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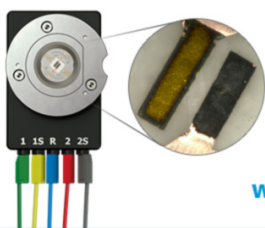
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Electronic Structure of Bi-Activated Luminescent Compounds and Pure Bismuth Photocatalytic Compounds

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The trends in electronic structure of Bi^{3+} and Bi^{2+} as luminescent dopant in wide bandgap inorganic compounds and that of pure Bi-compounds for photocatalytic splitting of water are explored by determination of vacuum referred electron binding energies. Spectroscopic data combined with the chemical shift model from the luminescence field and data on flatband potentials in electrochemistry provide most of the needed data. Occasionally data from photoelectron spectroscopy is used. The trends in VRBE of Bi^{3+} and Bi^{2+} ground state and excited state levels resemble that of Ce^{3+} and Eu^{2+} lanthanides. To some extent a pure Bi-compound can be regarded as a 100% Bi^{3+} doped La-compound. This all will be demonstrated and an overview on Bi electronic structure is presented. Comparison of electronic structure for Bi as luminescent dopant in inorganic compounds with pure Bi-compounds entails also a comparison of two disciplines in electro-chemistry, that of luminescence materials and of photo-catalytic compounds.

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Bismuth as a luminescent activator (Bi^{2+} or Bi^{3+}) and pure Bi-compounds have a very long history.¹⁻³ They are being studied for laser applications, phosphors for light emitting diodes (LED), near infrared optical amplifiers, nano-particles for bio-imaging.⁴ Bismuth is environmental friendly and non-toxic which is an important criterion for application. Besides luminescence activator, Bi^{3+} in a wide bandgap compound can also act as a hole trapping and as an electron trapping center, and those aspects can be exploited in afterglow and storage phosphor applications.⁵⁻⁷ The pure Bi-compounds are studied for photo-catalytic hydrogen production from water.⁸ BiVO_4 and Bi_2O_3 are among the best known examples.^{9,10} $\text{Bi}_4\text{Ge}_3\text{O}_{14}$ was discovered in 1973 as scintillation material¹¹ and today is still widely applied for detection of γ -ray photons. There is also interest in pure Bi-compounds for photo-voltaic applications,^{12,13} battery applications and as a super capacitor for energy storage.¹⁴

How bismuth doped inorganic compounds and pure bismuth compounds perform is intimately connected with the electronic structure. Figure 1a illustrates the principle in photo-catalytic water splitting using a Bi-compound as semi-conducting photo-anode. Valence band (VB) holes and conduction band (CB) electrons are generated by solar light in the photo-anode on the left. Due to band-bending at the anode-water interface, the CB electrons will move to the external circuit and the holes cause a redox reaction with water at the interface to generate the evolution of O_2 . The electrons via a metal electrode on the right cause a redox reaction leading to the evolution of H_2 . The bandgap of the photo-anode should be small to absorb large part of the solar spectrum. The electron binding energy at the VB-top at the interface must be below the electrochemical potential for the evolution of O_2 , and the electron binding energy at the CB-bottom must be above that for the evolution of H_2 . These potentials are at 0 V and +1.23 V vs the standard hydrogen electrode (SHE) potential which implies at -4.44 eV and -5.67 eV vs the vacuum level.^{9,15,16}

Figure 1b illustrates the function of Bi^{3+} and Bi^{2+} as activator and trapping centers in inorganic wide bandgap compounds. Here, the ground state of Bi^{3+} is located above the VB-top and its excited state below the CB-bottom. The levels of Bi^{2+} are located higher in the bandgap and closer to the CB-bottom. Here ground state location actually means the binding energy of an electron in such ground state relative to that at the VB-top. The locations are equivalent to the ($\text{Bi}^{3+}/\text{Bi}^{4+}$) and ($\text{Bi}^{2+}/\text{Bi}^{3+}$) charge transition levels. If the Fermi

level of the compound moves above these charge transition levels, Bi^{4+} will be reduced first to Bi^{3+} and next to Bi^{2+} . In the illustration of Fig. 1b, Bi^{3+} can trap a VB-hole (arrow 1) to become Bi^{4+} but it also can trap a CB-electron (arrow 2) to become Bi^{2+} . In combination with for example lanthanide based trapping centers, one may design suitable afterglow and charge carrier storage phosphors once the charge transition levels can be predicted.^{5,17} Bi^{3+} and Bi^{2+} can also act as luminescence centers emitting in the ultraviolet to blue (arrow 3) in the case of Bi^{3+} and emitting in the deep red (arrow 4) in the case of Bi^{2+} . Bi-luminescence can be quenched by thermal excitation of an electron from the excited state to the empty CB as shown by arrow 5 for Bi^{3+} . Bi^{3+} emission can also be quenched by thermal excitation of a hole to the VB. In the latter case one may use the hole picture to illustrate hole ionization.¹⁸ In Fig. 1b hole ionisation (arrow 6) is the quenching route since it requires less energy than electron ionization (arrow 5).

This work aims to provide an overview on the electronic structure of pure Bi-compounds and Bi^{3+} and Bi^{2+} doped compounds. Due to a lack of a common energy reference such perspective has been hidden or not recognized properly. Photocatalysis is an electrochemical topic where it is customary to use the standard (SHE) or normal hydrogen electrode (NHE) potential as a reference. In the luminescence field, a side-topic of electrochemistry, the energy at the top of the valence band is often used as a reference. However, we are interested in how Bi charge transition levels change with type of compound and using the VB-top as energy of reference will hide such changes. Also the use of different energy references in the different disciplines of electrochemistry prevents the inter-comparison of those fields. To avoid these compound dependent and discipline dependent energy referencing it is essential to use the vacuum level as the common reference for energy.

In the field of luminescence, a method has been developed to determine the binding energies of electrons in impurity and host band states with respect to the vacuum level.¹⁶ The method exploits the unique properties of the 4f-shell of the divalent and trivalent lanthanides. The 4f-shell is being filled with at most 14 electrons in going through the lanthanide series from La to Lu. The shell is located relatively close to the nucleus and surrounded by filled $5s^2$ and $5p^6$ orbitals of the atom. There are many different states in the partly filled 4f-shell as given by the famous Dieke level diagram,¹⁹ and transitions between those states provide the lanthanides with their rich, versatile, and excellent luminescence properties that are widely exploited in science and application. The chemical environment interacts with a lanthanide in different ways that will affect the

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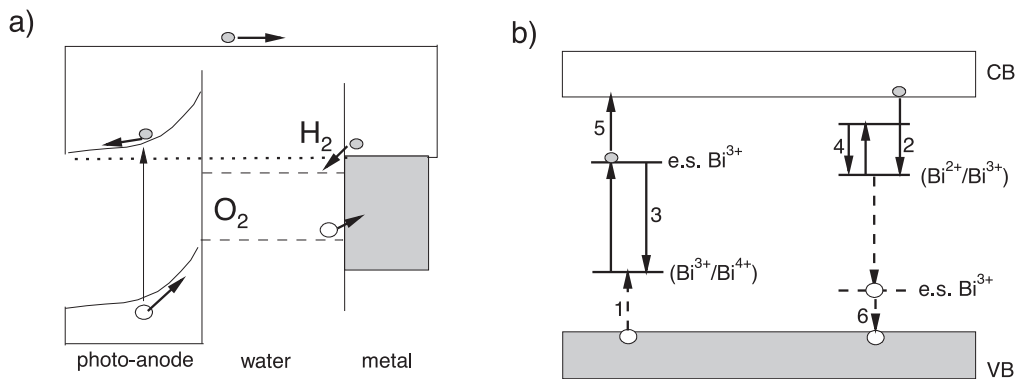


Figure 1. The role of electron binding energies in Bi-doped and pure Bi-compounds. (a) illustrates the use of Bi-compounds as photo-anode for the generation of hydrogen, (b) illustrates electron trapping in Bi^{3+} and hole trapping in Bi^{3+} , and the luminescence transitions in Bi^{3+} and Bi^{2+} . Dashed arrows and levels denote hole transitions and hole states.

electron binding energies in both the lanthanide and its surrounding anion ligands. We will distinguish three different interactions. (1) The covalence between lanthanide and anion orbitals together with anion polarizability leads to energy lowering of lanthanide electronic states. This is collectively known as the nephelauxetic effect.²⁰ (2) The low symmetry of a chemical environment, i.e., a crystalline lattice, as compared to the full rotational symmetry of free space, leads to crystal field splitting of otherwise degenerate states. A very important aspect is that inner 4f-orbitals of the lanthanides are rather insensitive to the nephelauxetic effect and crystal field splitting. The Dieke diagram of lanthanide excited states is for that reason almost invariant with type of chemical environment.

There is yet a third interaction (3) which is the chemical shift of binding energy due to the negative screening charge around a cation. The chemical shift of the $4f^7$ ground state of Eu^{2+} is about 20 eV in a liquid or solid chemical environment. Most unique is the small compound-to-compound variation in chemical shift. It appears only ± 0.3 eV and the variation is also highly predictable from the constituting elements and structure of the compound. What makes lanthanides further unique is the systematics in properties when going through the lanthanide series. The binding in the lanthanide $4f^n$ ground state always follows a similar zigzag pattern as function of n which means that once we know binding energy in one lanthanide we know them for all lanthanides.

In this work we will first briefly address the various methods to determine the binding energies in impurity and host band states with respect to the vacuum level. Next we will briefly review the chemical shift model to determine vacuum referred binding energy schemes from lanthanide spectroscopic data. Then we will apply those models to determine the VRBE energy in bismuth levels when as dopant in a compound and when as a pure Bi-compound. Results from this field of spectroscopy will be compared with that derived from other fields in electrochemistry. We will demonstrate clear systematics with level location or binding energy and the chemical properties of the environment which provides a predictive tool. We will also see that from the binding energy in the Bi^{3+} and Bi^{2+} ground states in an inorganic compound one may estimate binding energies in pure Bi-compounds. The overall aim is to provide an overview on how the VRBE in the Bi-levels change with type of compound, and to relate knowledge from the luminescence field with that from photocatalytics.

