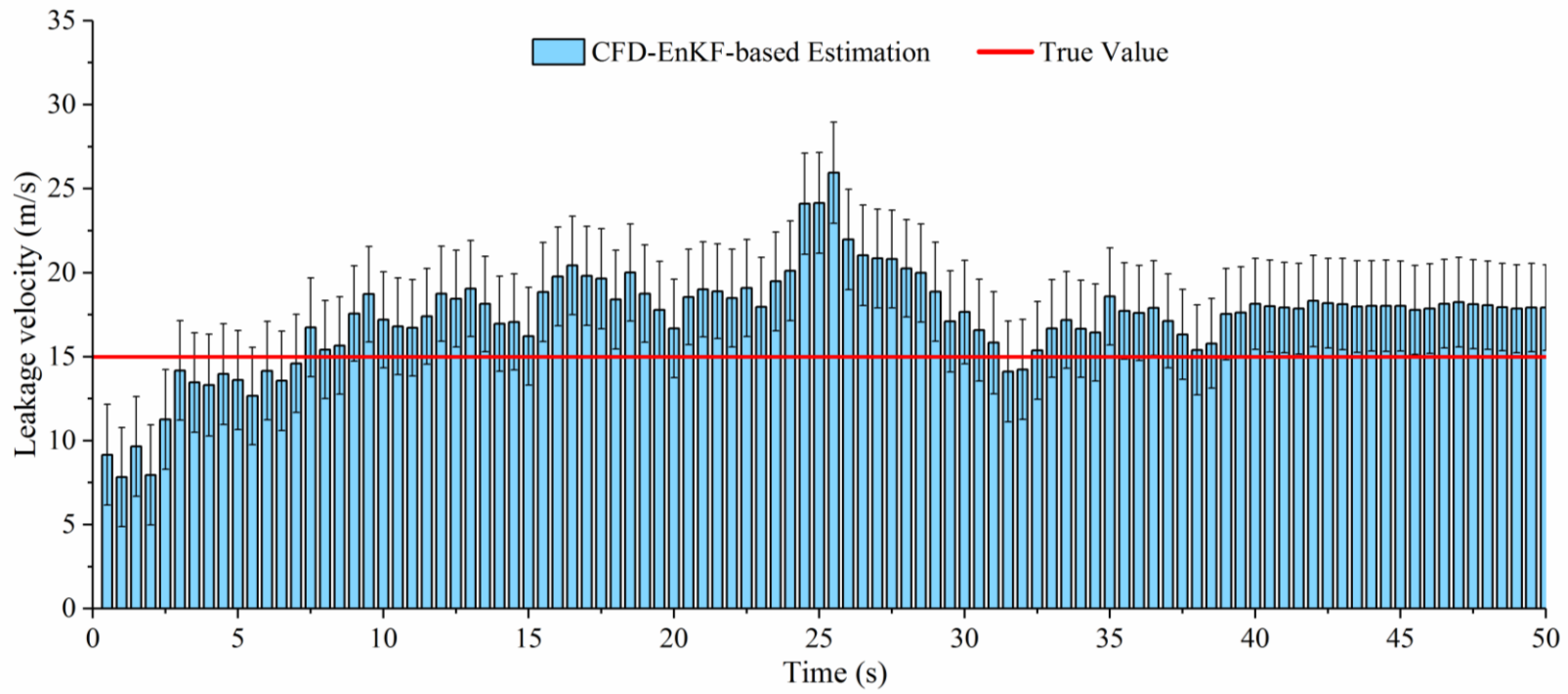


Fig.14 Leakage velocity estimation of the [CFD and EnKF coupling model](#)

459 **Fig.14** presents the leakage velocity estimation process of the LNG vapor at the
460 leak hole by the proposed **CFD and EnKF coupling model**. The underestimation of
461 leakage velocity can be seen at the initial period of time in **Fig.14**. That was because
462 the underestimation existing in the initial-guess leakage velocity had some influence on
463 the leakage velocity estimation and led to the errors of leakage velocity estimation at
464 the initial several data assimilation periods. However, the overestimation of leakage
465 velocity happened until around 30 s due to the overcorrection of the initial-guess
466 leakage velocity caused by the data assimilation process. Finally, the estimation of
467 leakage velocity became stable at around 18 m/s despite some fluctuations. The mean
468 relative error between the leakage velocity estimation and the true value was 24.6 %
469 from start to 30 s and the mean relative error of the leakage velocity estimation became
470 16.1 % from 30 s to the end due to the estimation of leakage velocity became stable
471 gradually after 30 s. Therefore, we come to a conclusion that the proposed **CFD and**
472 **EnKF coupling model** could be used to provide a reasonable estimation of LNG vapor
473 leakage velocity with a high similarity to the actual leakage velocity despite there are
474 huge errors existing in the initial-guess leakage velocity.

475 **4. Conclusion**

476 **In this paper, a three-dimensional CFD and EnKF coupling model was proposed**
477 **with the combination of CFD simulation and data assimilation technique, which is of**
478 **potentials to provide more accurate LNG vapor distributions and source term**
479 **estimations for emergency response and safety control of LNG vapor leakage accidents.**

480 The main conclusions of this paper are presented below:

481 a) An OpenFOAM-based model was evaluated and validated in the simulation of
482 LNG vapor leakage and dispersion by the Burro 8 spill test. The results show that the
483 rhoReactingBuoyantFoam solver is effective in the simulation of LNG vapor dispersion
484 compared with the experimental data and the ANSYS FLUENT results, which can be
485 used as an alternative tool for simulating LNG vapor dispersion.

486 b) At the initial stage of LNG leakage, the process of LNG vapor dispersion in the
487 LNG receiving terminal is dominated by the leakage velocity and the wind speed. Later,
488 the natural wind velocity, buoyancy forces and the complex obstacle layouts will have
489 a significant influence on the characteristics of the LNG vapor dispersion. The
490 spreading features of the dense vapor driven by the wind field and the gravity can be
491 well captured by the proposed CFD solver.

492 c) The proposed three-dimensional CFD and EnKF coupling model can obtain
493 high-confidence prediction of spatiotemporal distribution of leaked LNG vapor and
494 realize the reasonable estimation of LNG vapor leakage velocity. The effectiveness of
495 the LNG vapor distribution predictions in the horizontal and vertical sections with
496 different number of observation sites was evaluated with good reliability. Moreover, the
497 estimation of leakage velocity can be obtained with acceptable errors after a period of
498 data assimilation by the proposed model, which could be useful to provide leakage
499 source information for decision-makers.

500 With the development and popularity of the supercomputer and the high-
501 performance computing (HPC) technique, the computational efficiency of the proposed
502 CFD and EnKF coupling model would be significantly improved, which helps to
503 achieve a more timely source term estimation and LNG vapor distribution prediction.
504 Additionally, machine learning is also a promising technique that can realize timely
505 prediction of LNG vapor leakage and estimation of the leakage source by combining
506 with the proposed model, which can be employed to generate huge data with high-
507 confidence for model learning.

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