Methods to Determine Vacuum Referred Electron Binding Energies

The vacuum referred electron binding energy in a multi-electron state of a dopant or at the valence band (VB)-top or conduction band (CB)-bottom is defined as minus the energy needed to remove an electron from such state and bring it to a state where the electron will have zero energy. This is the vacuum level where both kinetic and potential energy is zero. One may distinguish purely experimental

methods, semi-empirical methods and computational methods to establish VRBE values.

Experimental and computational methods.—A straightforward method to determine vacuum referred binding energies is X-ray or ultraviolet photo-electron spectroscopy (XPS or UPS). Electrons are ejected from occupied states in the sample and their kinetic energy is measured in the vacuum. The method works well for conducting materials like metals and semi-conductors. However, such method applied to wide bandgap insulators faces problems with sample charging. Contact potentials can also introduce systematic errors. To deal with systematic errors, usually an internal reference is used like the binding at the top of the valence band or the Fermi level in metals. We will use information from photoelectron spectroscopy for a couple of pure Bi-compounds. Unfortunately, the method is not sensitive enough to probe electron binding energies in dopant states when concentrations are in the 1 mole% region.

Flatband potentials are measured by the onset potential for generating photocurrents in semi-conductors. Figure 1a shows CB-bending at the photo-anode water interface. By applying a bias the bending can be reduced to zero (flatband) which then provides information on the energy at the conduction band bottom. For example in Ref. 21 the flatband potential of BiVO_4 was determined as -0.58 eV vs the Ag/AgCl redox potential at $\text{pH} = 6.6$. This potential can then be converted to a VRBE at the CB-bottom of -4.49 eV. Subtracting the bandgap energy as determined from a Tauc plot then provides the VB-top at -7.0 eV.

An empirical method frequently encountered in the field of photocatalytic materials is based on the concept of absolute electronegativity of semiconductors. Pearson's²² or Mulliken's absolute electronegativity of an atom is defined as the arithmetic average of electron affinity and first ionisation potential of that atom. The absolute electronegativity of a semiconductor is then defined as the geometric mean value for the compound, and it defines the mid bandgap VRBE. Meng et al.²³ used that method to determine the VRBE at the CB-bottom and VB-top of bismuth photocatalytic semiconductors. The method is however rather inaccurate. In this work we will see that for pure Bi-compounds it systematically predicts too low VRBEs at the band edges.

Ab-initio and first principle calculations can provide detailed insight in the electronic bandstructure, the wavefunctions of initial and final states in luminescence transitions, and lattice relaxation phenomena. However, calculations still face severe problems when dealing with unoccupied states like that of the conduction band. Bandgaps tend to be largely (30%) under-estimated, and special methods are needed to repair that. At this stage we rate the accuracy of computational methods to establish VRBE energies too poor to be useful for our purpose. What remains as most reliable are the results from the measurement of flatband potentials in electrochemistry and the chemical shift method from lanthanide spectroscopy.

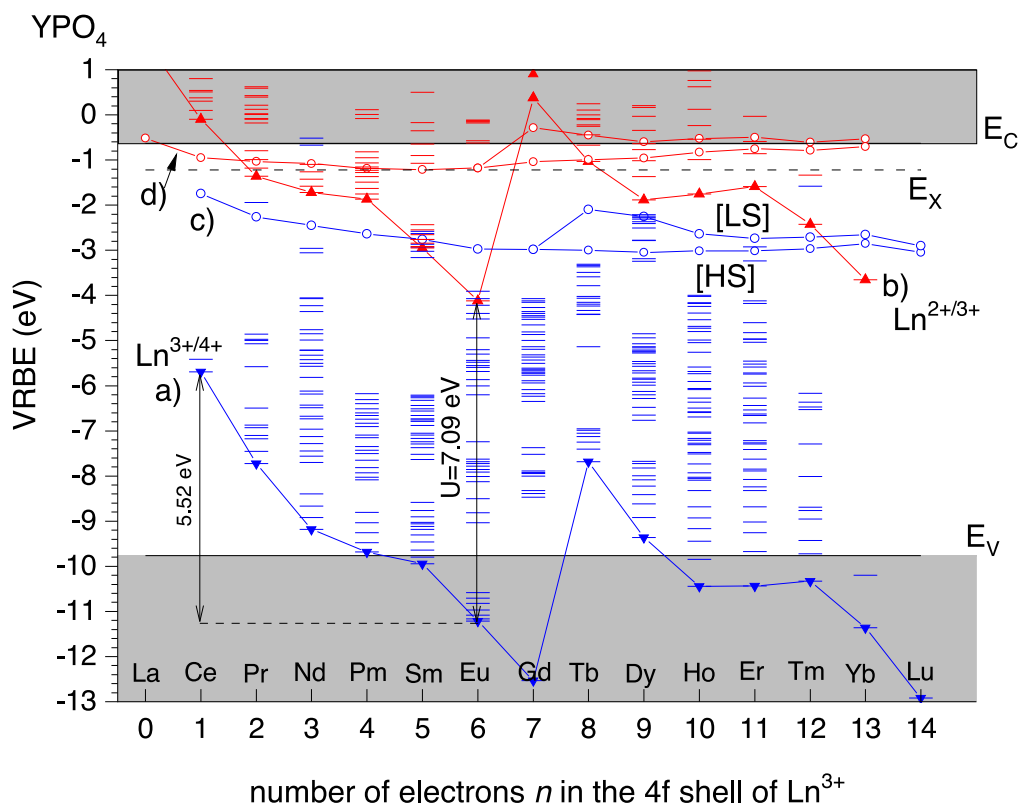


Figure 2. The vacuum referred binding energy scheme for the trivalent and divalent $4f^n$ lanthanide ground and excited state levels in YPO_4 . (a) Connects the VRBE in the $\text{Ln}^{3+} 4f^n$ ground state levels and can also be denoted as the $(\text{Ln}^{3+}/\text{Ln}^{4+})$ or $\text{Ln}^{3+/4+}$ charge transition levels, (b) connects the same for divalent lanthanides, (c) connects the VRBE in the lowest energy $4f^{n-1}5d$ states of trivalent lanthanides where for $n > 7$ a distinction between the high spin [HS] and low spin [LS] states is made, (d) connects the same for divalent lanthanides. E_V , E_X , E_C are the VRBE at the valence band top, in the host exciton state, and at the conduction band bottom, respectively.

The chemical shift method.—A lanthanide VRBE scheme as in Fig. 2 shows the binding energies in the divalent and trivalent lanthanide $4f^n$ states and the lowest energy $4f^{n-1}5d$ excited states together with that at the band edges. With the development of the chemical shift model in 2012¹⁶ and its further refinement in 2020^{24,25} we are able to construct such schemes routinely with sufficient accuracy to explain and predict many lanthanide luminescence phenomena.

The main physics behind the chemical shift model is a screening of the positive charge of the lanthanide by the surrounding chemical environment. An Ln^{2+} will be effectively screened by $-2e$ of negative charge and an Ln^{3+} by $-3e$ of negative charge. Screening is most optimal in a metal environment where the free conduction band electrons can approach the lanthanide most closely. Screening is least optimal in a fluoride compound where electrons are strongly bonded in the $2p^6$ fluorine orbitals. In between, screening scales with how strong electrons are bonded in the anion which in turn follows the familiar nephelauxetic sequences, i.e., $F < O < Cl < Br < N < I < S < Se$ and within the oxides $\text{SO}_4^{2-} < \text{CO}_3^{2-} < \text{PO}_4^{3-} < \text{H}_2\text{O} < \text{BO}_3^{3-} < \text{SiO}_4^{4-} < \text{aluminates} < \text{RE}_2\text{O}_3$.²⁰ The Coulomb repulsion between the negative screening charge with an electron in the lanthanide causes a reduction in that electron binding energy. This reduction is called the chemical shift and is by definition zero for the electrons in the free and unscreened lanthanide ions. Equation 1 is the expression from the chemical shift model for the VRBE in the Eu^{2+} ground state where the second term on the right hand side represents the chemical shift.^{24,25} The value of -24.92 eV is the binding in the $4f^7$ ground state of Eu^{2+} as free ion and is equivalent to the negative of the 3th ionisation potential of Eu.

$$E_{4f}(7, 2 + , A) = -24.92 + \frac{18.05 - U(6, A)}{0.777 - 0.0353U(6, A)} \quad [1]$$

Over the years YPO_4 has served as a model compound to develop, to test, and to refine the chemical shift model, and a diversity of techniques has been applied to obtain data on energy level locations. Figure 2 shows the lanthanide VRBE diagram for YPO_4 . It was obtained with the refined chemical shift model and the diagram can also be found in Ref. 25. The main parameter is the Coulomb repulsion energy $U(6, A)$ defined as the electron binding energy difference between the Eu^{2+} and Eu^{3+} ground states in chemical environment A . Its value can be deduced from a so-called host referred binding energy (HRBE) diagram derived from lanthanide spectroscopic data. It can also be deduced from the observed centroid shift $\epsilon_c(A)$ of the $\text{Ce}^{3+} 5d$ -levels in the compound.²⁶ Equation 1 connects the value for $U(6, A)$ with the VRBE $E_{4f}(7, 2 + , A)$ in the $4f^7$ ground state of Eu^{2+} in chemical environment A . $U(6, \text{free})$ is 18.05 eV for free europium ions and varies from 7.6 eV in highly ionic fluoride compounds (strong anion electron bonding) down to ≈ 6.0 eV in highly polarizable sulfide and selenide compounds (weak anion electron bonding). The smallest value of about 5.7 eV applies for Eu metal with free conduction band electrons. For YPO_4 in Fig. 2 a value of 7.09 eV applies.

In the refined chemical shift model of 2020, the nephelauxetic effect on the binding energy in the lanthanide $4f^n$ ground state was included. It turns out that the binding energy for $n \geq 8$ may increase (becomes more negative) several 0.1 eV due to the nephelauxetic effect; the effect for $n \leq 7$ is quite insignificant. The schemes and VRBE data presented in this work were all obtained with the refined chemical shift model.

The VRBE in Divalent and Trivalent Bismuth States

Bi^{3+} has $6s^2$ ground state electron configuration and the typical energy level scheme is shown in Fig. 3a. Exchange splitting in the

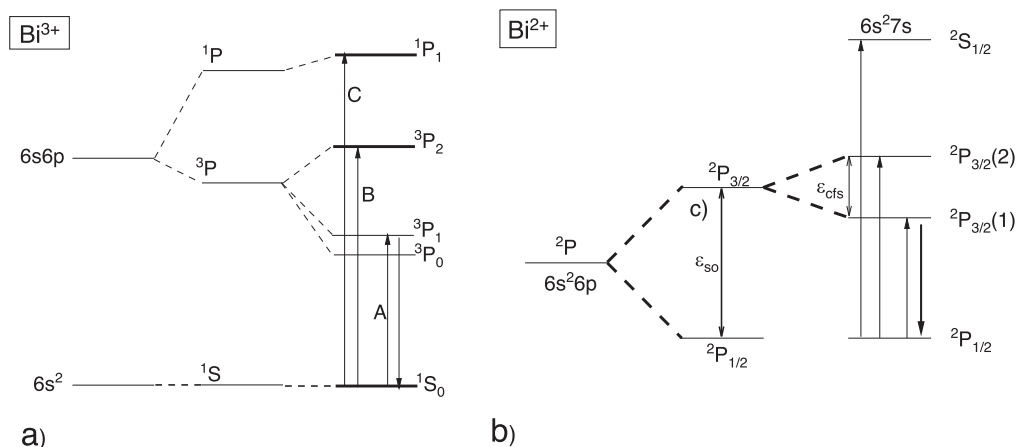


Figure 3. The level scheme for (a) Bi^{3+} and (b) Bi^{2+} . The $6s6p$ excited Bi^{3+} state is split by the exchange interaction into a 3P and 1P state that are further split by spin-orbit interaction. Spin-orbit interaction in the $6p$ -orbital of the $6s^26p$ configuration of Bi^{2+} creates the ${}^2P_{1/2}$ ground state and the ${}^2P_{3/2}$ excited state that is further split by the crystal field. ${}^2S_{1/2}$ is the higher energy level of the $6s^27s$ configuration.

excited $6s6p$ configuration creates an upper 1P spin singlet and lower 3P spin triplet state. The latter is further split by spin orbit interaction. For Bi^{3+} , we traditionally distinguish the spin forbidden A and B-band transitions plus the spin allowed C-band transition.²⁷ Transitions to 3P_0 are usually too weak to be observed. The wavelength of emission from the 3P_1 level, or A-band emission, varies depending on type of compound from the ultraviolet around 220 nm to the blue around 430 nm. Figure 3b shows the levels of Bi^{2+} with $6s^26p$ electron configuration. The 2P state is split by spin-orbit interaction, and the ${}^2P_{3/2}$ state is further split by the crystal field. The Bi^{2+} emission is from the ${}^2P_{3/2}(1)$ level and is usually found in the 600–700 nm range.

We will demonstrate that the VRBE in the Bi^{3+} ground state or the $(\text{Bi}^{3+}/\text{Bi}^{4+})$ charge transition level is located above the VB-top in wide bandgap compounds and the Bi^{2+} ground state or $(\text{Bi}^{2+}/\text{Bi}^{3+})$ charge transition level is found not only below the CB-bottom but also tends to be below the first excited state of Bi^{3+} . This then suggests that in pure Bi-compounds the VB-top will have a strong contribution from Bi^{3+} ground state orbitals and the CB-bottom from Bi^{2+} ground state orbitals. To verify this, the VRBE data on pure Bi-compounds will be compared with that of La-compounds and Bi-doped compounds. Clear systematics will appear.

The VRBE in the Bi^{3+} Dopant Levels.— Bi^{3+} is the preferred valence and has been studied as luminescent center in many types of inorganic compounds. Plenty of information is available on the intrinsic transitions between the 1S_0 ground state and excited states, known as the A, B, and C-band transitions, see Fig. 3 (a). In addition to these intrinsic transitions, also bands attributed to a transition from Bi^{3+} to the CB is regularly observed which is known as the D-band. With knowledge on the VRBE at the CB-bottom and the D-band energy one may derive the VRBE in the Bi^{3+} ground state. This method was first employed by Awater and Dorenbos.^{28–30} Regarding Bi^{3+} we can limit here with reviewing and updating the results of that earlier work.

We will start with our model compound YPO_4 . Blasse et al.² already reported in 1968 a broad 3.7 eV emission band with excitation around 5.4 eV. The excitation band was assigned to the Bi^{3+} A-band in Ref. 31. In 2013 Boutinaud et al.³² suggested that the 3.7 eV emission might origin from a metal to metal charge transfer (MMCT). One year later, Cavalli et al.³³ extended the studies into the vacuum ultraviolet and reported a broad band between 150 nm and 190 nm that was attributed to the C-band excitation. Again one year later Srivastava et al.³⁴ assigned the 3.7 eV emission to pairs of Bi^{3+} in YPO_4 . Awater and Dorenbos³⁰ resolved the band between 150 nm and 190 nm into a relatively narrow C-band excitation at

7.9 eV with a broader lower energy band around 7.29 eV which was attributed to the D-band or $\text{Bi}^{3+} \rightarrow \text{CB}$ transition. This D-band can now be used to locate the 1S_0 ground state of Bi^{3+} below the CB. In Fig. 4 we assumed like in Ref. 35 that the VRBE of the electron after D-band excitation falls in between the genuine CB-bottom and E_X . The VRBE in the Bi^{3+} ground state, or equivalently the $(\text{Bi}^{3+}/\text{Bi}^{4+})$ charge transition level, is then at -8.2 V.

Upon X-ray irradiation of $\text{YPO}_4:\text{Bi}^{3+}$, a new type of emission appears around 1.85 eV (670 nm) that was attributed to Bi^{2+} emission.³⁰ The emission shows a quenching temperature of $T_{50} = 380$ K which translates to a quenching energy barrier of about 0.6 eV. Putting things together the Bi^{2+} ground state or $(\text{Bi}^{2+}/\text{Bi}^{3+})$ charge transition level is then estimated at VRBE of -3.5 eV. Note that in Fig. 4 the $(\text{Bi}^{2+}/\text{Bi}^{3+})$ charge transition level falls below the VRBE in the 3P_1 excited state of Bi^{3+} . Upon A-band excitation of Bi^{3+} , spontaneous electron transfer to a neighboring Bi^{3+} to form a $\text{Bi}^{4+}\text{-Bi}^{2+}$ pair is then energetically possible. It is now well accepted that the 3.7 eV emission reported already in Ref. 2 originates from Bi-pair emission as suggested in Ref. 34. With the derived charge transition level energies, it becomes clear that Bi^{3+} forms a 1.57 eV deep trapping center for a hole from the VB and it also forms a ≈ 2.9 eV deep trapping center for an electron from the CB. The electron and hole trapping properties of Bi^{3+} together with that of trivalent lanthanides in YPO_4 , LaPO_4 , LuPO_4 and their solid solutions were studied in Ref. 5 by means of thermo-luminescence and spectroscopic techniques. The results are consistent with the VRBE scheme of Fig. 4. Recently Liu et al.³⁶ conducted an experimental and theoretical study on charge carrier storage properties of Bi^{3+} in YPO_4 . Density Functional Theory (DFT) confirms the location of the charge transition levels above the VB and below the CB. Their calculation also suggest that it is better to speak of a $(\text{Bi}^{3+}\text{-Bi}^{3+})^*$ excited pair state than in terms of a $\text{Bi}^{4+}\text{-Bi}^{2+}$ state. That suggestion was followed in Fig. 4.

Figure 5 shows a stacked VRBE diagram with a compilation of Bi^{3+} VRBE data in inorganic compounds. Here compounds were selected where data are reasonably reliable and where one may illustrate the trends in level location with type of compound. A quite similar diagram with more compounds can be found in Awater et al.^{28,29} In each case the VRBE at the VB-top and CB-bottom is based on lanthanide spectroscopy data combined with the Refined Chemical Shift model. Compounds are in sequence of decreasing value for $U(6, A)$.

Clear trends are observed in Fig. 5. In sequence of decreasing U -value, the polarizability of the anion ligands and its screening potential of the positive Bi^{3+} cation increases. The chemical shift increases and the VRBE in the Bi^{3+} 1S_0 ground state becomes less negative from values around -11 to -10 eV for $U = 7.3\text{--}7.4$ eV in

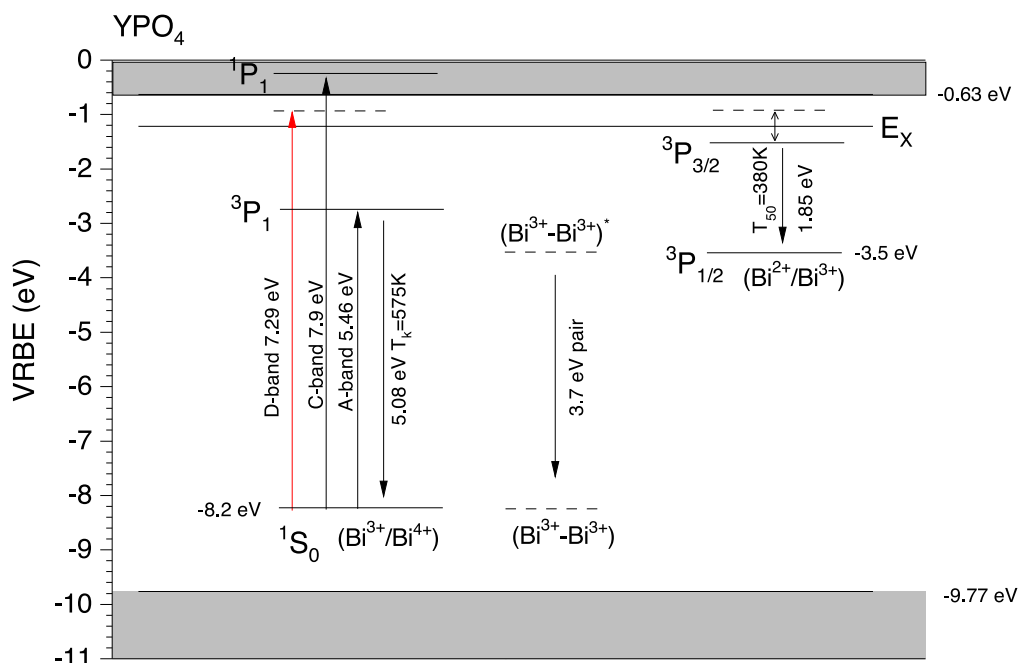


Figure 4. The vacuum referred binding energy scheme for on the left Bi^{3+} and on the right Bi^{2+} levels in YPO_4 . In the middle the levels of Bi-pairs are illustrated.

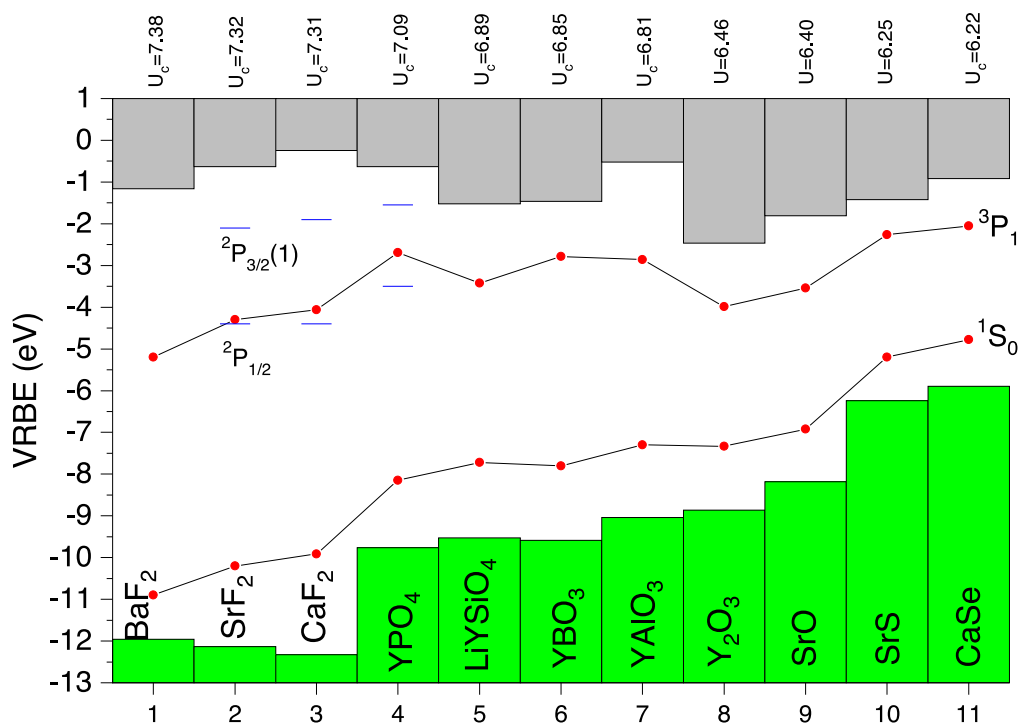


Figure 5. Stacked diagram showing the VRBEs at the VB-top and the CB-bottom together with the VRBE in the $\text{Bi}^{3+} 1S_0$ and $3P_1$ states that are connected with the drawn solid curves. The used value for the $U(6, A)$ parameter is provided at the top of the diagram. If available, the (estimated) location of $\text{Bi}^{2+} 2P_{1/2}$ ground state and $2P_{3/2}(1)$ excited states are shown. For the indirect bandgap materials SrO, SrS, and CaSe, the VRBE at the CB-bottom pertaining to the direct bandgap is shown.

fluoride compounds to values increasing from -8 eV to -7 eV in oxide compounds with $U = 7.1 \rightarrow 6.4\text{ eV}$ until finally around -5 eV for CaSe with $U = 6.22\text{ eV}$. The VRBE in the $3P_1$ excited Bi^{3+} state changes then from -5 to -2.5 eV . The excited state VRBE increases therefore less strongly than the ground state VRBE, and as a consequence the energy of the A-band absorption and emission decreases with decreasing U -value.

Figure 6 compiles data on the A-band absorption energy against the U -value assigned to the compound. A clear trend is revealed that confirms a long known observation that the A-band energy lowers with increasing nephelauxetic effect.^{1,2} In other words it scales with how strong electrons are bonded in the anions and therefore with the $U(6, A)$ value of the chemical shift model. Data on Bi^{3+} in GdOCl , LaOBr , YOCl , and LaOCl are outliers in Fig. 6 which may suggest

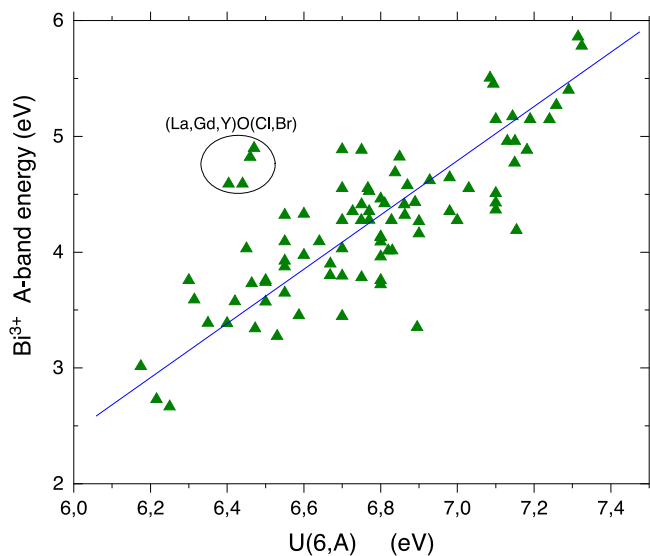


Figure 6. The energy of the Bi^{3+} A-band energy in compounds observed in absorption or in excitation spectra against the $U(6, A)$ value assigned to that compound.

that either improper assignments have been made or that specific compound properties are at play; this needs further analysis.

The VRBE in the Bi^{2+} dopant levels.— Bi^{3+} is the preferred valence in inorganic compounds but also Bi^{2+} can be stable although information is much less abundant. The Bi^{2+} emission is usually found in the 550–720 nm spectral region.^{37–39} Interest in Bi^{2+} has increased because of potential phosphor application in white-LEDs, and there is also active research in afterglow and storage phosphor applications where Bi^{3+} may act as a stable electron trapping and/or hole trapping center^{5,17,40,41} as illustrated in Fig. 1b.

Various methods to determine or estimate the VRBE in the $^2P_{1/2}$ ground state and emitting $^2P_{3/2}(1)$ excited state of Bi^{2+} were used in Ref. 29. For a couple of compounds one can use information on energy of electron transfer from Bi^{2+} to the CB-bottom or from the

VB-top to Bi^{3+} . However, very little information appears available. The presence of Bi^{2+} emission and the quenching temperature of that emission also provides information on excited state level location with respect to the CB-bottom. Information on the VRBE in Bi^{2+} levels has been compiled in the stacked diagram of Fig. 7.

For the compounds 1 until 14, Bi^{2+} emission and its excitation spectra have been reported.²⁹ The approximate VRBE energies in the $^2P_{3/2}(1)$ excited state were deduced from the thermal quenching temperature T_{50} or the onset of thermal quenching T_k of the Bi^{2+} emission. We regard the thermal ionization to the conduction band as the quenching mechanism, and with a typical lifetime of 10–20 μs ^{39,42–44} roughly 600 K eV^{-1} change in T_{50} is assumed. The relatively low quenching temperature of $T_{50} = 250$ K in $\text{SrB}_6\text{O}_{10}$ then translates to a $^2P_{3/2}(1)$ location less than 0.5 eV below the CB-bottom. T_{50} values are also known for CaSO_4 , $\text{Sr}_2\text{P}_2\text{O}_7$, $\text{Ba}_3(\text{PO}_4)_2$, and YPO_4 (see Fig. 4). In each case, a VRBE in the Bi^{2+} ground state is found around -3.6 eV, and similar values for compounds where only a lower limit for T_k is available was assumed.

The data on YPO_4 (compound 14) are the same as in Fig. 2 and Fig. 4. The last three compounds NaYGeO_4 , MgGeO_3 and $\text{Y}_3\text{Al}_5\text{O}_{12}$ in Fig. 7 have relatively low VRBE at the CB-bottom, i.e. < -2 eV, and no Bi^{2+} emission is observed. Evidently the $^2P_{3/2}(1)$ excited state is located inside the CB. For these compounds Bi^{2+} VRBE values can be estimated from thermoluminescence data on Bi^{3+} (co)-doped compounds. Bi^{3+} acting as an electron trapping center was studied in NaYGeO_4 by Lyu et al.,¹⁷ in MgGeO_3 by Katayama et al.,⁴¹ and in $\text{Y}_3\text{Al}_5\text{O}_{12}$ by Katayama et al.⁴⁰ For example in Bi^{3+} doped NaYGeO_4 a glow peak at ≈ 290 K has been assigned to electron release from Bi^{2+17} and this translates to a Bi^{2+} g.s. location about 0.6 eV below the CB-bottom as in Fig. 7. The glow peak appears at 320 K in MgGeO_3 and at 375 K in $\text{Y}_3\text{Al}_5\text{O}_{12}$. Dashed arrows (1), (2), (3) are observed charge transfer bands. Arrow 1) of length 5.34 eV was assigned to the $\text{Bi}^{3+} \rightarrow \text{CB}$ transition and provides the Bi^{3+} VRBE.¹⁷ The charge transfer band at 4.86 eV (arrow 2) in MgGeO_3 from Ref. 41 was assigned to the $\text{Bi}^{3+} \rightarrow \text{CB}$ transition. However, one may not fully exclude that it is the $\text{VB} \rightarrow \text{Bi}^{3+}$ CT, and both options are illustrated in Fig. 7. Similar applies to the 5.93 eV (arrow 3) CT-band in $\text{Y}_3\text{Al}_5\text{O}_{12}$ from Ref. 45 that was assigned to the $\text{Bi}^{3+} \rightarrow \text{CB}$ transition in Ref. 28. The other option is

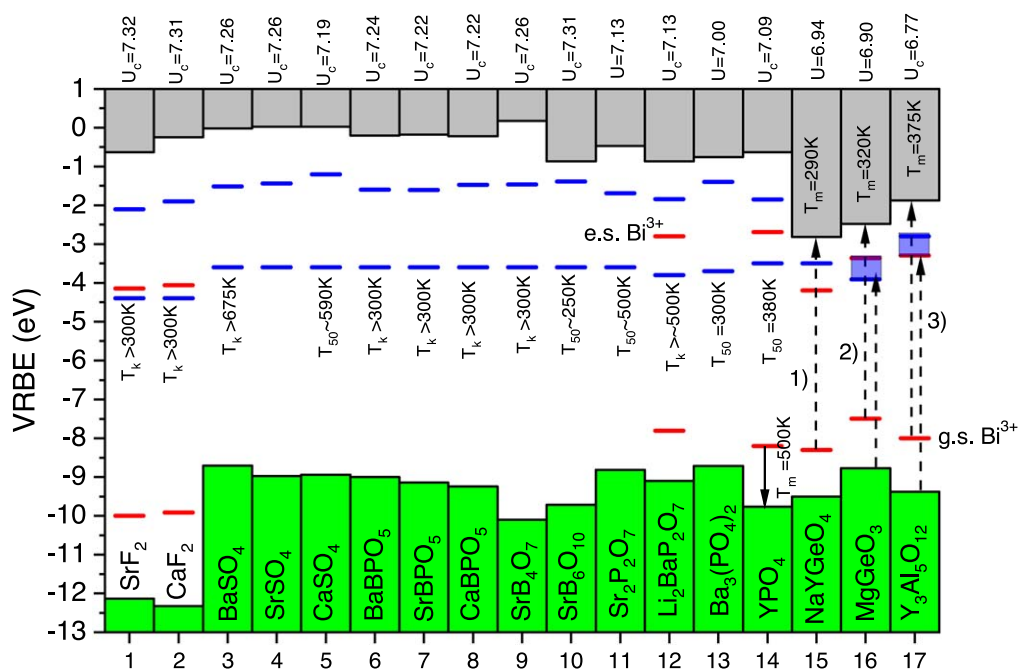


Figure 7. Stacked diagram showing the VRBEs at the VB-top and the CB-bottom together with Bi^{2+} level locations (in blue), and when available also Bi^{3+} levels (in red). The $U(6, A)$ parameter is provided at the top of the diagram. Luminescence quenching temperatures T_k and T_{50} are provided.

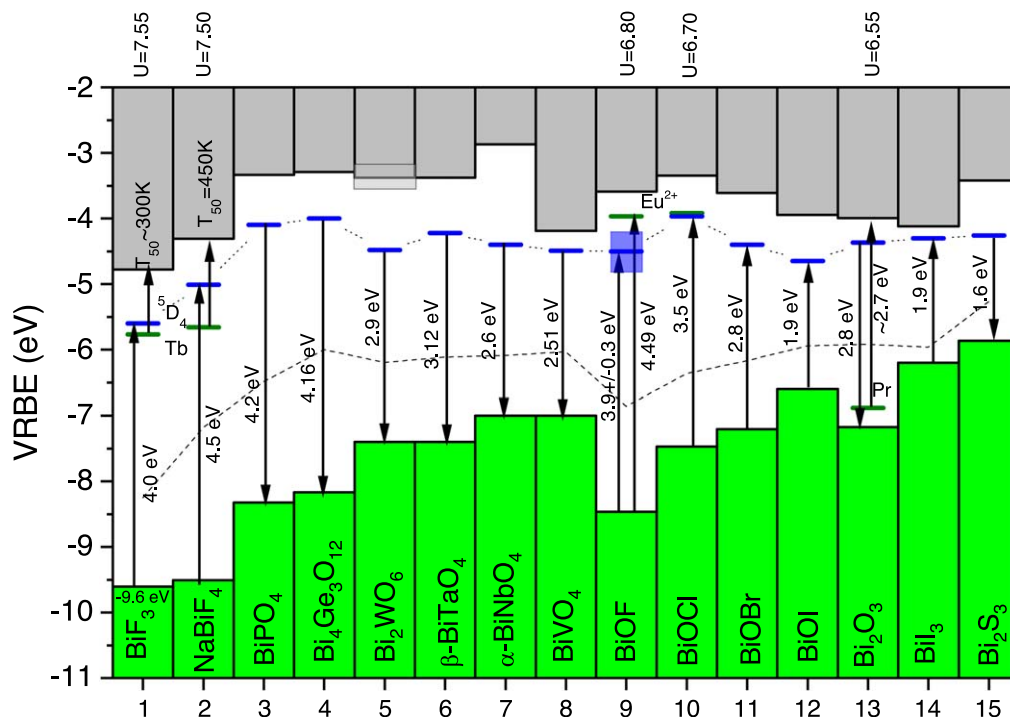


Figure 8. Stacked VRBE scheme for pure Bi-compounds. The horizontal bars (blue) connected with a dotted curve in the bandgap represent the flatband potentials. Occasionally relevant levels of Tb^{3+} , Eu^{2+} and Pr^{3+} are shown (green). In case of downward pointing arrows, the VRBE at the VB-top is derived from the measured flatband. In case of upward pointing arrows, the flatband was derived from the VB-top. The dashed curve connects the VRBE at mid bandgap energy as predicted from the absolute semiconductor electronegativity.

also shown in Fig. 7. This illustrates that depending on level locations in the bandgap a proper assignment of broad CT-bands becomes difficult or ambiguous.

Thermoluminescence can also be used to determine the VRBE in the Bi^{3+} ground state. In Eu^{3+} and Bi^{3+} co-doped YPO_4 , Eu^{3+} appears to be a deeper electron trap than the hole trap depth of Bi^{3+} . During TL-readout the hole is released from Bi^{4+} to recombine with the electron trapped on Eu^{2+} to generate Eu^{3+} emission appearing as a TL-glow peak around $T_m = 500$ K.⁵ With such information we can then estimate that the VRBE in the Bi^{3+} ground state must be at least 1 eV above the VB-top which is then consistent with Fig. 4.

Figure 7 shows that the VRBE in the Bi^{2+} ground state is fairly constant with values (tentatively) slightly below 4 eV in fluoride compounds to values around -3.6 eV in more polarizable oxide compounds. Comparing Fig. 5 with Fig. 7 one may notice that, at a given U -value, the VRBE in the Bi^{2+} ground state tends to fall below the VRBE in the Bi^{3+} excited state. This was clearly illustrated for Bi^{2+} and Bi^{3+} in YPO_4 in Fig. 4. This confirms again that when two Bi^{3+} dopants are close together and one of them is brought to the excited state, a lower energy ($\text{Bi}^{3+}\text{-Bi}^{3+}$)* excited pair state may form. The electron back transfer may then generate so called Bi-pair emission or, in case the back transfer is radiationless, form a concentration quenching route for ordinary Bi^{3+} A-band emission as suggested in Awater et al.²⁹

The VRBE in Pure Bi-compounds

The obtained data on pure Bi-compounds are presented as a stacked VRBE diagram in Fig. 8. Here a distinction is made between a definition of CB-bottom in semi-conducting compounds and in wide bandgap luminescent compounds. In the former, the optical bandgap or fundamental absorption threshold E_{fa} is obtained from a Tauc plot. E_{fa} then defines the location of the CB-bottom above the VB-top. In wide bandgap compounds like YPO_4 in Fig. 2, E_{fa} is often followed by a distinct excitation peak at E^{ex} due to host exciton creation. This defines E_X in Fig. 2. Since an exciton is a bound electron-hole pair we still need to add the exciton binding energy

E_{e-h} to reach the mobility edge defined as the CB-bottom E_C in VRBE diagrams. The empirical relation

$$E_{eh} = 0.008 \times (E^{ex})^2 \quad [2]$$

has been used.⁴⁶ For ≈ 3 eV bandgap semi-conductors, the bonding is about 0.1 eV and one may expect that at room temperature exciton dissociation generates already free charge carriers. For ≈ 10 eV wide bandgap compounds binding energies increase toward 1 eV, and excitation at E_{fa} does not create free charge carriers.

Spectroscopic information on lanthanides in pure Bi-compounds is too rare to routinely derive the VRBE at the VB-top and CB-bottom with the chemical shift method, and we need data from other methods. The electrochemical determination of the flatband potential is regarded as the best alternative. By subtracting the value for E_{fa} from the flatband potential, the VRBE at the VB-top is obtained. Figure 8 shows the measured or derived flatband potentials on the VRBE scale as horizontal levels connected by a dotted curve. Down pointing arrows show how the VB-top is reached using measured values for E_{fa} . By adding the energy where optical absorption is maximum, E_X is reached and with Eq. 2 E_C is finally obtained. Those E_C values are used in Fig. 8. Note that they are related to the direct bandgap whereas E_{fa} can be from the indirect bandgap. It is realized that the maximum in optical absorption not necessarily corresponds with E^{ex} and then E_C may not represent the genuine mobility edge of the compounds, but at the moment this seems the best approach we can take. In the end it is not that essential for the conclusions of this work. An account on how data were obtained for each individual compound in Fig. 8 is provided below.

Data used for the pure Bi-compounds.—Fluorides. The VRBE of -9.6 eV at the VB-top of BiF_3 is from X-ray photoelectron spectroscopy (XPS).⁴⁷ Information on $E_{fa} \approx 4.0$ eV and $E^{ex} = 4.65$ eV from Refs. 48, 49 was used to estimate the flatband potential and E_C . Figure 8 shows for BiF_3 the 5D_4 excited state of Tb^{3+} at -5.77 eV. The emission from this state has a reported quenching temperature of $T_{50} \approx 300$ K.⁴⁹ In Ref. 18 such quenching temperature was related to

an energy difference with $E_C \approx E(^5D_4) + 0.4 + T_{50}/475$. We thus estimate $E_C \approx -4.7$ eV which is fully consistent. For NaBiF₄, with ⁵D₄ level at -5.66 eV and luminescence quenching temperature $T_{50} = 450$ K from Ref. 49 one obtains $E_C \approx -4.3$ eV. Further, with $E^{ex} = 5.0$ eV and $E_{fa} = 4.5$ eV,^{49,50} the VRBE at the VB-top at -9.5 eV and the flatband potential at -5 eV is derived.

Oxides. For the monoclinic phase of BiPO₄, a flatband potential of -4.1 eV is from Refs. 51, 52 and with $E_{fa} \approx 4.2$ eV and $E^{ex} = 4.8$ eV,^{52,53} E_V and E_C were obtained. The VRBEs in the host bands of Bi₄Ge₃O₁₂ are an educated guess where we assumed a flatband potential of -4 eV which is typical for other Bi-compounds in Fig. 8. Subtracting $E_{fa} = 4.16$ eV from Ref. 54 assigned to the indirect bandgap provides $E_V = -8.16$ eV. The optically determined $E^{ex}(LT) \approx 4.7$ eV then provides E_C .^{55,56}

Transition metal compounds. For Bi₂WO₆, the flatband potential of -4.48 eV and $E_{fa} = 2.9$ eV were used.⁵⁷ Reports on the maximum of the absorbance vary from 3.7 eV in Refs. 58, 59 to 4.1 eV in Refs. 57, 60, 61 which gives uncertainty in E^{ex} and where to locate E_C ; a value of 3.9 ± 0.2 eV was used. For the triclinic β -BiTaO₄ phase we used the flatband potential of -4.22 eV and $E_{fa} = 3.18$ eV from Ref. 62 to derive E_V , and with $E^{ex} = 3.9$ eV to derive E_C .^{63–65} For the α -BiNbO₄ phase we used a flatband potential of ≈ -4.4 eV and $E_{fa} = 2.6$ eV to obtain E_V .⁶⁶ With $E^{ex} = 4.0$ eV, E_C is found.^{63,67} For monoclinic phase BiVO₄ we used the flatband potential of -4.49 eV and $E_{fa} = 2.51$ eV from Ref. 21 to determine E_V and $E^{ex} = 2.75$ eV from Refs. 68, 69 to determine E_C .

Halo-oxides. For the halo-oxide family information on electrochemical flatband determination was not found, and other methods were followed to deduce them. For BiOF with $U = 6.8$ eV, the (Eu²⁺/Eu³⁺) charge transition level is at -3.97 eV. The VB \rightarrow Eu³⁺ charge transfer band is at 4.49 eV,⁷⁰ and then $E_V = -8.46$ eV. The host absorption maximum is seen at 4.88 eV in Ref. 71 and at 4.63 eV in Ref. 72 yielding $E_X \approx -3.8$ eV. In Ref. 73 a VB-top at -8.39 eV was suggested to explain the mechanism of photocatalytic activity. With computational methods the VB-top is found at -8.2 eV.⁷⁴ Considering systematic errors of several 0.1 eV in each method used, the VRBE at the VB-top appears consistent. To estimate the flatband potential, E_{fa} needs to be added to $E_V = -8.46$ eV. Experimental values of 3.6 eV and 4.2 eV have been reported.^{72,73,76} A computed value of 4.2 eV is reported in Ganose et al.⁷⁴ We estimate a flatband potential somewhere around -4.5 ± 0.3 eV.

For BiOCl, $E_{fa} = 3.5$ eV and $E^{ex} = 4.0$ eV are reported.^{75–77} Information on flatband potential studies was not found and the VRBE was derived from lanthanide spectroscopy instead. The (Eu²⁺/Eu³⁺) charge transition level when $U = 6.7$ eV is at -3.92 eV, and with a VB \rightarrow Eu³⁺ CT band reported near 3.55 eV,^{75,78,79} the VB-top is reached at -7.47 eV. Adding E_{fa} , a flatband potential around -3.97 eV is expected.

For BiOBr, experimental information on lanthanide spectroscopy and flatband studies are not available. From the absolute semiconductor electronegativity, the mid bandgap VRBE is calculated at -6.1 eV.^{23,80} With $E^{ex} = 3.5$ eV and $E_{fa} \approx 2.8$ eV,^{79–82} the VB-top would be at -7.5 eV, the flatband at -4.7 eV, and E_C at -3.9 eV. However, as will be shown later absolute semiconductor electronegativity systematically provides too low values for the band positions in pure Bi-compounds. We tentatively assumed 0.3 eV higher values which locates the flatband at -4.4 eV.

For BiOI, we followed the same method as for BiOBr. The concept of absolute semiconductor electronegativity used in Refs. 23, 83 yields the mid bandgap VRBE at -5.94 eV. With $E^{ex} = 2.6$ eV from Refs. 80, 84, 85 and $E_{fa} = 1.94$ eV from Refs. 80, 83, 84, one obtains $E_V = -6.85$ eV, a flatband at -4.9 eV, and E_C at -4 eV. These values are quite similar to that of computational studies in Ganose et al.⁷⁴ providing $E_V = -7$ eV and a flatband at -5 eV. Yet, because of the systematic error, we will place the band edges at 0.25 eV higher energy bringing the flatband at -4.65 eV.

BiI₃, Bi₂O₃ and Bi₂S₃. For BiI₃, a workfunction of 5.8 eV as obtained from photoelectric effect measurements suggest $E_V = -5.8$ eV.⁸⁶ UPS studies indicate E_V between -6 and -6.3 eV.¹³ A strong exciton peak at $E^{ex} = 2.0$ – 2.1 eV is reported in Refs. 87–89 with direct bandgap of 1.96 eV and indirect bandgap of 1.67 eV.⁸⁸ Altogether we used $E_V \approx -6.2$ eV, a flatband near -4.3 eV and E_C near -4.1 eV in Fig. 8 as compromise between the different sets of data.

Bi₂O₃ is well-studied for photo-catalytic purposes^{90–92} with a measured flatband potential of -4.37 eV.⁹⁰ With $E^{ex} = 3.1$ eV and $E_{fa} = 2.8$ eV, $E_V \approx -7.2$ eV is obtained.^{90,92–94} We can also exploit data on Pr³⁺ in Bi₂O₃. Pr³⁺ creates a broad unresolved diffuse reflectance band extending from 425 nm (2.9 eV) to 525 nm (2.4 eV)⁹⁴ that we here attribute to the Pr³⁺ \rightarrow CB intervalence charge transfer (IVCT) band. With the (Pr³⁺/Pr⁴⁺) charge transition level at -6.88 eV for $U(6, A) = 6.55$ eV this is fully consistent with the VRBE data in Fig. 8.

Bi₂S₃ has a measured flatband potential of -4.26 eV.⁹⁰ With $E^{ex} = 2.4$ eV and $E_{fa} = 1.6$ eV,^{95,95–97} $E_V = -5.86$ eV and $E_C = -3.4$ eV are obtained.

A first inspection of Fig. 8 shows that the flatband potentials are fairly constant and usually fall between -4 and -4.5 eV. For the two fluoride compounds they are 1 eV lower. For each compound in Fig. 8, the VRBE at mid bandgap was also calculated from the absolute semiconductor electronegativity, see also,²³ and the values are connected by the dashed line. In all cases it runs significantly below the mid bandgap energy as derived experimentally. Clearly there appears to be a systematic difference which raises doubts on the validity of the frequent use of absolute semiconductor electronegativity in the field of photocatalytic compounds. For compounds where information on lanthanide spectroscopy combined with the chemical shift model has been used, results are consistent with experimental flatband determinations.

Equivalent La-based compounds.—Bi³⁺ has similar ionic radius and charge as La³⁺ and also the crystal structure of a pure Bi-compound is usually similar to that of the equivalent La-compound. It is then of interest to compare the VRBE in the pure Bi-compounds of Fig. 8 with that of La-compounds as shown in 9. Since there is no equivalent La-compound for Bi₄Ge₃O₁₂ we used information on LaAlGe₂O₇ instead. Lanthanide spectroscopy on La₂WO₆ appears too scarce, and instead we used Y₂WO₆ as equivalent compound for Bi₂WO₆ in Fig. 9. The standard method of the (refined) chemical shift model was used to construct the lanthanide VRBE diagrams. The two fluorides are 11 eV wide bandgap compounds. The VB-top in the oxide and halo-oxide compounds are found in the -8 eV to -9 eV region, and that of LaI₃ and La₂S₃ at 3 eV higher energy. Note the relatively low lying CB-bottom in the four transition metal based compounds which is dominated by the VRBE in the $5d$ (W⁵⁺ and Ta⁴⁺), $4d$ (Nb⁴⁺), and $3d$ (V⁴⁺) orbitals.⁹⁸ Germanium based compounds, as in LaAlGe₂O₇ also tend to have low lying CB-bottom.

For several of the La-compounds and for Y₂WO₆, spectroscopic data on Bi³⁺ is available enabling to determine or estimate the VRBE in the Bi³⁺ and Bi²⁺ impurity ground states. Bi data for LaPO₄ can be found in Ref. 5 for Y₂WO₆ in Refs. 2, 28, 99, for LaNbO₄ in Refs. 28, 100, for LaVO₄ in Refs. 28, 101. For LaOBr we interpreted a broad 4.26 eV excitation band for Bi emission¹⁰² as the VB \rightarrow Bi³⁺ CT-band. Similar was done for the 4.48 eV excitation band in Bi³⁺ doped LaOCl in Ref. 103 and for the 5.0 eV band in La₂O₃ from Refs. 104, 105. The interpretation of the broad bands in these latter three compounds remains speculative. The alternative interpretation of a Bi³⁺ \rightarrow CB or a broad band (Bi³⁺-Bi³⁺) pair excitation cannot be excluded at this stage.

In Fig. 9 the VRBE of the CB-bottom, flatband potential, and VB-top of the corresponding pure Bi-compounds of Fig. 8 are connected by curves a), b), and c), respectively. Curve c) tends to follow the same patterns as the VRBE at the VB-top of the

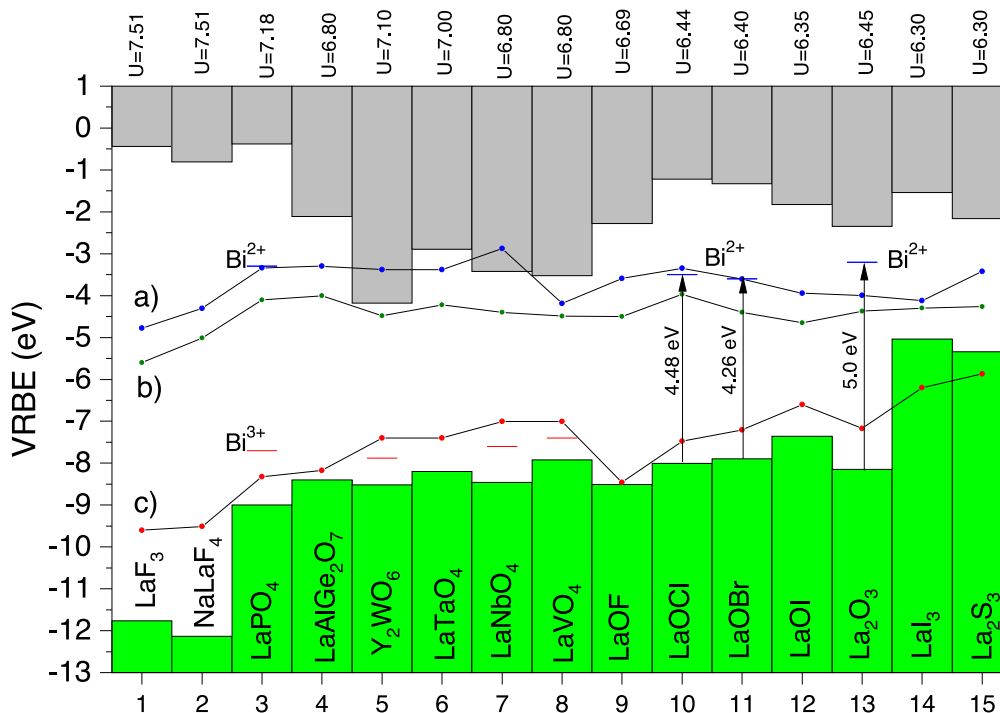


Figure 9. Stacked diagram showing the VRBEs at the VB-top and the CB-bottom of La-based compounds and of Y_2WO_6 . For several compounds the (Bi^{3+}/Bi^{4+}) and (Bi^{2+}/Bi^{3+}) charge transition levels are shown. Solid curves a), b), and c) connect the VRBE at the CB-bottom, of the flatband potential, and VB-top of corresponding pure Bi-compounds, respectively.

La-compounds whereas the flatband potential is fairly constant around -4 eV without a correlation with the CB-bottom of the La-compounds.

Discussion

In discussing the trends in VRBE in the Bi^{3+} and Bi^{2+} ground and excited states we will compare the observations with trends known for the lanthanides Ce^{3+} and Eu^{2+} that have about similar ionic radius as Bi^{3+} and Bi^{2+} . An important difference is the localized and atomic character of the inner 4f-orbital that is occupied with one or seven electrons in the ground states of Ce^{3+} or Eu^{2+} . The VRBE in the

lanthanide $4f^n$ ground states is very little affected by crystal field splitting and the nephelauxetic effect. The remaining compound dependent effect is the chemical shift. Equation 1 is the expression for the VRBE in the Eu^{2+} ground state. Subtracting $U(6, A)$ and adding the VRBE difference $\Delta E(Ce^{3+}, Eu^{3+})$ between Ce^{3+} and Eu^{3+} one obtains the VRBE $E_{4f}(1, 3+, A)$ in the Ce^{3+} ground state as in Eqs. 3 and 4. That difference is 5.52 eV in Fig. 2 and does not significantly change with type of compound.

$$E_{4f}(1, 3+, A) = E_{4f}(7, 2+, A) - U(6, A) + \Delta E(Ce^{3+}, Eu^{3+}) \quad [3]$$

$$\Delta E(Ce^{3+}, Eu^{3+}) \approx 5.5 \text{ eV} \quad [4]$$

The VRBE in the 4f ground state of Ce^{3+} as free ion is -36.9 eV, and with $U(6, A)$ increasing from 7.6 eV toward 6.2 eV that VRBE increases from -6.40 eV toward -4.33 eV as shown with curve a) in Fig. 10. The VRBE in the Bi^{3+} $6s^2$ ground state as free ion is equivalent to the negative of the 4th ionisation potential of bismuth and equals -45.4 eV. Figure 5 shows that in compounds the Bi^{3+} VRBE increases from -11 eV in BaF_2 up to near -5 eV in $CaSe$. It appears thus that the chemical shift in absolute number (≈ 34 eV) and its increase of ≈ 6 eV with decreasing U -value is somewhat larger than the values of ≈ 31 eV and 2.5 eV for Ce^{3+} . Nevertheless the upward trend is precisely the same and follows the nephelauxetic sequence. The stronger trend for Bi^{3+} may be related with a stronger interaction of the outer $6s^2$ orbital with the anion screening charge as compared with that of the inner 4f-orbital, and supposedly also covalence with the anion ligands will be more strong.

Let us now turn to the VRBE in the 3P_1 excited Bi^{3+} state and compare that with the VRBE in the lowest energy excited 5d state of Ce^{3+} . The 5d-orbital extends to the outside of the Ce^{3+} cation and besides chemical shift it is also subject to crystal field splitting and nephelauxetic effect as illustrated in Fig. 11. The nephelauxetic effect, is responsible for the so-called centroid shift ϵ_c of 5d-energy.²⁶ The increase of centroid shift with decreasing $U(6, A)$ is about the same as the increase of chemical shift, and as a result the average VRBE of the

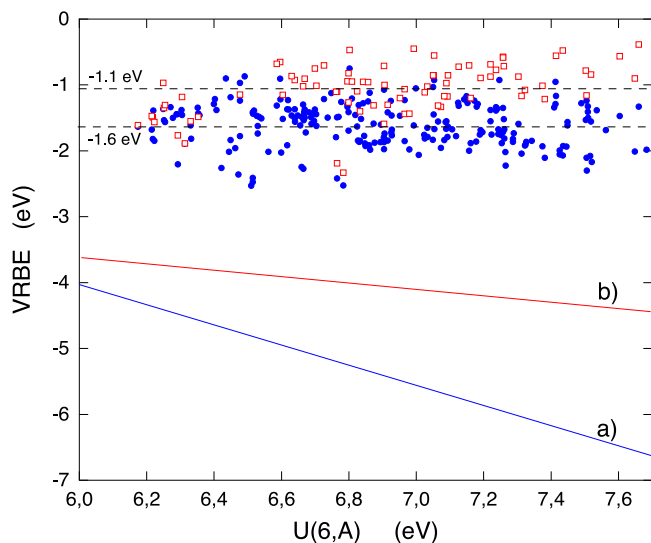


Figure 10. The VRBE in the (curve a) Ce^{3+} and in the (curve b) Eu^{2+} 4f ground state. Solid data symbols are the VRBE in the lowest energy Ce^{3+} 5d state with compound average VRBE of -1.6 eV, and open symbols in the lowest energy $4f^65d$ state of Eu^{2+} with compound average VRBE of -1.1 eV. Data on 225 compounds were used.

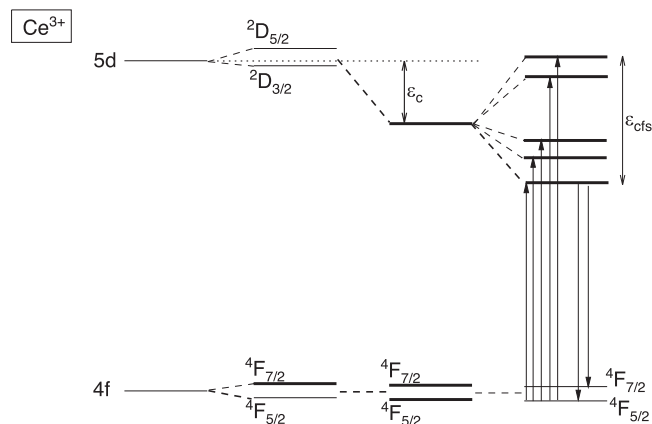


Figure 11. The level scheme for Ce^{3+} . The spin orbit split $2D$ levels of Ce^{3+} are lowered by the centroid shift ϵ_c and depending on site symmetry split into at most five 5d levels. ϵ_{cfs} is the difference between lowest and highest energy 5d level.

five 5d-levels appears almost invariant with type of compound. This means that the compound to compound variation in the VRBE in the lowest energy 5d-level shown with the data in Fig. 10 is caused by compound-to-compound variation in the 5d crystal field splitting ϵ_{cfs} .

Clearly for Bi^{3+} , both the $6s^2$ ground state and $6s6p$ excited state orbitals extend to the outside of the cation and both will have strong interaction with the anion ligands which makes VRBE interpretation more complex than with Ce^{3+} . Figure 5 shows that the VRBE in the 3P_1 excited state increases less strongly than that in the 1S_0 ground state when $U(6, A)$ decreases. The A-band energy decreases as shown in Fig. 6, and this is the same trend as can be seen in Fig. 10 for the energy difference between the Ce^{3+} ground state (curve a) and the lowest energy 5d-state (solid data symbols).

The VRBE in the $6s^2 6p$ ground state of the free ion Bi^{2+} is -25.5 eV and this is almost the same as -24.92 eV for Eu^{2+} (see Eq. 1). Figure 7 shows that in compounds the Bi^{2+} ground state VRBE is found around -4 to -3.5 eV and this is at most a few 0.1 eV above that for Eu^{2+} in Fig. 10. The variation in ground state VRBE with $U(6, A)$ -value is like curve b) in Fig. 10 for Eu^{2+} rather mild. Unlike the A-band of Bi^{3+} there appears no decreasing trend in energy difference between ground and excited Bi^{2+} states with decreasing U -value. This suggests that compound-to-compound variations are related with changing crystal field splitting and spin orbit splitting of the Bi^{2+} levels, see also Fig. 3. Data are actually too few to enter into a detailed discussion on the relation between structure and chemistry of compounds and the wavelength of Bi^{2+} emission.

In Fig. 5, the VRBE in the Bi^{3+} ground state appears always above the top of the VB formed by the anion. Extrapolating toward 100% Bi^{3+} concentration suggests that the top of the VB in pure Bi-compounds will largely be determined by the $\text{Bi}^{3+} 6s^2$ cation orbitals rather than the anion orbitals. Indeed the VRBE at the VB-top in the pure Bi-compounds of Fig. 8 appears at similar energy as that in the Bi^{3+} ground state in Bi^{3+} doped compounds in Fig. 5. With decreasing U -value it decreases from just above -10 eV in BiF_3 to around -6 eV in CaSe . The flatband potential of the pure Bi-compounds in Fig. 8 is always near -4 eV and this is then consistent with the VRBE of around -3.6 eV in the ground state of Bi^{2+} as dopant in the compounds of Fig. 7.

The La-compounds in Fig. 9 are, when doped with 100% Bi^{3+} , regarded to be similar as the Bi-compounds in 8. Curve c) in Fig. 9 connects the VRBE at the VB-top of those Bi-compounds. For the oxide and halooxide compounds, curve c) runs close above the VB-top which suggest that the VB-top in the equivalent Bi-compound is likely to be of mixed cation anion orbital character. For the two fluoride compounds there is about 2 eV difference which then suggest that the VB-top in the fluorides is dominated by the

Bi^{3+} ground state orbitals. In LaI_3 and La_2S_3 the situation is reversed. This suggests that Bi increases the bonding in the anion thus lowering E_V . Computational methods can provide more detailed insight. Curve b) representing the flatband potentials and curve c) in Fig. 9 is usually well below the CB-bottom of the La-compounds and then the CB-bottom in the Bi-compound will be formed by Bi^{2+} orbitals. However in case of Y_2WO_6 , LaTaO_4 , LaNbO_4 , and LaVO_4 we deal with a low lying CB-bottom formed by the transition metal d-orbital states. Curve b) is now close to that CB-bottom, and the CB-bottom is likely of mixed $\text{Bi}^{2+} 6s^2 6p$ and transition metal d-orbital type. Indeed computational methods show that the CB-bottom in BiVO_4 and also Bi_2WO_6 is dominated by $V^{4+} 3d$ and $W^{5+} 5d$ -orbitals.^{10,61,106}

The parameter $U(6, A)$ is the energy difference between the ($\text{Eu}^{2+}/\text{Eu}^{3+}$) and ($\text{Eu}^{3+}/\text{Eu}^{4+}$) charge transition levels and varies from 7.6 eV down to 6.0 eV in a predictable fashion. One may compare this with the energy difference U_{Bi} between the ($\text{Bi}^{2+}/\text{Bi}^{3+}$) and ($\text{Bi}^{3+}/\text{Bi}^{4+}$) charge transition levels. Figure 8 suggest about 4.5 eV for fluorides compounds, 3.7 eV in YPO_4 in Fig. 4, and 2.8 eV for Bi_2O_3 in Fig. 8 and possibly even lower values in sulfide and selenide compounds. The trends are the same as with $U(6, A)$.

The interpretation of the spectroscopy of Bi^{3+} in compounds has always been difficult and controversial, and it often still is. Special about Bi is that both the ($\text{Bi}^{3+}/\text{Bi}^{4+}$) and ($\text{Bi}^{2+}/\text{Bi}^{3+}$) charge transition levels are found inside the forbidden gap of wide band insulators. Furthermore the Bi^{3+} excited state is usually above and in any case near the Bi^{2+} ground state. One may then in principle observe three broad electron transfer bands in a Bi^{3+} doped compound, i.e., the $\text{VB} \rightarrow \text{Bi}^{3+}$ electron transfer band, the $\text{Bi}^{3+} \rightarrow \text{CB}$ electron transfer band and, when Bi^{3+} ions are nearest neighbors, the $\text{Bi}^{3+} \rightarrow \text{Bi}^{3+}$ electron transfer band. Each electron transfer can be followed by broad band charge transfer emission. Without detailed knowledge on the location of the charge transition levels, assignment of the broad bands remains speculative. The quenching of Bi^{3+} emission may proceed via thermal ionization of an electron to the CB but also by thermal ionization of a hole to the VB, see Fig. 3 and again the location of the charge transition levels is detrimental for which quenching route prevails.

Conclusions

The chemical shift method of VRBE scheme construction combined with spectroscopy on Bi^{3+} and Bi^{2+} enables to derive the electron VRBE in the divalent and trivalent Bi-levels. When compounds are organized in order of decreasing $U(6, A)$ -value, which means increasing nephelauxetic effect, increasing polarizability of the anions, and increasing co-valence, clear systematics appear as shown in Fig. 5 and Fig. 7. Just like Ce^{3+} , the ground state VRBE increases with smaller value for U . A smaller cation charge leads to less dependence of VRBE on type of compound. This is known for Eu^{2+} as compared to Ce^{3+} as can be seen in Fig. 10, but this work confirms the same for Bi^{2+} compared to Bi^{3+} . One may then roughly estimate the VRBE energies in the Bi^{2+} and Bi^{3+} ground states from the composition of the compound beforehand. In lanthanides the 4f-orbital is shielded and electron VRBE is hardly affected by the nephelauxetic effect and crystal field splitting. This is different for bismuth where the $6s^2$ and $6s^2 6p$ orbital extends to the outside of the atom and more compound-to-compound variation in Bi ground state VRBE results.

This work also shows that knowledge on the VRBE in Bi doped compounds can be transferred to pure Bi-compounds. Here we see in Fig. 8 the same systematics. The VB-top raises with smaller U -value like the Bi^{3+} ground state VRBE in Fig. 5 and the flatband potential is fairly constant -4 to -3.5 eV just like that of the Bi^{2+} ground state VRBE in Fig. 7. Transition metals like V^{5+} , Nb^{5+} , Ta^{6+} or W^{6+} have a low lying CB-bottom near -3 eV to -4 eV where also the VRBE of the Bi^{2+} ground state usually appears as can be seen in Fig. 9. In compounds like BiVO_4 and Bi_2WO_6 , CB-bottom is then likely to be of mixed transition metal and bismuth character.

In this work we used information from different disciplines of science and different techniques to deduce and compare VRBEs. The refined chemical shift model exploits the systematics in lanthanide spectroscopy to derive VRBE in the lanthanide levels but also at the VB-top and CB-bottom. Results from photoelectric effect studies and photoelectron spectroscopy were used. Results from electrochemical determination of flatband potentials were used for the pure Bi-compounds. Spectroscopy of Bi^{3+} and Bi^{2+} emission was used and findings from thermoluminescence spectroscopy involving bismuth and lanthanide dopants. In addition the empirical method of absolute semi-conductor electronegativity has been addressed. Each technique has its own shortcomings, systematic errors, and own family of compounds where it has been applied to. Yet a consistent picture emerges with clear trends in VRBE energies. This work hopefully has demonstrated that knowledge and techniques from different disciplines of science can be joined to reach better insight in bismuth related materials properties. One important criterion is then to use the vacuum level as the common reference of energy.

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